



Study of Wakefields and Methods for Their Reduction in an Energy Recovery Linac

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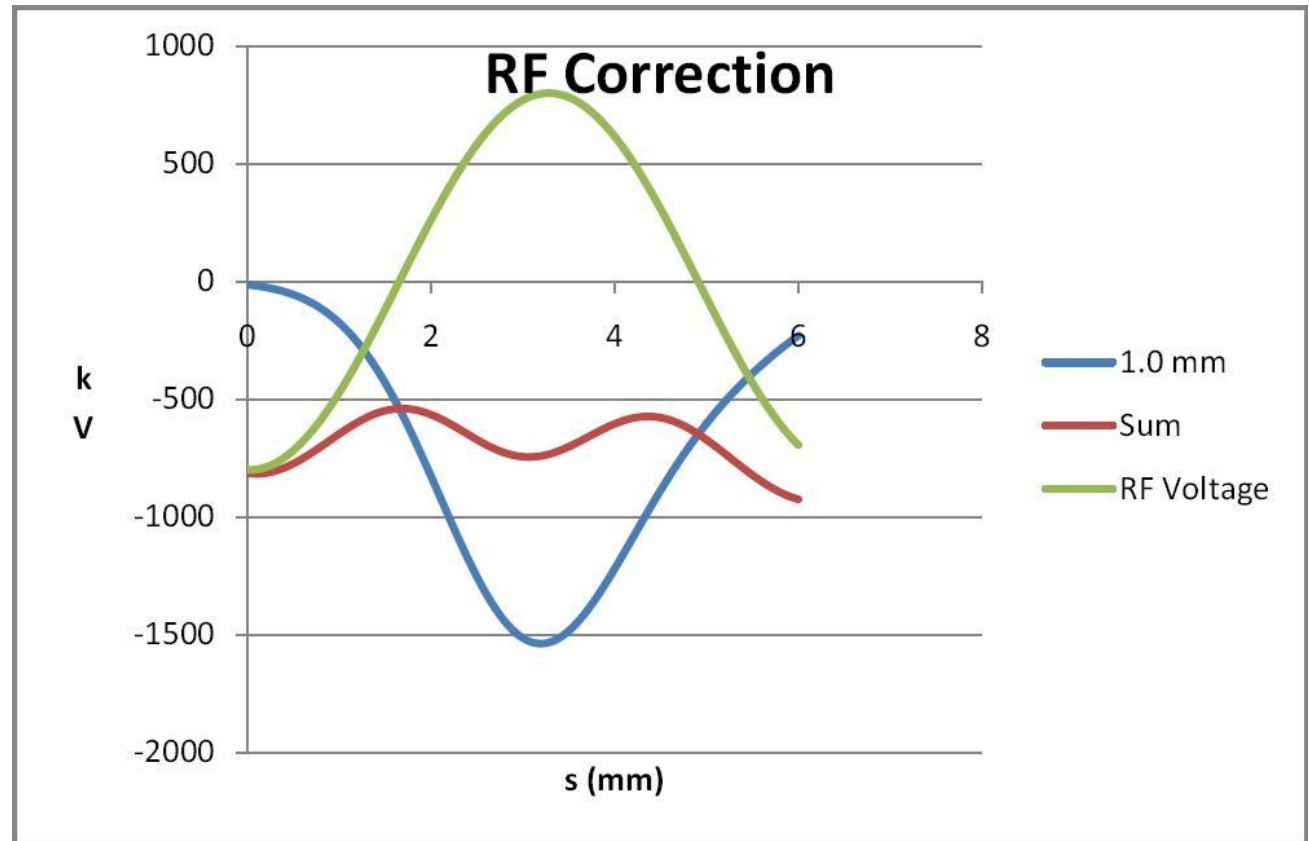
Laboratory for Elementary-Particle Physics



- The ERL is valued for its efficiency and capability to produce bright x-rays and short x-ray pulses.
- Wakefields can be obstructions that do not allow the ERL to achieve it's full potential:
 - Wakefields adversely affect energy spread.
- Energy recovery can be used via “dielectric power extractors” to mitigate wakefield effects.
- Design-oriented project focused on implementation of a “dielectric power extractor” in a two beam acceleration scheme.



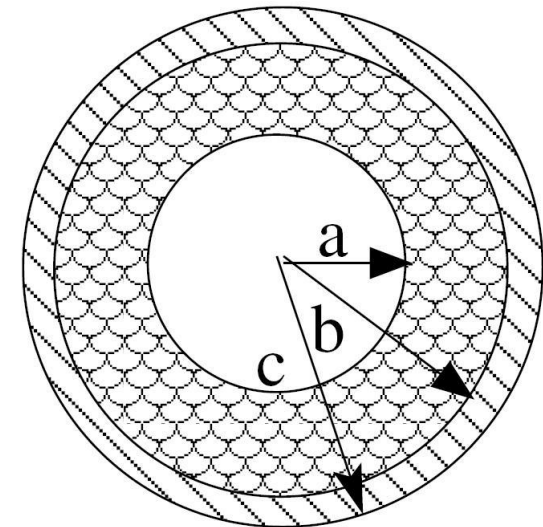
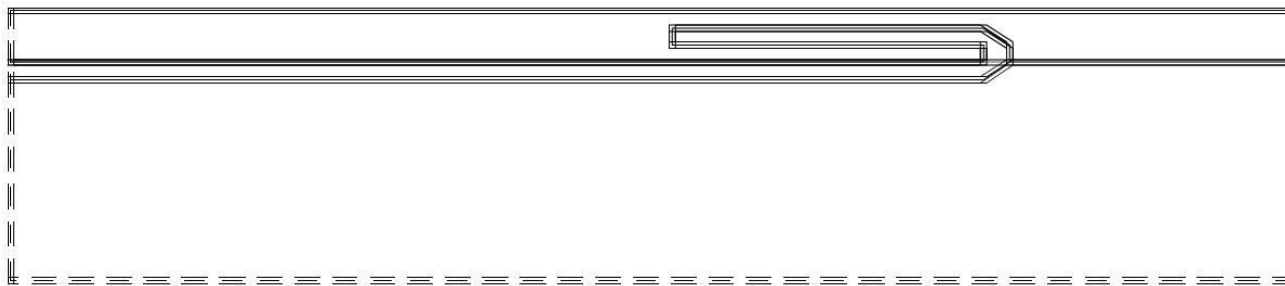
If it were possible to superimpose an RF voltage with an erroneous wakefield, one could improve bunch energy spread while accelerating the beam.



Goal - Frequency: 45 GHz, Amplitude: 1.6 MV



- Tested at Argonne National Laboratory.
- Cylindrically symmetric structure that has a thin lining of dielectric.
- Couplers attached to the endpoints of the dielectric layer

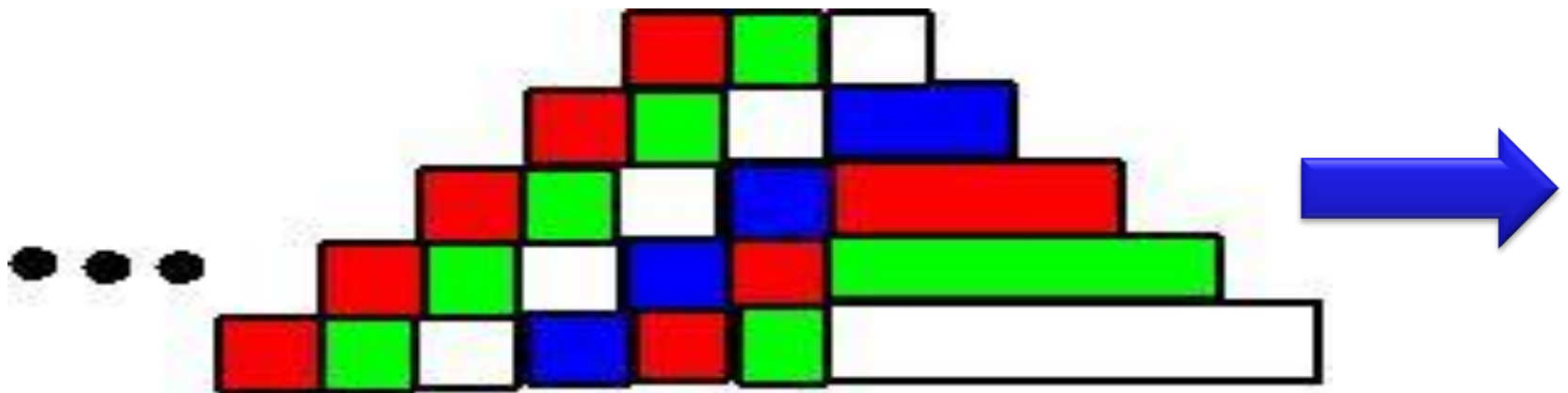




1. The first bunch in a series of bunches traversing through the pipe at frequency ω enters the dielectric power extractor.
2. The bunch excites a wakefield at a specific mode based on the design of the structure.
3. The voltage is a function of the adjusted resonance frequency, the loaded quality factor (assume matched impedance condition), and the loss factor. The RF pulse propagates at a group velocity slower than the bunch velocity (assumed ideally relativistic).
4. The RF pulse is decays as the bunch leaves the dielectric power extractor.
$$V_{RF} = 2k(\omega'_{RF})q\cos(\omega'_{RF}t)e^{\left[-\frac{\omega'_{RF}t}{2Q_{loaded}}\right]}$$
5. While the RF pulse is still propagating within the dielectric power extractor, a subsequent bunch enter the structure and excites its own RF pulse that superimposes with the tail of the existing RF pulse.



- The wakefields extracted from neighboring bunches interfere constructively, producing a flat-top amplitude.





- In order for the RF pulses to interfere constructively, the power extracting mode must be a harmonic of the bunch frequency.
- The desired frequency can be calculated as follows:

$$n = \left\lfloor \frac{Q_{loaded} \omega}{\omega_{RF}} \right\rfloor$$
$$\omega'_{RF} = \frac{2Q_{loaded} \omega}{n}$$

- Simulations suggest that by adjusting the coupler length, one can achieve a tuning range of ~200 MHz.



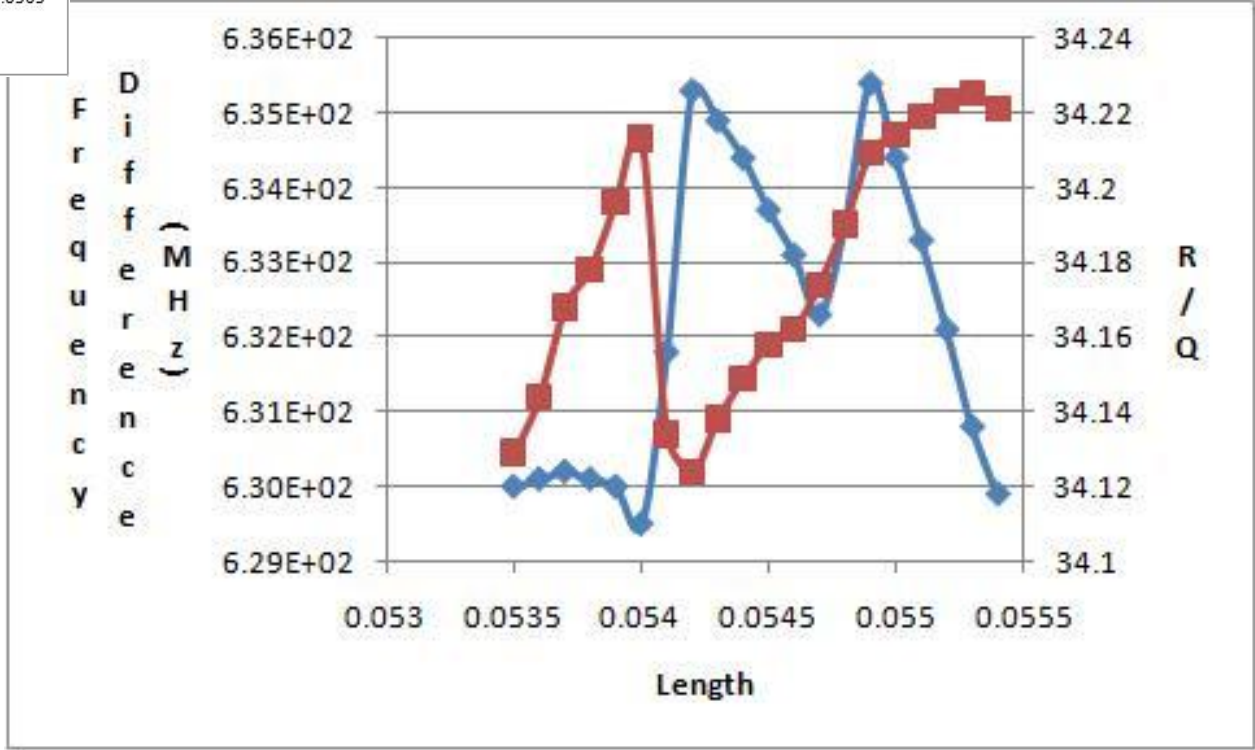
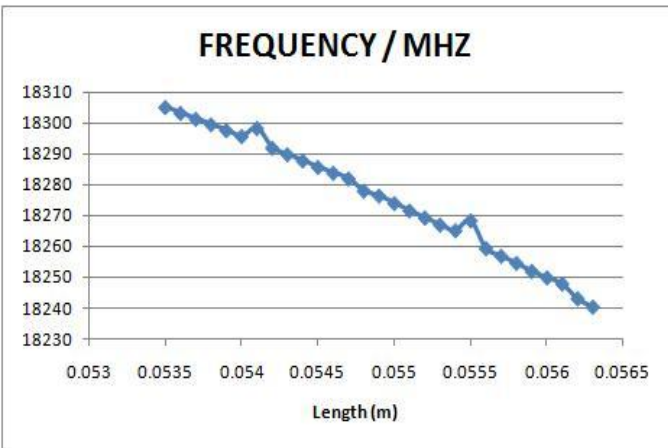
- Attempted to optimize dielectric power extractor design by varying:
 - Dielectric layer length
 - Coupler length
 - Dielectric layer thickness
 - Taper length
- All parameters were varied independently and sequentially.
- Desirable features for a given mode were spatial localization, a high R/Q , and a high Q .



- Frequency inversely related to length.
- When the R/Q for a given mode is maximized, the neighboring modes are more spread apart in frequency
- R/Q varies sinusoidally as the length of the couplers are varied
- The Q for a particular mode decreases as length increases



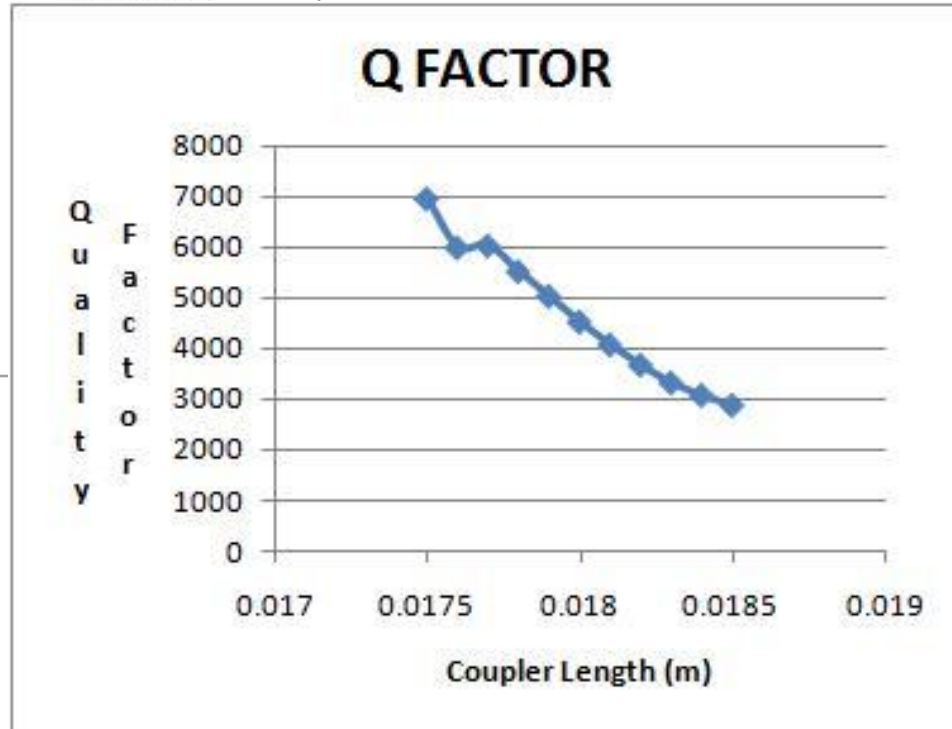
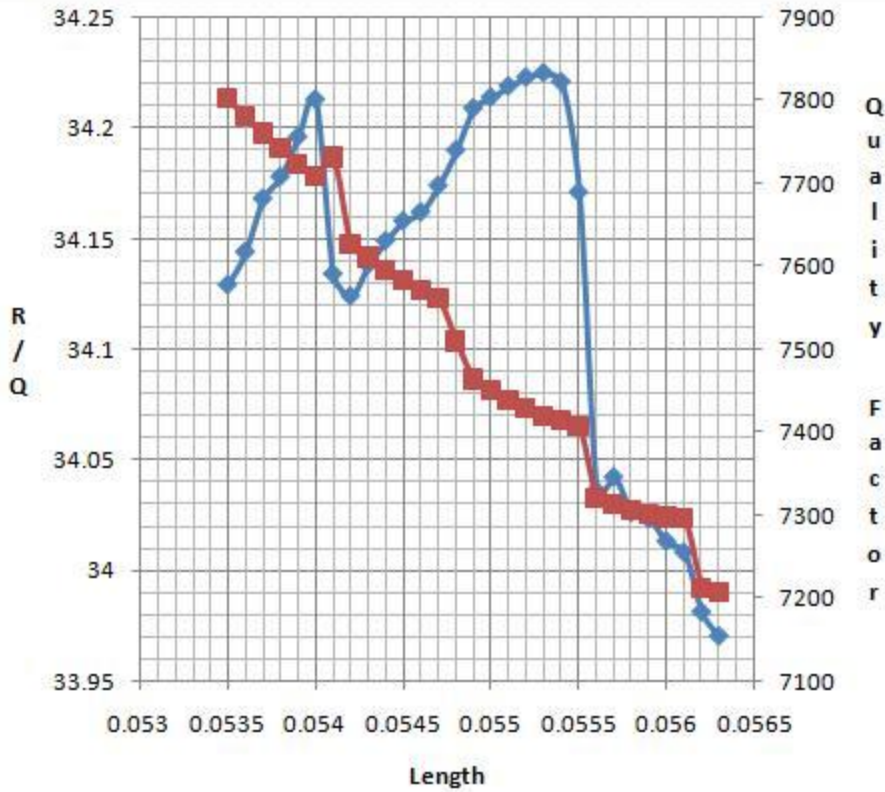
Length Variation



Trend discontinuities most probably explained by mesh allocation within dielectric

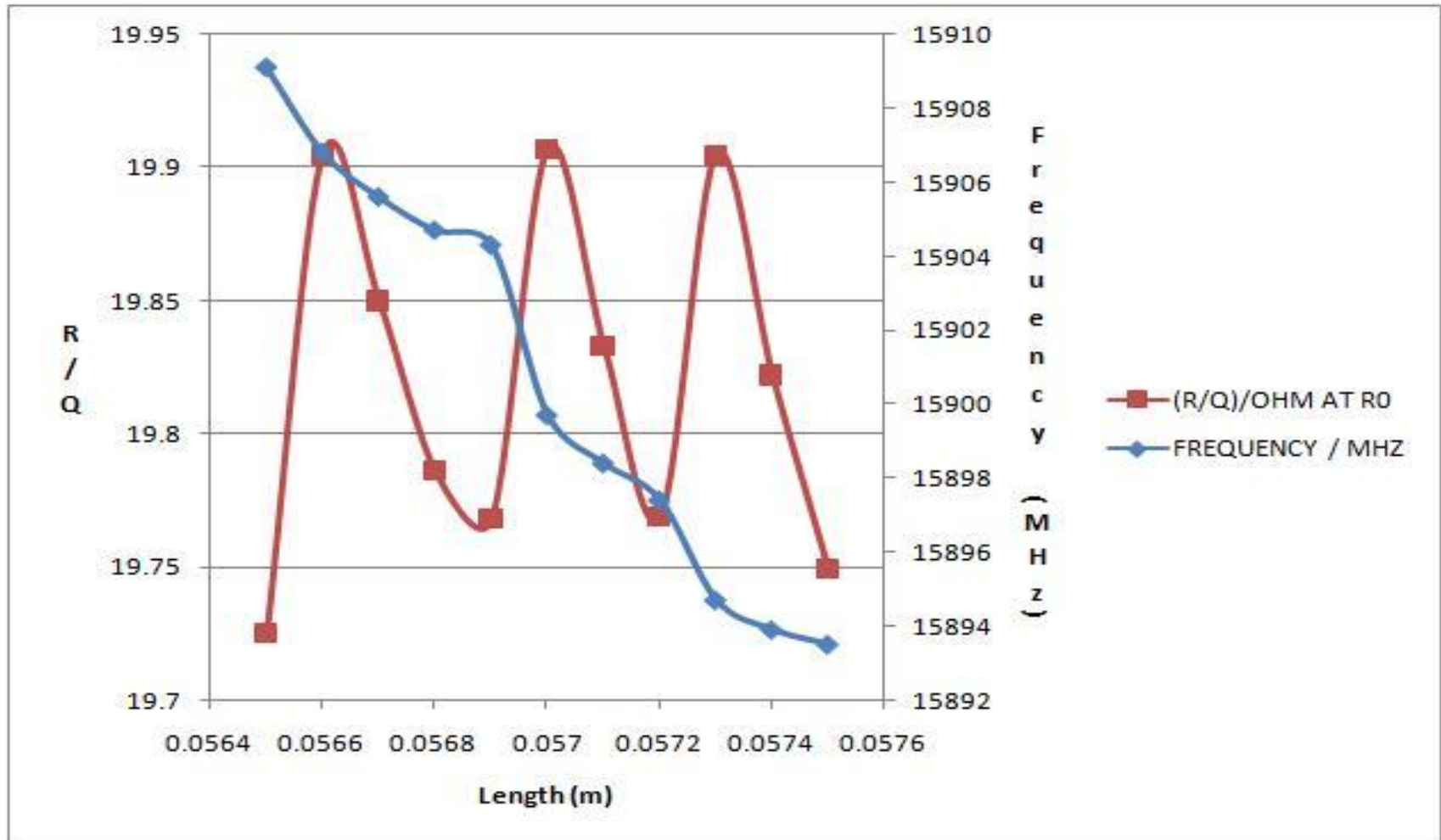


Q Factor Trend





R/Q Sinusoidal Behavior

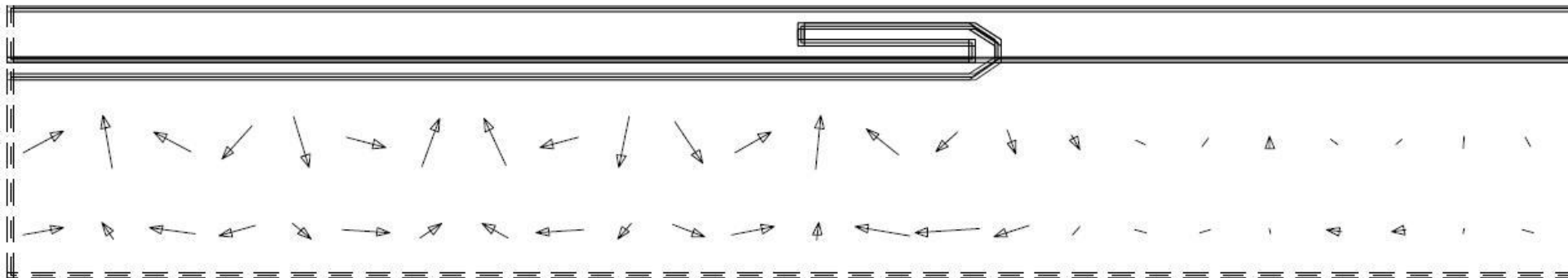


Demonstrates tuning plausibility (able to maintain R/Q while adjusting frequency within a ~200 MHz range)



- Trapped modes found only when couplers were attached.
- Dielectric discontinuity was not enough (so far) to localize modes

Dielectric Length	Coupler Length	Frequency (GHz)	R/Q	Q-Factor
0.114 m	0.011 m	15.07	21.016	3848





- Calculations for the TBA scheme were done for the “optimal” mode.

Tuned Frequency	Peak RF Voltage
15.31 GHz	7.164 kV

- Required frequency within tuning range
- At least 2×140 dielectric power extractors are needed (i.e. $\sim 2 \times 21 = 42$ meters of structure)
- Additional power extractors will be needed to account for attenuation in lossy walls.
- Bunch length will have to be adjusted



- The use of a dielectric power extractor to accelerate and decelerate the beam has much potential.
- Higher order modes with even more outstanding qualifications may exist but could not be searched for due to software limitations and time constraints.
- Notable discoveries:
 - Tuning the power extractor via minute length adjustments is feasible
 - Couplers play an important role in localizing modes



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