

# Top Jets & Boosted QCD Jets @ the LHC

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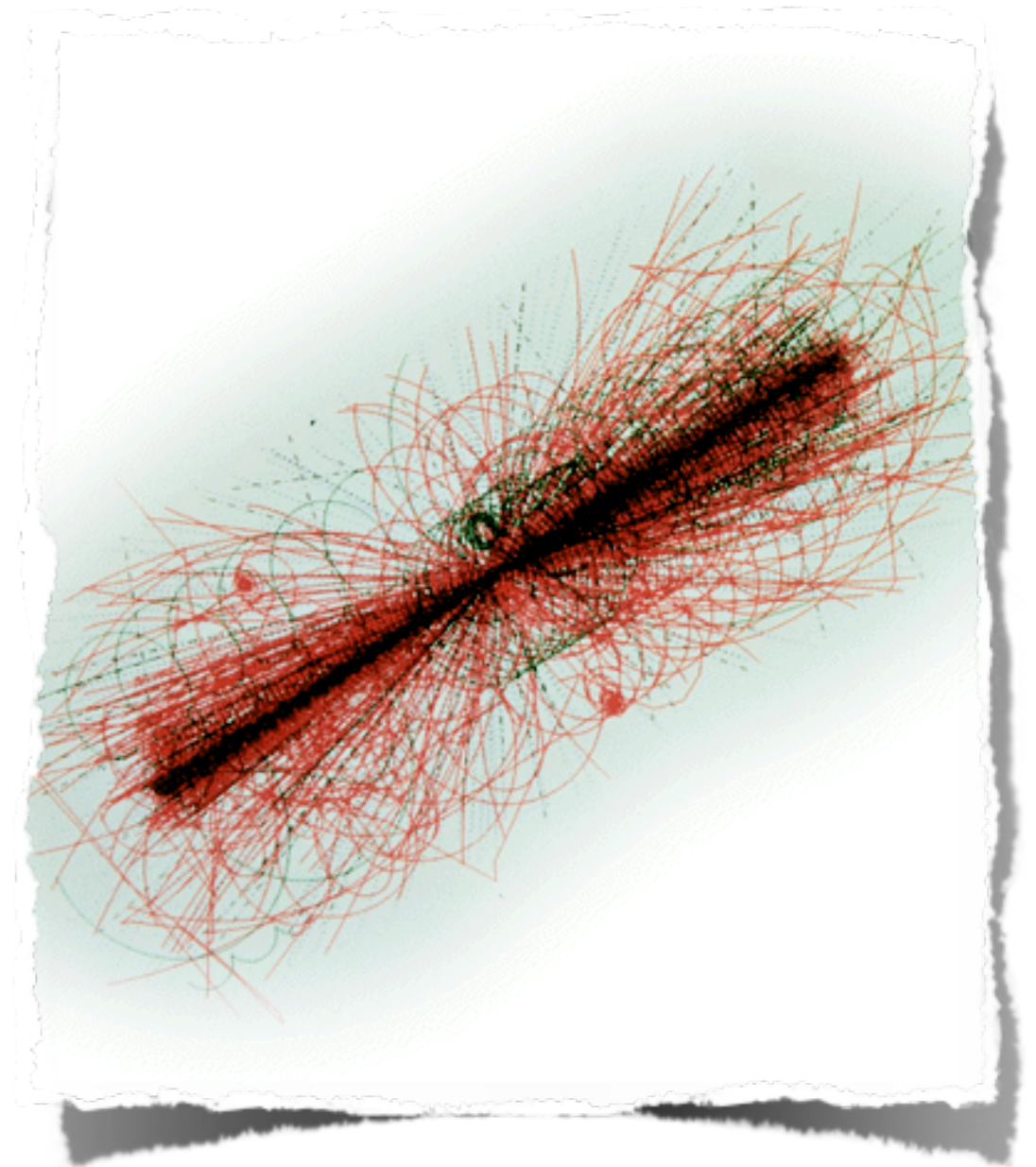
arXiv:0807.0234, work in preparation

Cornell University, September 3, 2008

# Outline

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- ◆ Introduction
- ◆ Emergence of high  $p_T$  top (W,Z,h) jets at the LHC
- ◆ Jet mass: Signal & QCD BG (theory+MC)
- ◆ Jet substructure, massive jet event shapes
- ◆ Top polarization
- ◆ Summary



# Introduction

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- ◆ In the SM (& beyond) top is unique:
  - only ultra heavy quark,  $m_t \sim \langle H \rangle$
  - induce most severe fine tuning;
  - controls flavor & custodial violation;
  - linked to EW breaking in natural models.

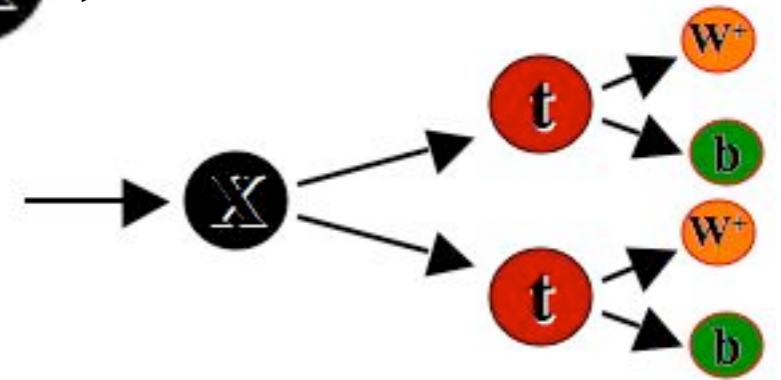
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  - controls flavor & custodial violation;
  - linked to EW breaking in natural models.
- ◆ Direct info' is limited (Tevatron)
- ◆ At the LHC:  $10^7$  top/yr
- ◆ SM: more than  $10^4$  top/yr with  $\gamma_t \geq 5$ .

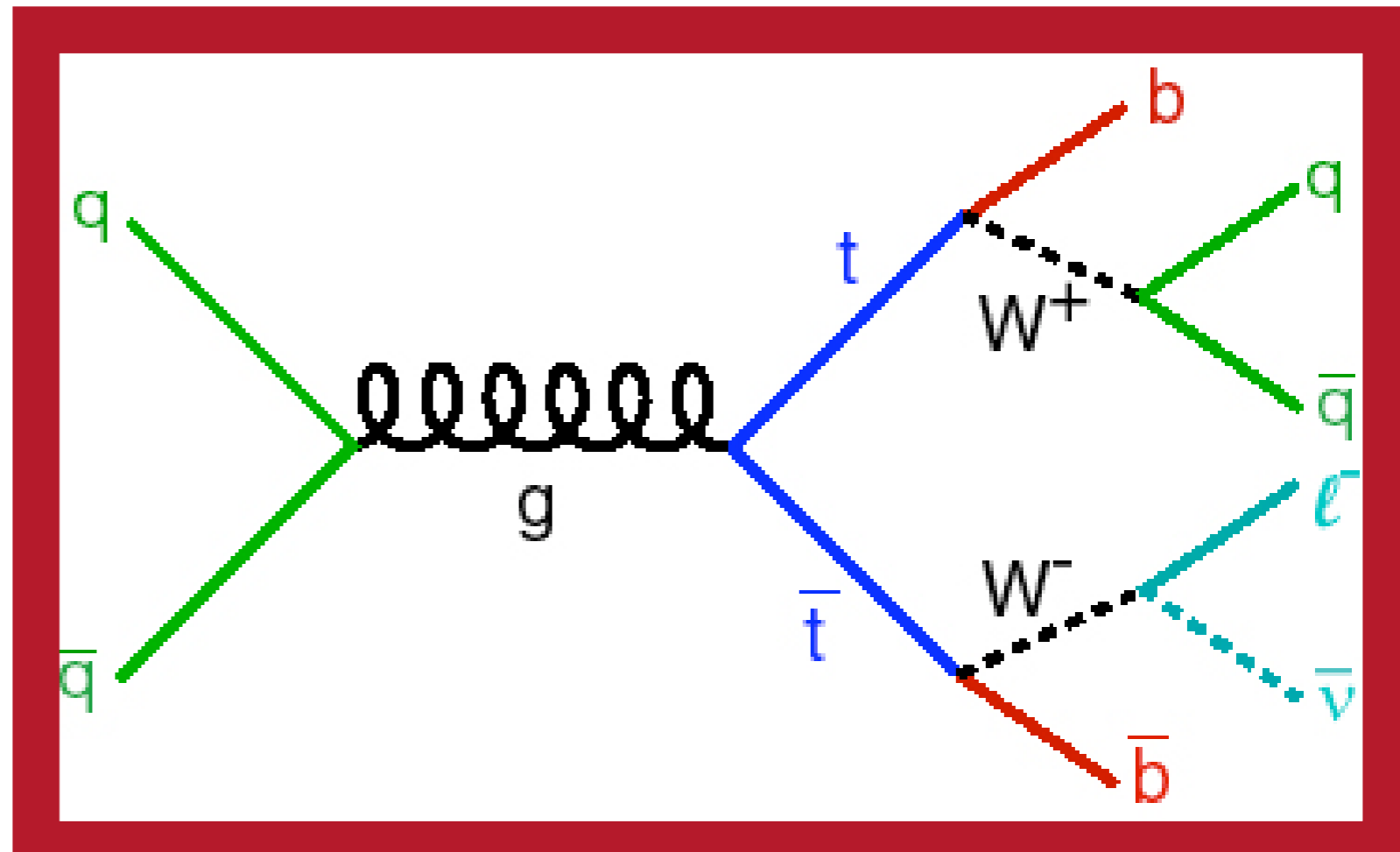
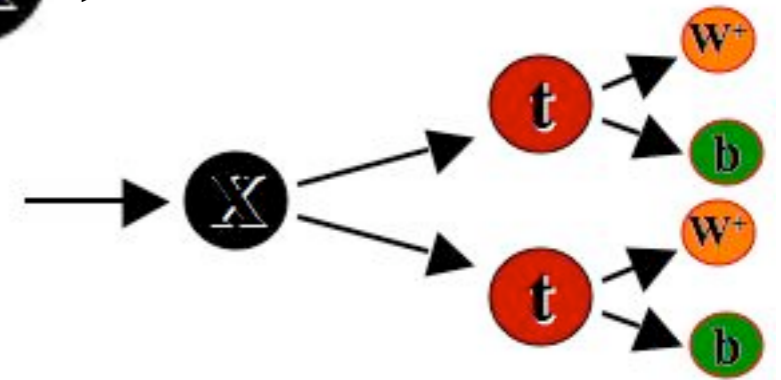
# The challenge of highly boosted tops

- First, let's consider NP particle  $X$ , whose dominant decay channel is  $t\bar{t}$ :  $X$  might be heavy



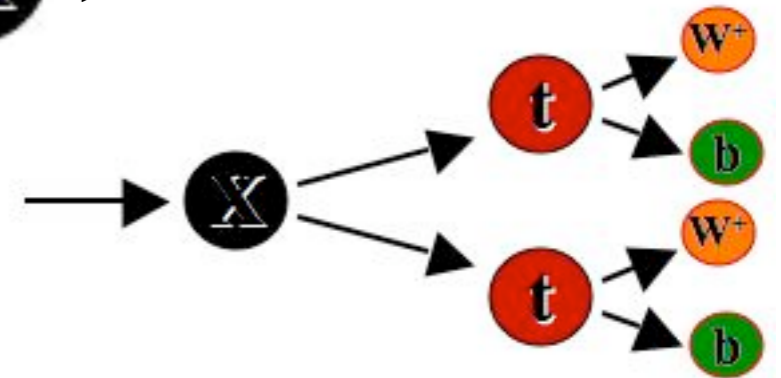
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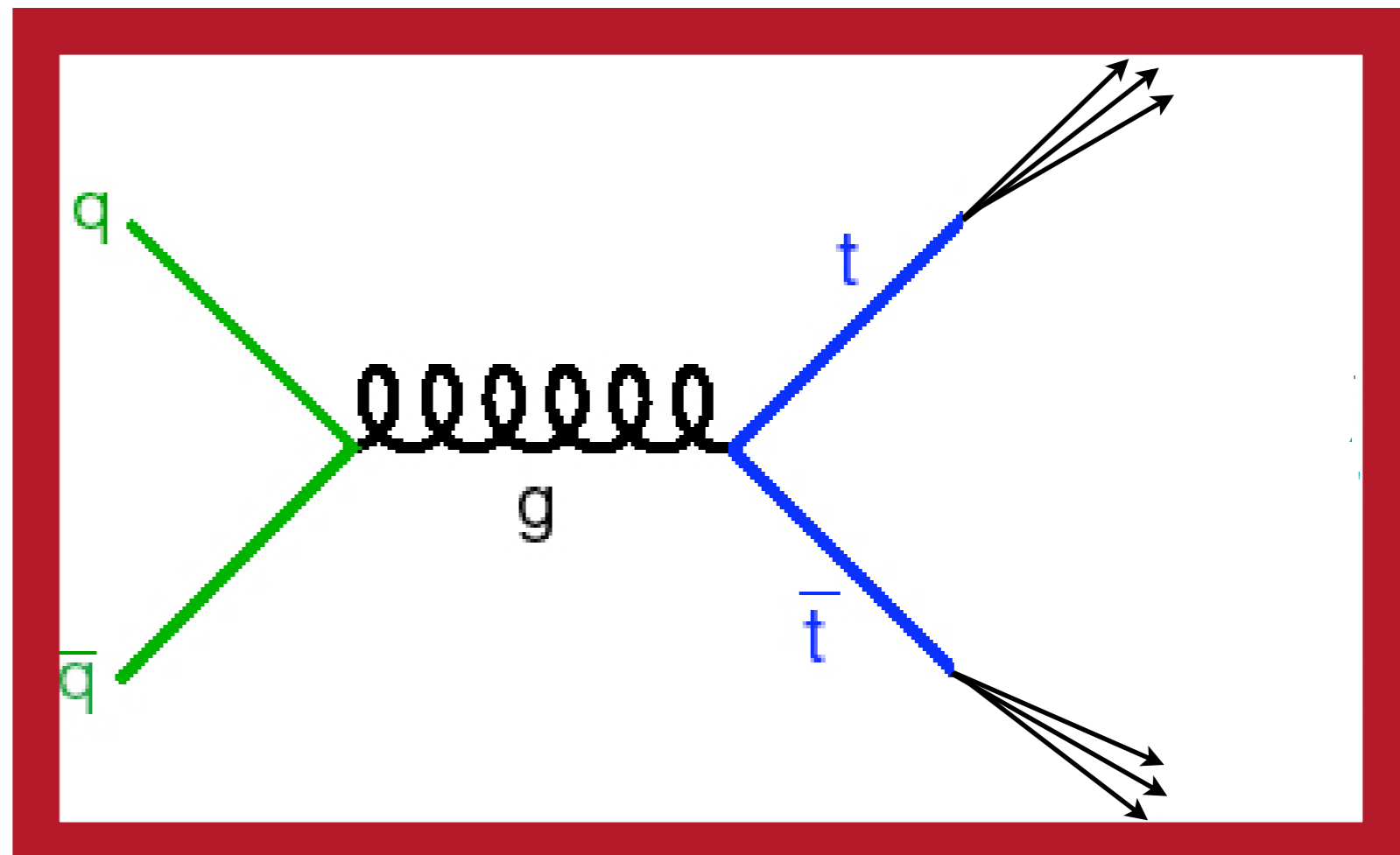


# The challenge of highly boosted tops

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- ◆ Alas, above a TeV, top becomes similar to a light jet, signal is **lost**!

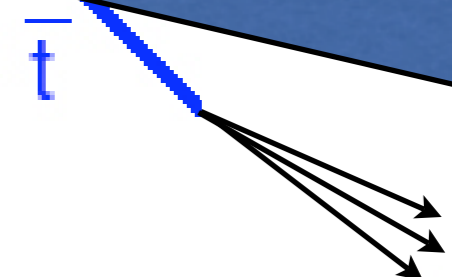
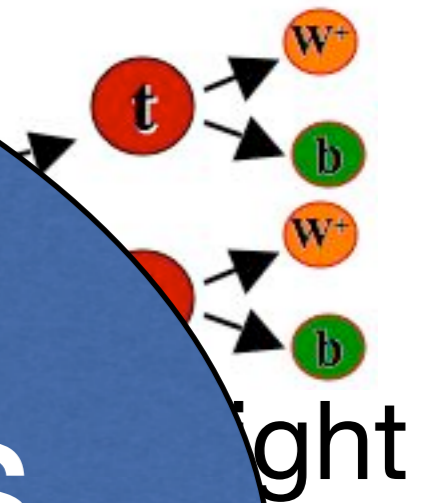




# The challenge of highly boosted tops

- First, let's consider  $t\bar{t}$  production  
whose decay is  $t \rightarrow W^+ b$  and  $\bar{t} \rightarrow W^- \bar{b}$

New object emerges,  
top jet!





# Resolution problem \w boosted tops

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- ◆ The hadronic calorimeters cannot go below  $R \sim 0.4$

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**Why:** Hadronic granularity is  $R \sim 0.1 \times 0.1$

$$m^2 = (p_1 + p_2)^2 \sim 2p^2 [1 - (1 - R^2/2)] = p^2 R^2$$

pure geometrical mass:  $m \sim R p$

(say with  $R, p = 0.2, 500$ ,  $m \sim 100\text{GeV}$ )

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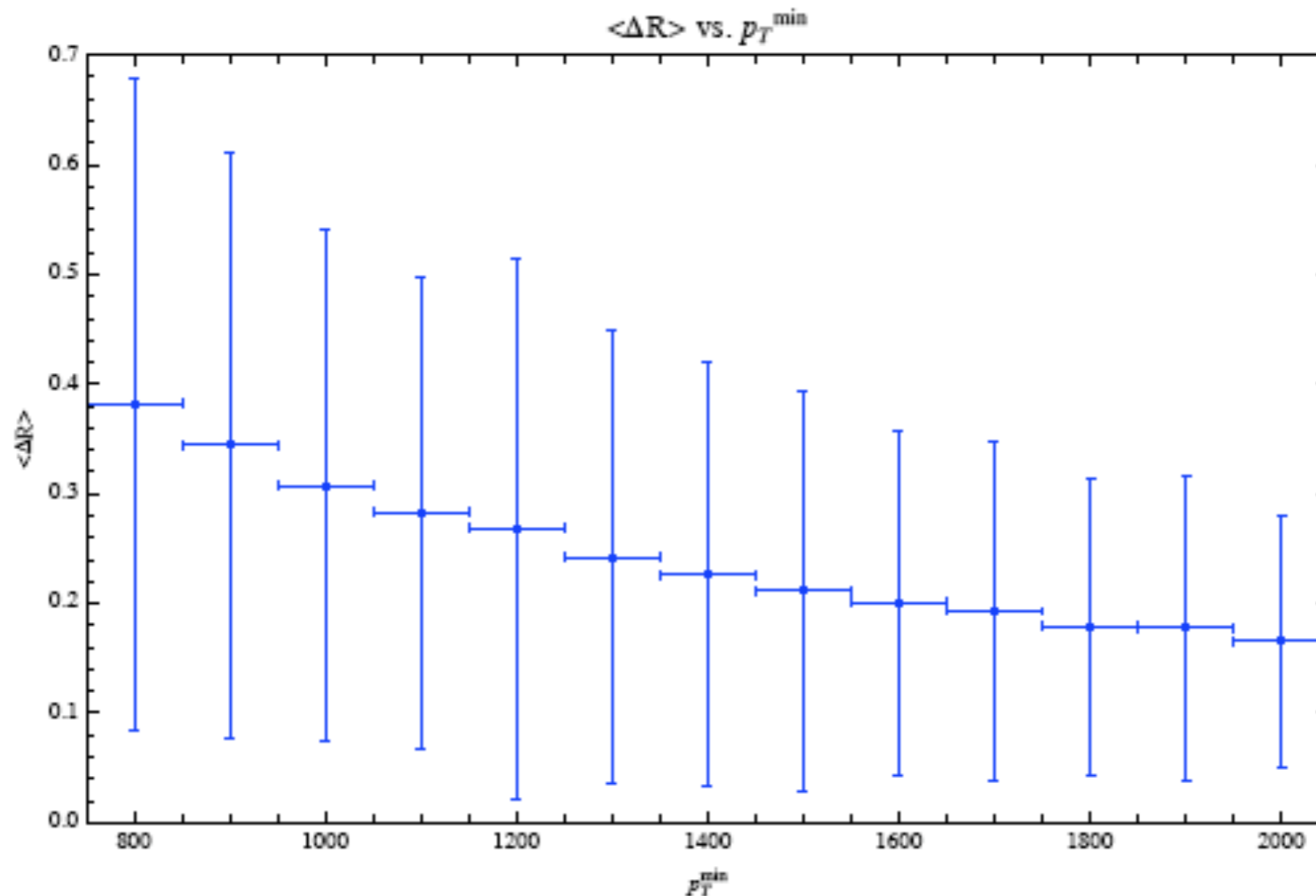
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- ◆ If  $R$  between decay products of top is smaller than 0.4, you cannot resolve the top into daughter jets. (top jet = single jet)

# Boosted top (w/z/h) jets & collimation



Partonic  
Level

Highly Boosted Tops:  
High Collimations!

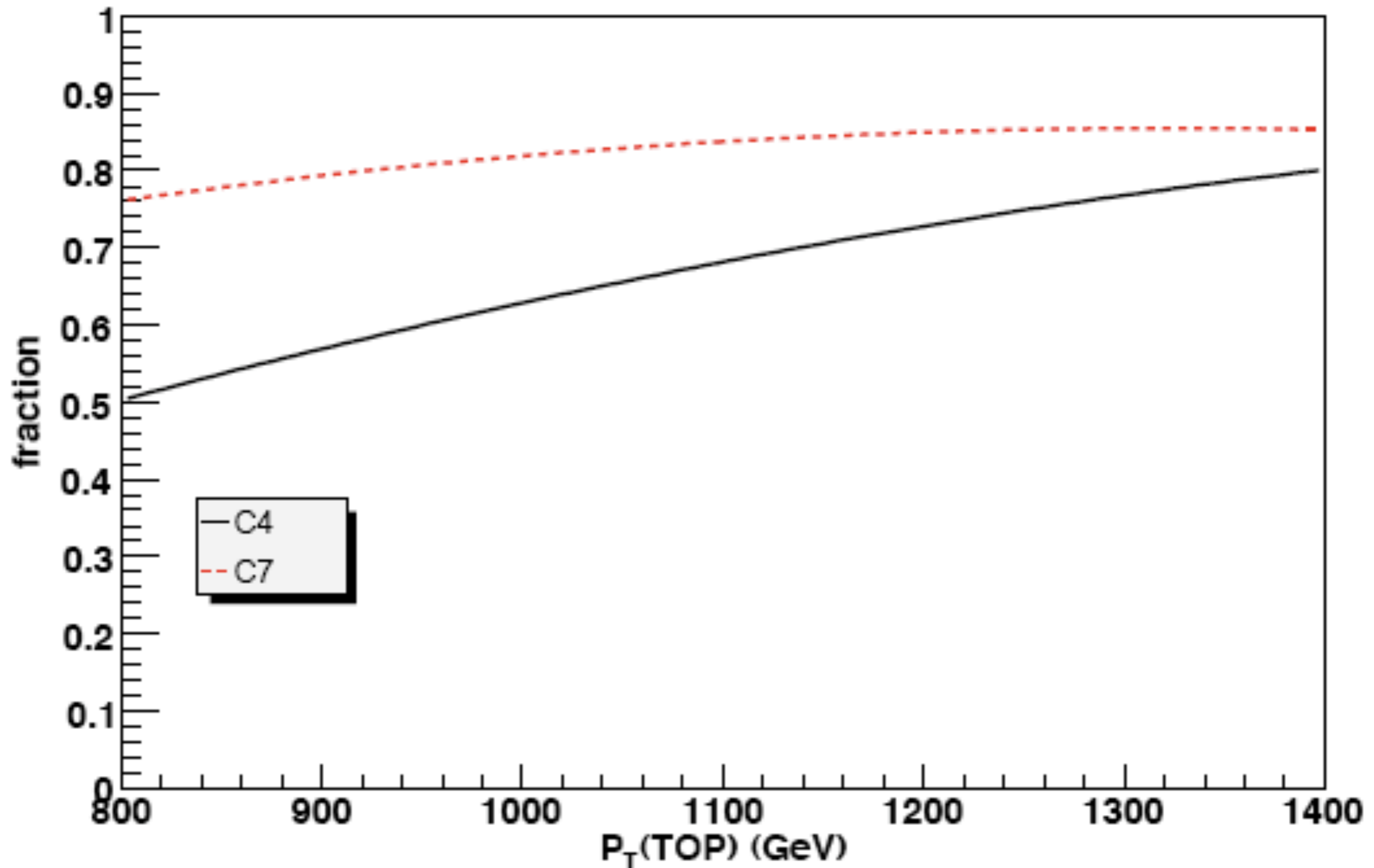
$\Delta R$  vs.  $P_T$

$$\Delta R = \sqrt{\Delta\eta^2 + \Delta\phi^2}$$

# Boosted top (w/z/h) jets & collimation

Collimation Rate

Final state Jets Level

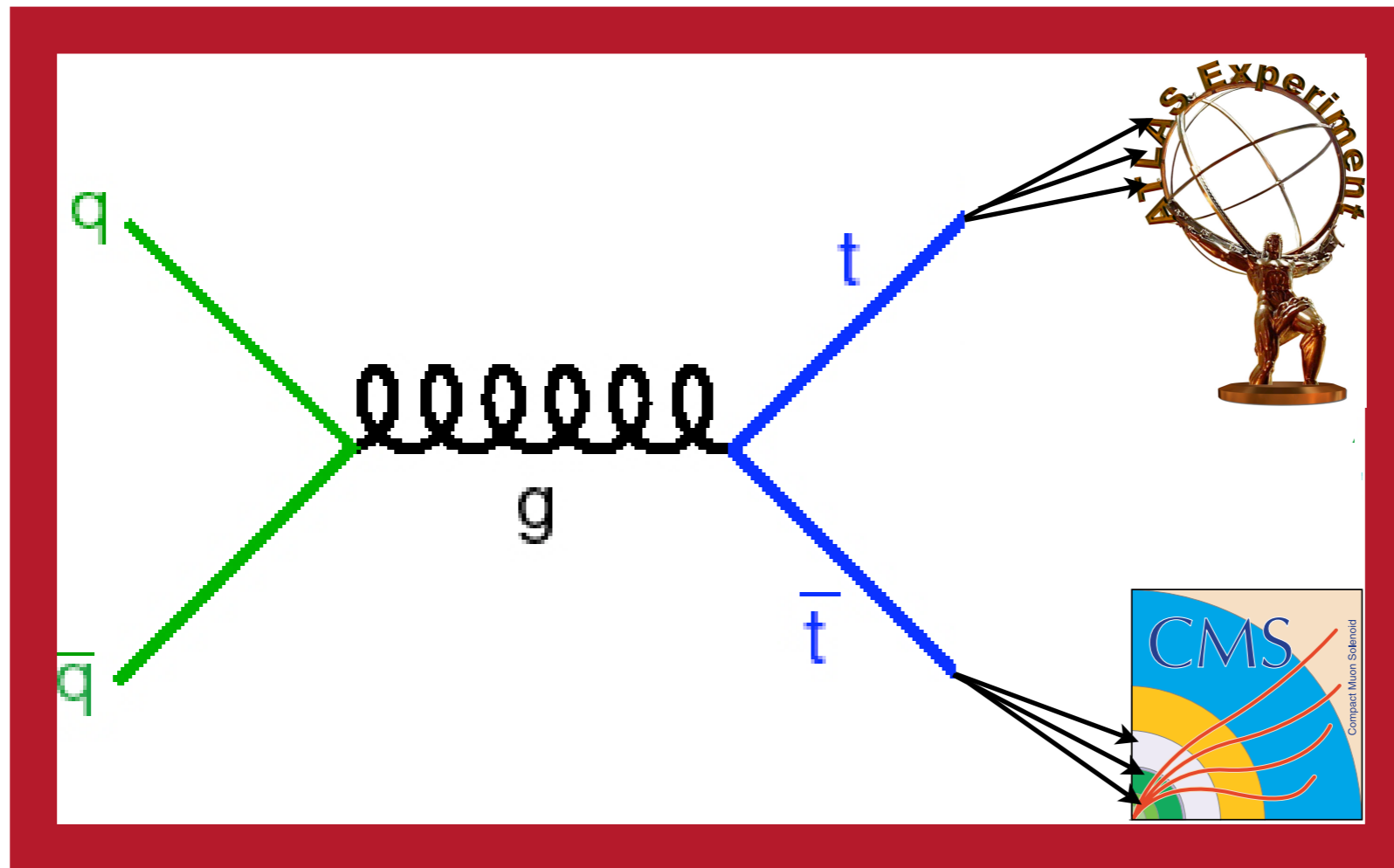


# Top jets at the LHC

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- (i) Jet mass.
- (ii) Jet substructure.



# Top-jets @ the LHC

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◆ Are they different from high  $p_T$  light jets?

$S/B \sim 1/140$ , for  $p_T(j) > 1000$  GeV,  $R=0.4$   
( $\sim 20$  pb for  $jj+X$ ,  $\sim 140$  fb for  $t\bar{t}+X$ )

◆ **top-jet**: call for theory, analysis & techniques

Most (naive) direct attempt - mass tagging

*Skiba & Tucker-Smith, PRD(07); Holdom, JHEP (07); Frederix & Maltoni (0712.2355); Ellis, Huston, Hatakeyama, Loch & Tonnesmann, PPNP (08); Agashe et. al. PRD(07).*

# Rejection based on jet mass

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- ◆ **Jet cone mass**-sum of “massless” momenta in h-cal inside the cone:  $m_J^2 = \left(\sum_{i \in R} P_i\right)^2$ ,  $P_i^2 = 0$
- ◆ Jet cone mass is non-trivial both for S & B
- ◆ Understand S&B distributions from 1st principles & compare to MC “data”
- ◆ Add detector effects

# Cone top-jet mass distribution

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- ◆ Naively the signal is  $J \propto \delta(m_J - m_t)$
- ◆ In practice:  $m_J^t \sim m_t + \delta m_{QCD} + \delta m_{EW}$   
+ detector smearing.

$$J^t(m_J, m_t, R, p_T) \sim \int dm_{QCD} dm_{EW} dm_0 \delta(m_0 - m_t) \delta(m_J - m_{QCD} - m_{EW}) \times \\ J_{QCD}^t(m_{QCD}, R, p_T) \times J_{EW}^t(m_{EW}, m_t/(p_T R)).$$

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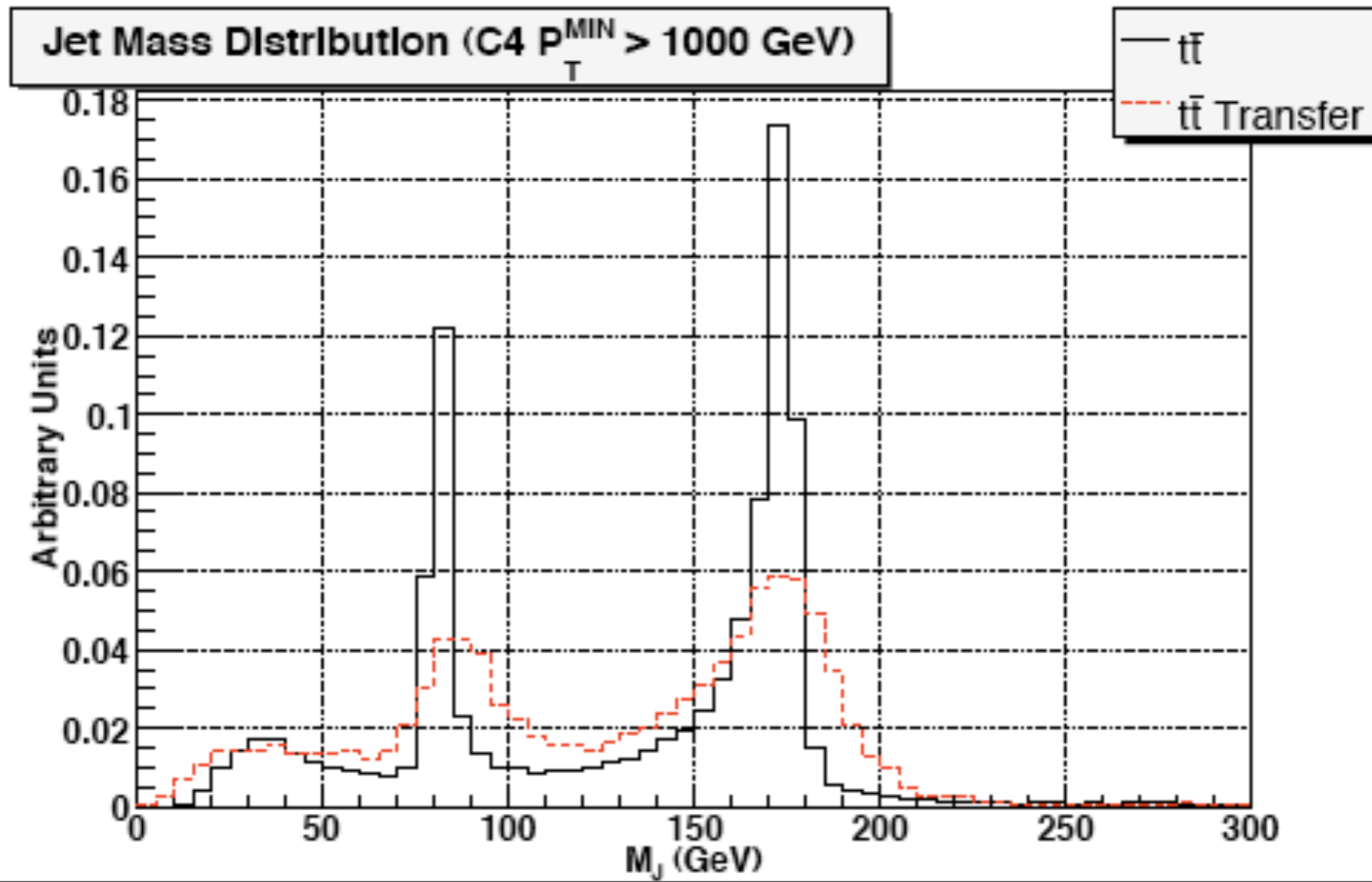
Pure kinematical  
bW(qq) dist'  
in/out cone  
much longer

$$J^t(m_J, m_t, R, p_T) \sim \int dm_{QCD} dm_{EW} J_{QCD}^t(m_{QCD}, R, p_T) \times \dots$$

# Cone top-jet mass distribution

Sherpa => Full Simulation  
(CKKW)

Preliminary (Transfer function “Full Simulation”)



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# QCD cone jet mass distribution

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We are interested in the following processes:

$$H_a(p_a) + H_b(p_b) \rightarrow J_1(m_{J_1}^2, p_{1,T}, R) + X$$

$$H_a(p_a) + H_b(p_b) \rightarrow J_1(m_{J_1}^2, p_{1,T}, R) + J_2(m_{J_2}^2, p_{2,T}, R) + X$$



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Factorized hadronic cross section:

$$\frac{d\sigma_{H_A H_B \rightarrow J_1 X}(R)}{dp_T dm_J d\eta} = \sum_{abc} \int dx_a dx_b \underbrace{\phi_a(x_a) \phi_b(x_b)}_{\text{PDF}} \frac{d\hat{\sigma}_{ab \rightarrow cX}}{dp_T dm_J d\eta}(x_a, x_b, p_T, \eta, m_J, R)$$

# QCD cone jet mass distribution

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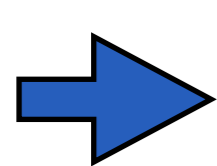
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**Hard** perturbative (Born) cross-section



$$\frac{d\sigma_{H_A H_B \rightarrow J_1 X}(R)}{dp_T dm_J d\eta} = \sum_{abc} \int dx_a dx_b \phi_a(x_a) \phi_b(x_b) \overbrace{H_{ab \rightarrow cX}(x_a, x_b, p_T, \eta, R)}^{\text{Hard}} \underbrace{\times J_1^c(m_J, p_T, R)}_{\text{Jet function}}$$

At the leading order

**Jet function**

# QCD cone jet mass distribution

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## Boosted QCD Jet via factorization:

$$\int dm_J J^c = 1$$

$$\frac{d\sigma(R)}{dp_T dm_J} = \sum_c J^c(m_J, p_T, R) \frac{d\hat{\sigma}^c(R)}{dp_T},$$

where  $c$  represents the flavour of the jet, and where

$$\frac{d\hat{\sigma}^c(R)}{dp_T} = \sum_{ab} \int dx_a dx_b \phi_a \phi_b \int d\eta \int dm_J \frac{d\hat{\sigma}_{ab \rightarrow cX}(R)}{dp_T dm_J d\eta}.$$

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Contact with Data (MC):

$$\frac{d\sigma_{pred}(R)}{dp_T dm_J} = \sum_c J^c(m_J, p_T, R) \left( \frac{d\sigma^c(R)}{dp_T} \right)_{MC}$$

# QCD cone jet mass distribution

Boosted QCD Jet via factorization:

$$\int dm_J J^c = 1$$

$$\frac{d\sigma(R)}{dp_T dm_J} = \sum J^c(m_J, p_T, R) \frac{d\hat{\sigma}^c(R)}{dp_T},$$

where  $\hat{\sigma}^c$  is the hard cross-section, and where

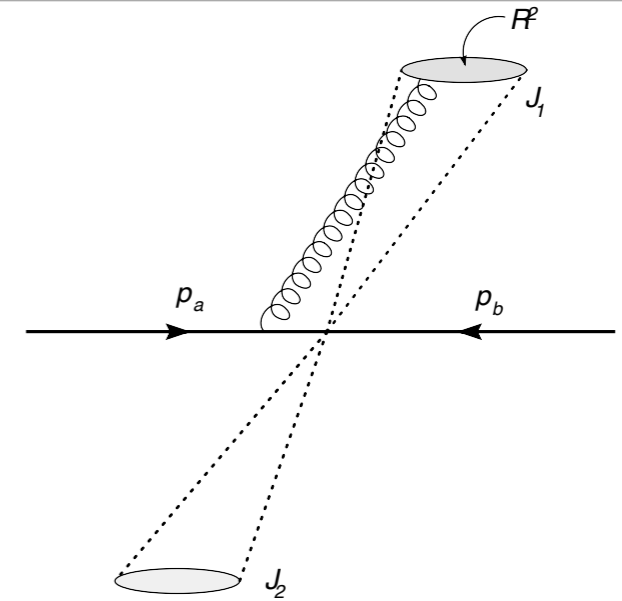
For large jet mass & small  $R$ ,  
no large logs =>  
 $J^i$  can be calculated via  
perturbative QCD!

$$\phi_a \phi_b \int d\eta \int dm_J \frac{d\hat{\sigma}_{ab \rightarrow cX}(R)}{dp_T dm_J d\eta}.$$

$$\frac{d\sigma(R)}{dp_T dm_J} = \sum_c J^c(m_J, p_T, R) \left( \frac{d\sigma^c(R)}{dp_T} \right)_{MC}$$

# QCD Jet mass distribution, Q+G

Main idea: calculating mass due to two-body QCD bremsstrahlung:

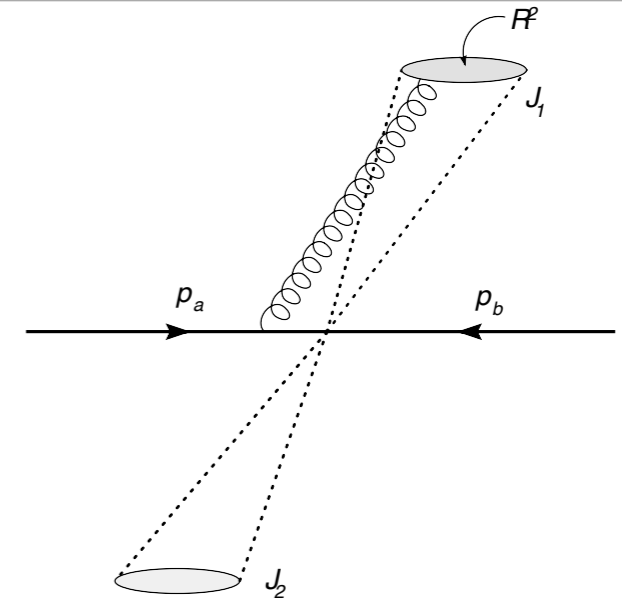


$$J^{(eik),c}(m_J, p_T, R) = \alpha_s(p_T) \frac{4C_c}{\pi m_J} \log \left( \frac{1}{z} \tan \left( \frac{R}{2} \right) \sqrt{4 - z^2} \right)$$
$$\approx \alpha_s(p_T) \frac{4C_c}{\pi m_J} \log \left( \frac{R p_T}{m_J} \right),$$

$$z = \frac{m_J}{p_T}$$

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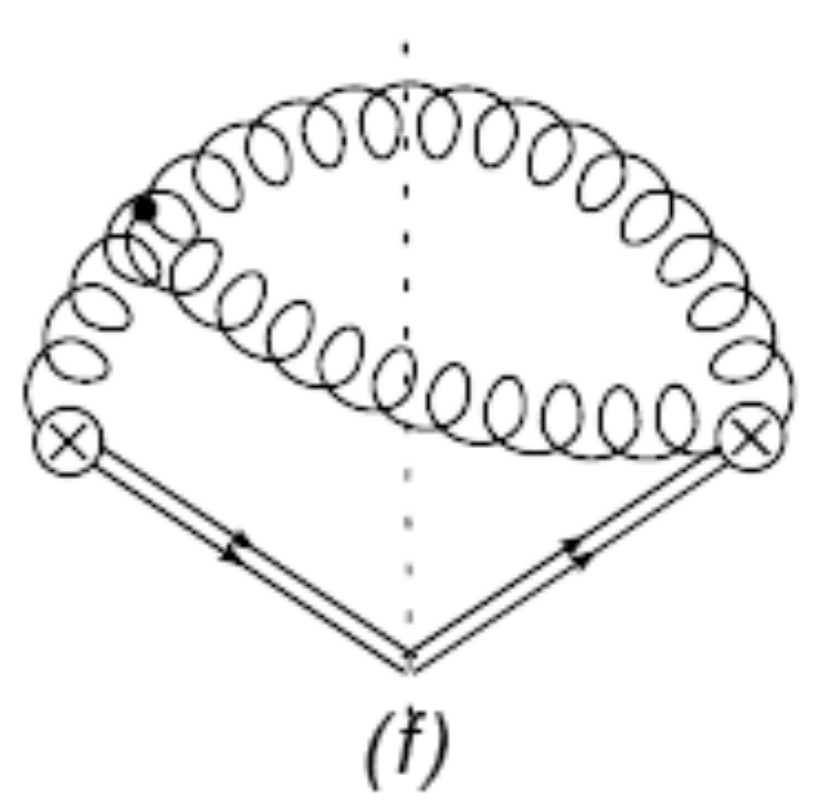
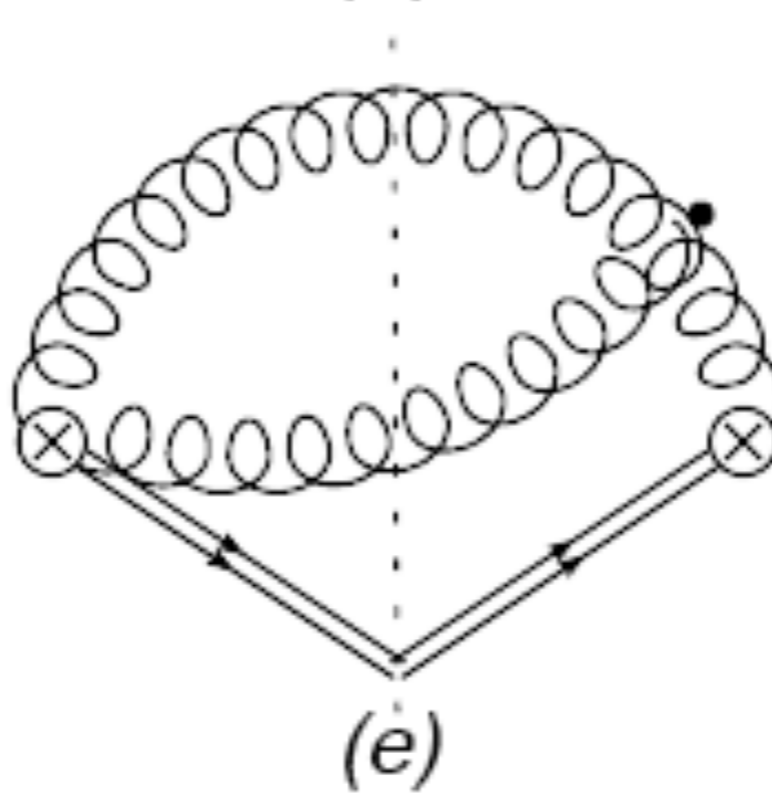
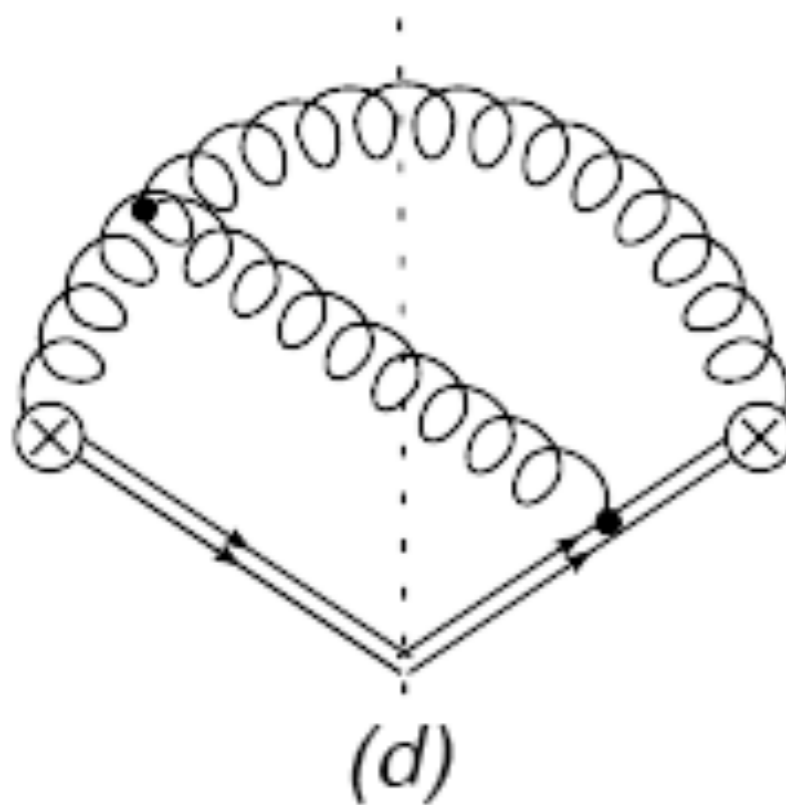
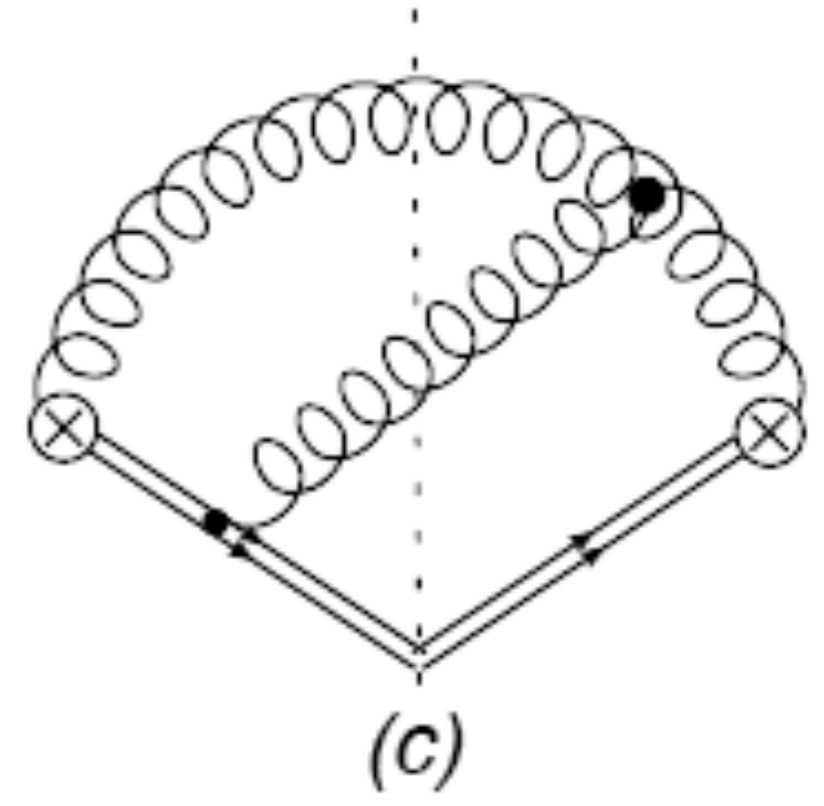
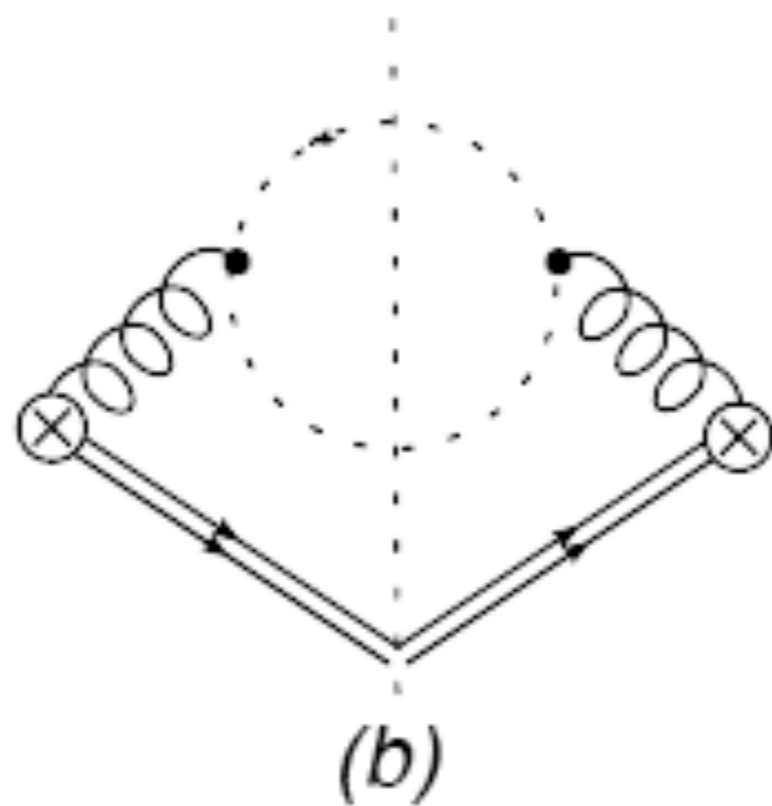
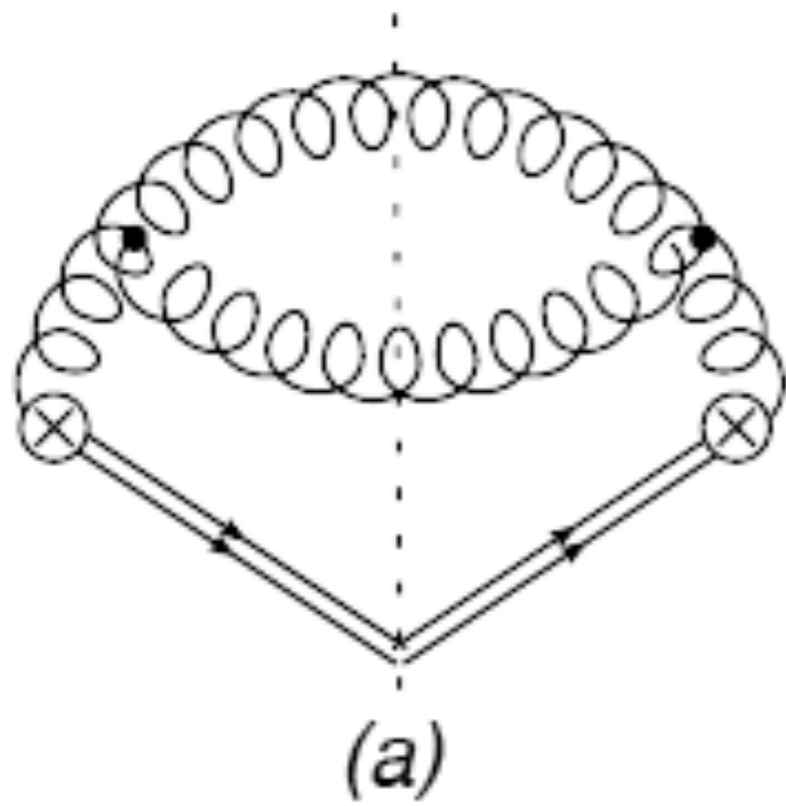
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$C$  { quark jets:  $C_{(q)} = C_F = \frac{4}{3}$   
gluon jets:  $C_{(g)} = C_A = 3$

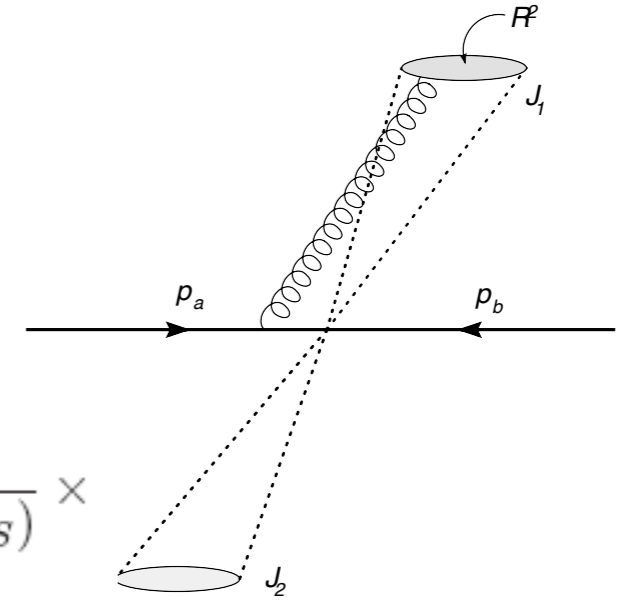


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$$J_i^{q(1)}(m_J^2, p_{0,J_i}, R) = \frac{C_F \beta_i}{4m_{J_i}^2} \int_{\cos(R)}^{\beta_i} \frac{d \cos \theta_S}{\pi} \frac{\alpha_S(k_0) z^4}{(2(1 - \beta_i \cos \theta_S) - z^2)(1 - \beta_i \cos \theta_S)} \times$$

$$\left\{ z^2 \frac{(1 + \cos \theta_S)^2}{(1 - \beta_i \cos \theta_S)(2(1 + \beta_i)(1 - \beta_i \cos \theta_S) - z^2(1 + \cos \theta_S))} + \frac{3(1 + \beta_i)}{z^2} + \frac{1}{z^4} \frac{(2(1 + \beta_i)(1 - \beta_i \cos \theta_S) - z^2(1 + \cos \theta_S))^2}{(1 + \cos \theta_S)(1 - \beta_i \cos \theta_S)} \right\},$$

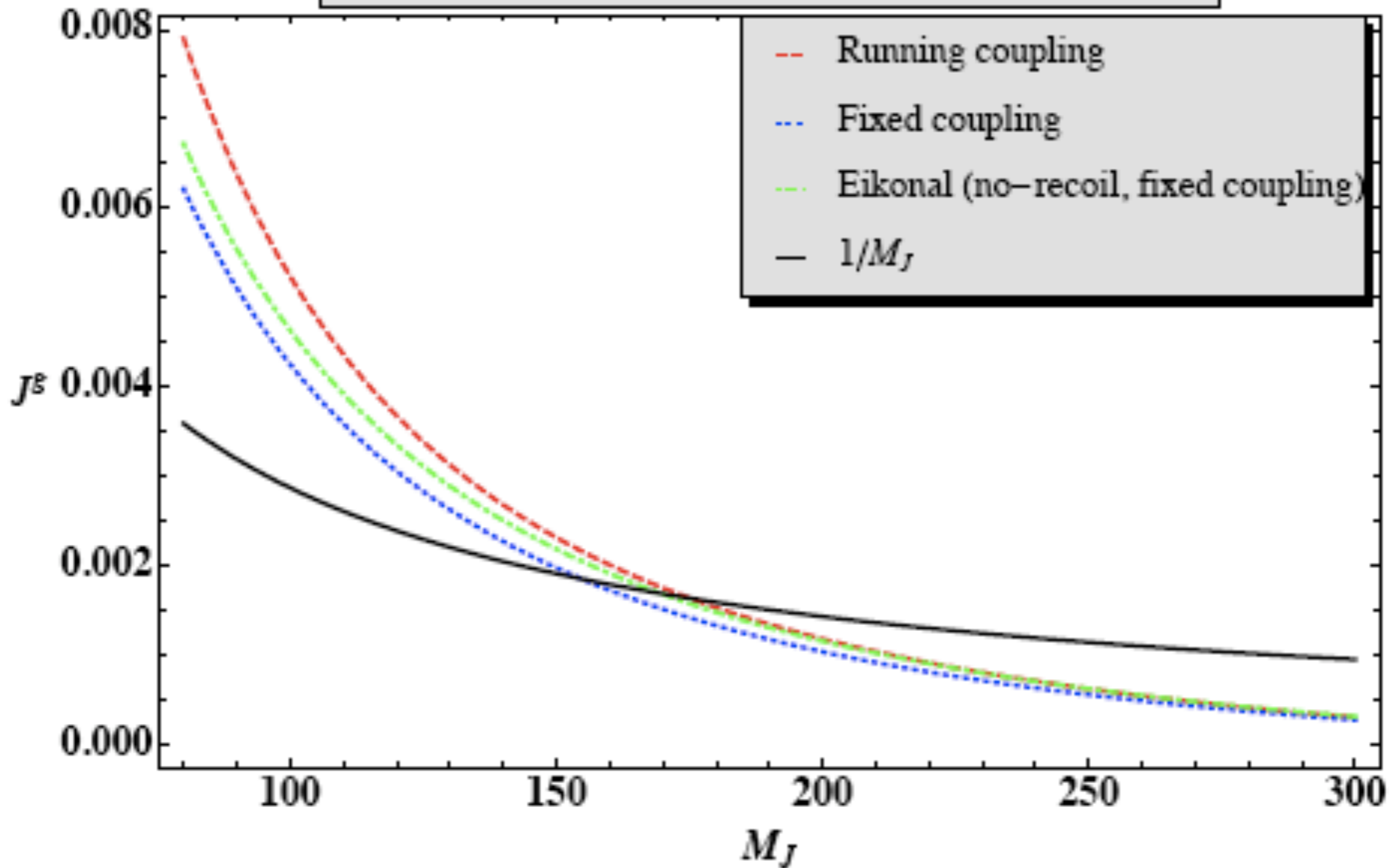
$$\beta_i = \sqrt{1 - m_{J_i}^2/p_{0,J_i}^2} \quad z = \frac{m_{J_i}}{p_{0,J_i}}, \quad p_{0,J_i} = \sqrt{m_{J_i}^2 + p_T^2}, \quad \text{and } k_0 = \frac{p_{0,J_i}}{2} \frac{z^2}{1 - \beta_i \cos \theta_S}.$$

$$J_i^{g(1)}(m_J^2, p_{0,J_i}, R) = \frac{C_A \beta_i}{16m_{J_i}^2} \int_{\cos(R)}^{\beta_i} \frac{d \cos \theta_S}{\pi} \frac{\alpha_S(k_0)}{(1 - \beta \cos \theta_S)^2 (1 - \cos^2 \theta_S) (2(1 + \beta) - z^2)}$$

$$\times (z^4(1 + \cos \theta_S)^2 + z^2(1 - \cos^2 \theta_S)(2(1 + \beta_i) - z^2) + (1 - \cos \theta_S)^2(2(1 + \beta_i) - z^2)^2)$$

# QCD Jet mass distribution, Q+G

$$J^g = \frac{1}{\sigma} \frac{d\sigma}{dM_J} \quad (\text{Gluon Jet Functions, } P_T = 1 \text{ TeV, } R=0.4)$$



# Jet mass distribution theory vs. MC

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Revisiting our prediction:

$$\frac{d\sigma_{pred}(R)}{dp_T dm_J} = \sum_c J^c(m_J, p_T, R) \left( \frac{d\sigma^c(R)}{dp_T} \right)_{MC}$$

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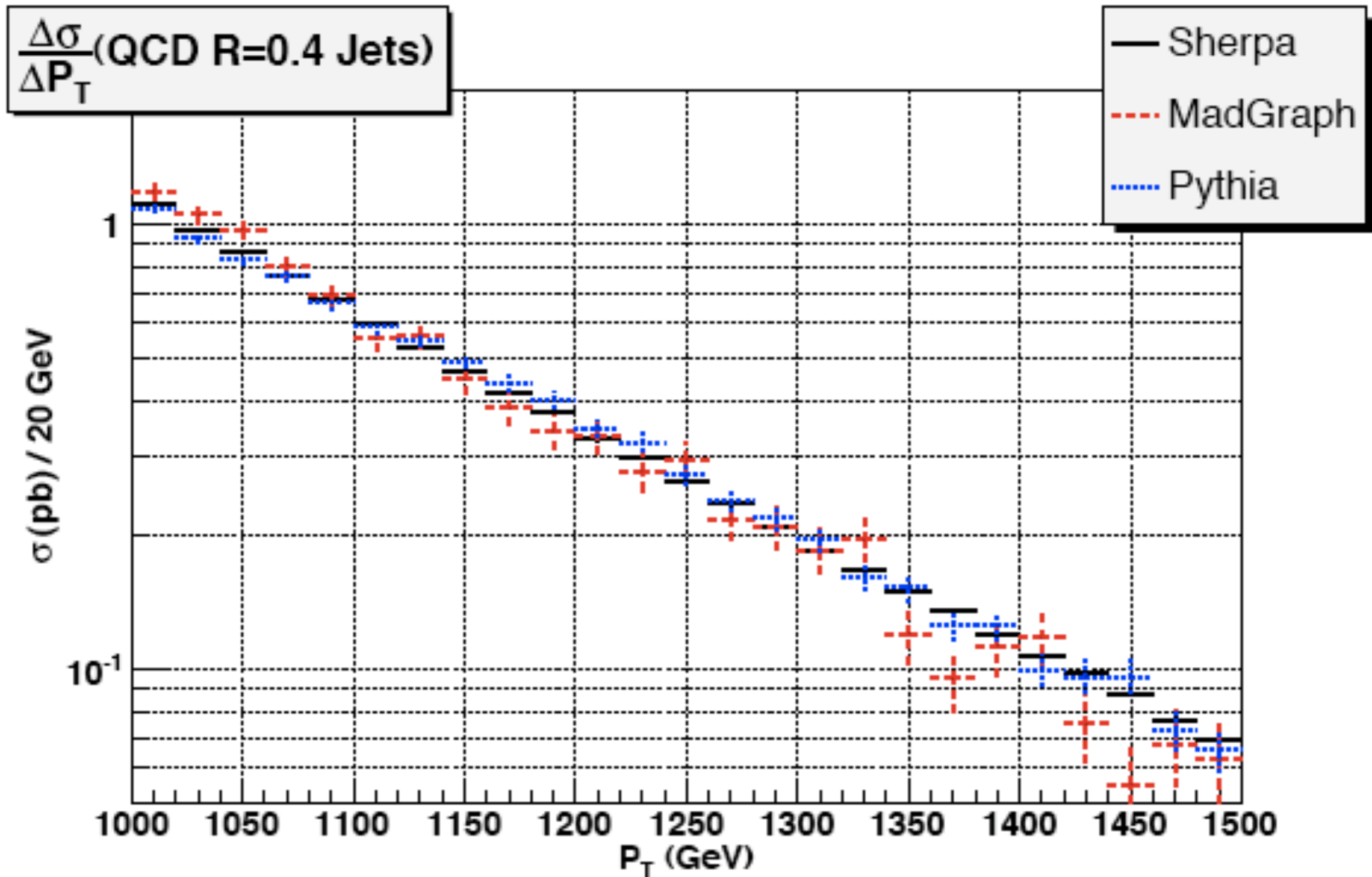
$$\frac{d\sigma_{pred}(R)}{dp_T dm_J} = \sum_c J^c(m_J, p_T, R) \left( \frac{d\sigma^c(R)}{dp_T} \right)_{MC}$$

But, in practice, cannot distinguish partonic origin of a jet: can only give bounds:  $J^g > J^q$

$$\frac{d\sigma_{pred}(R)}{dp_T dm_J} \text{ upper bound} = J^g(m_J, p_T, R) \sum_c \left( \frac{d\sigma^c(R)}{dp_T} \right)_{MC}$$

$$\frac{d\sigma_{pred}(R)}{dp_T dm_J} \text{ lower bound} = J^q(m_J, p_T, R) \sum_c \left( \frac{d\sigma^c(R)}{dp_T} \right)_{MC}$$

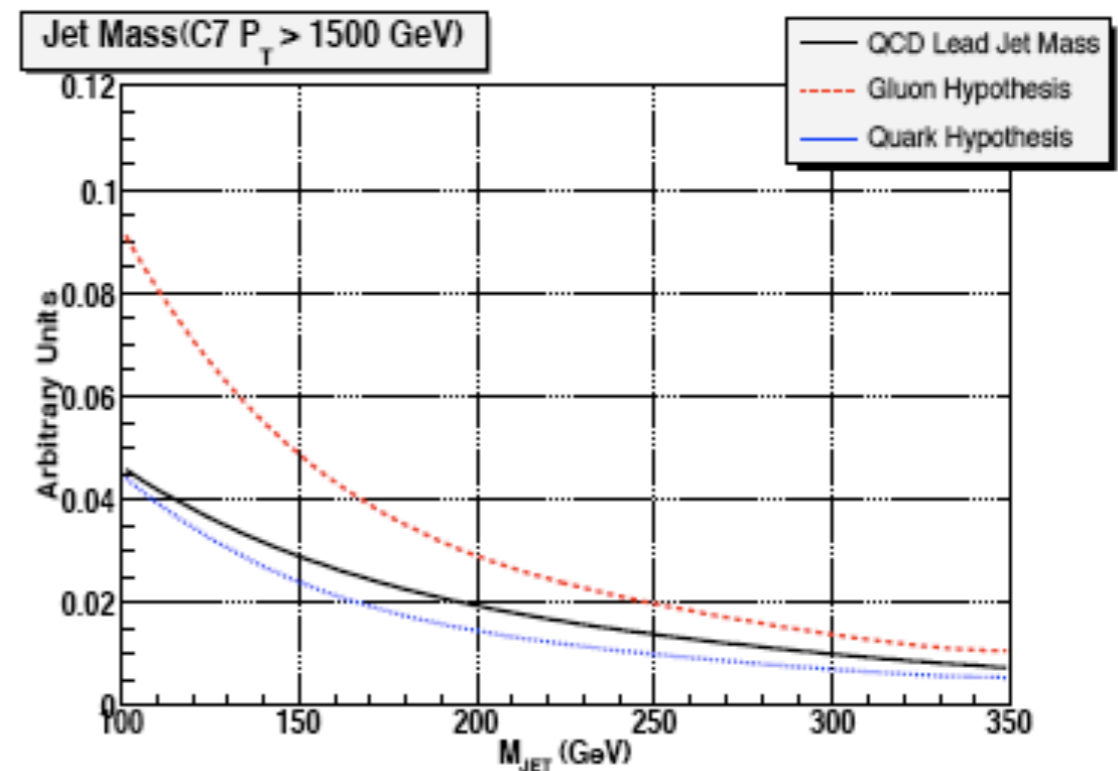
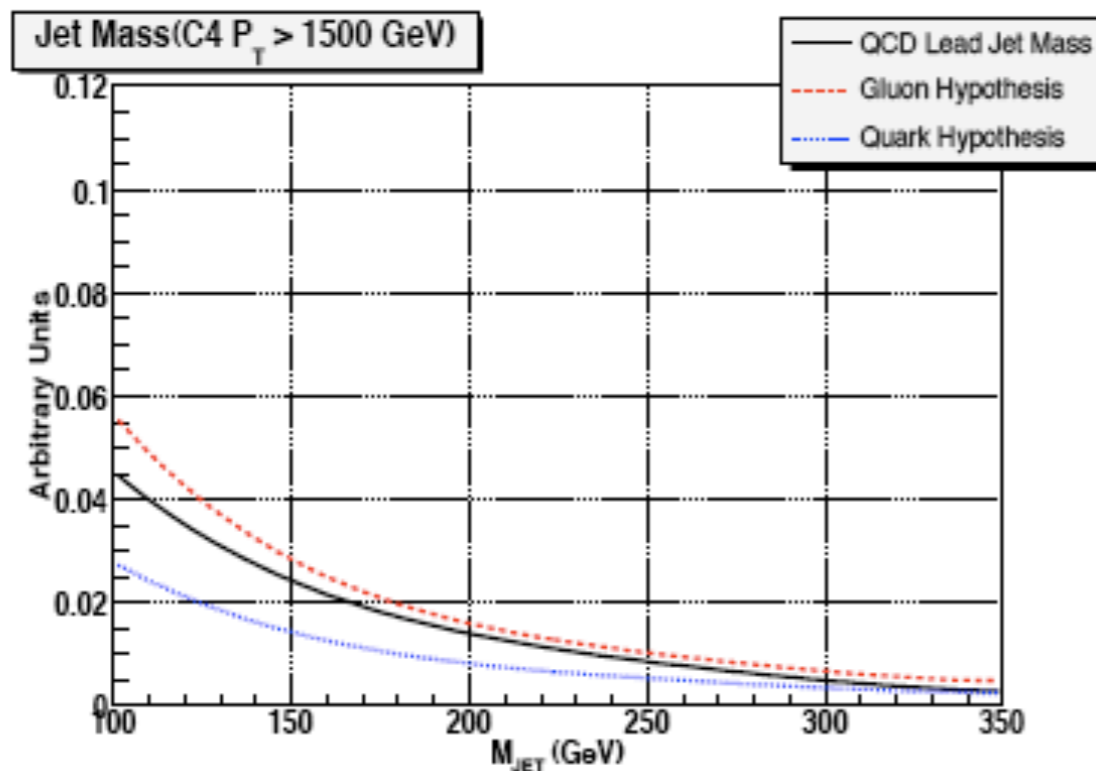
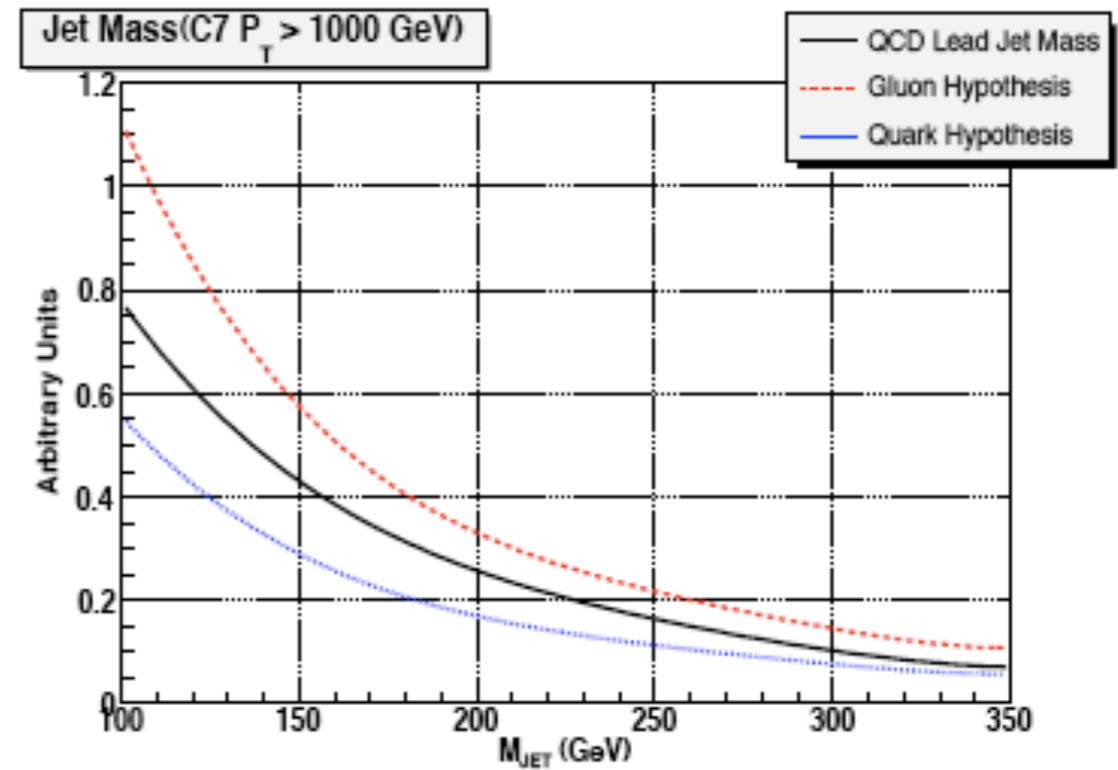
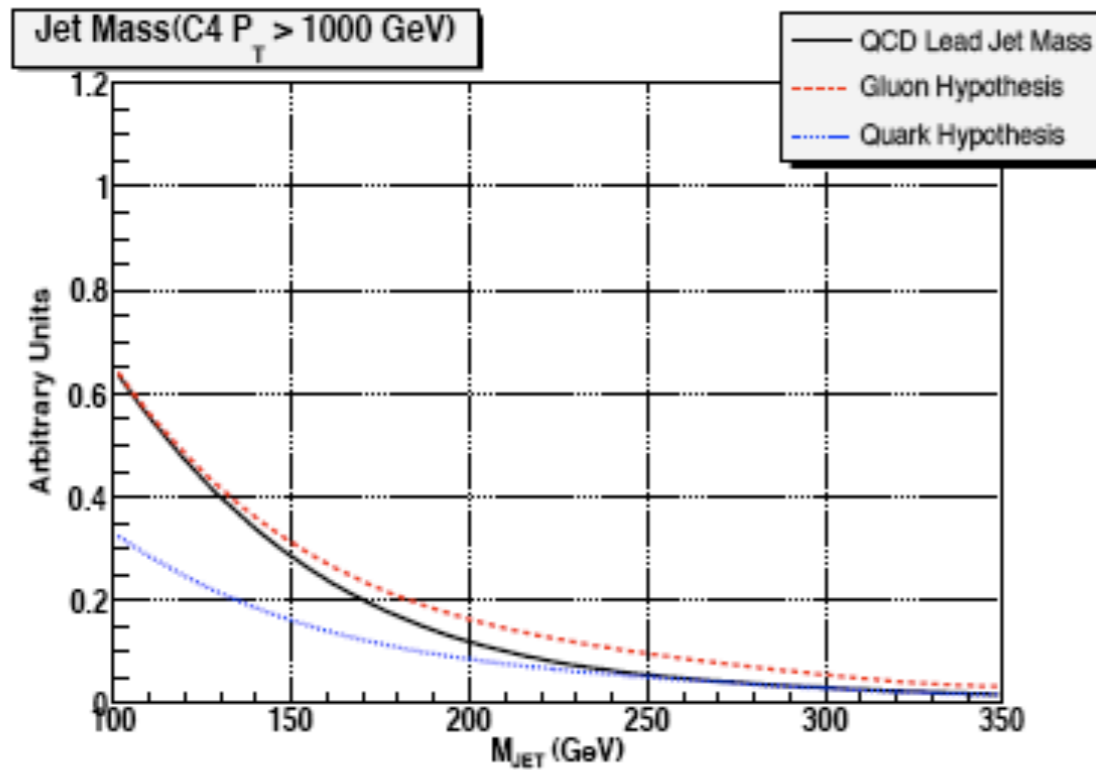
# Jet mass distribution theory vs. MC





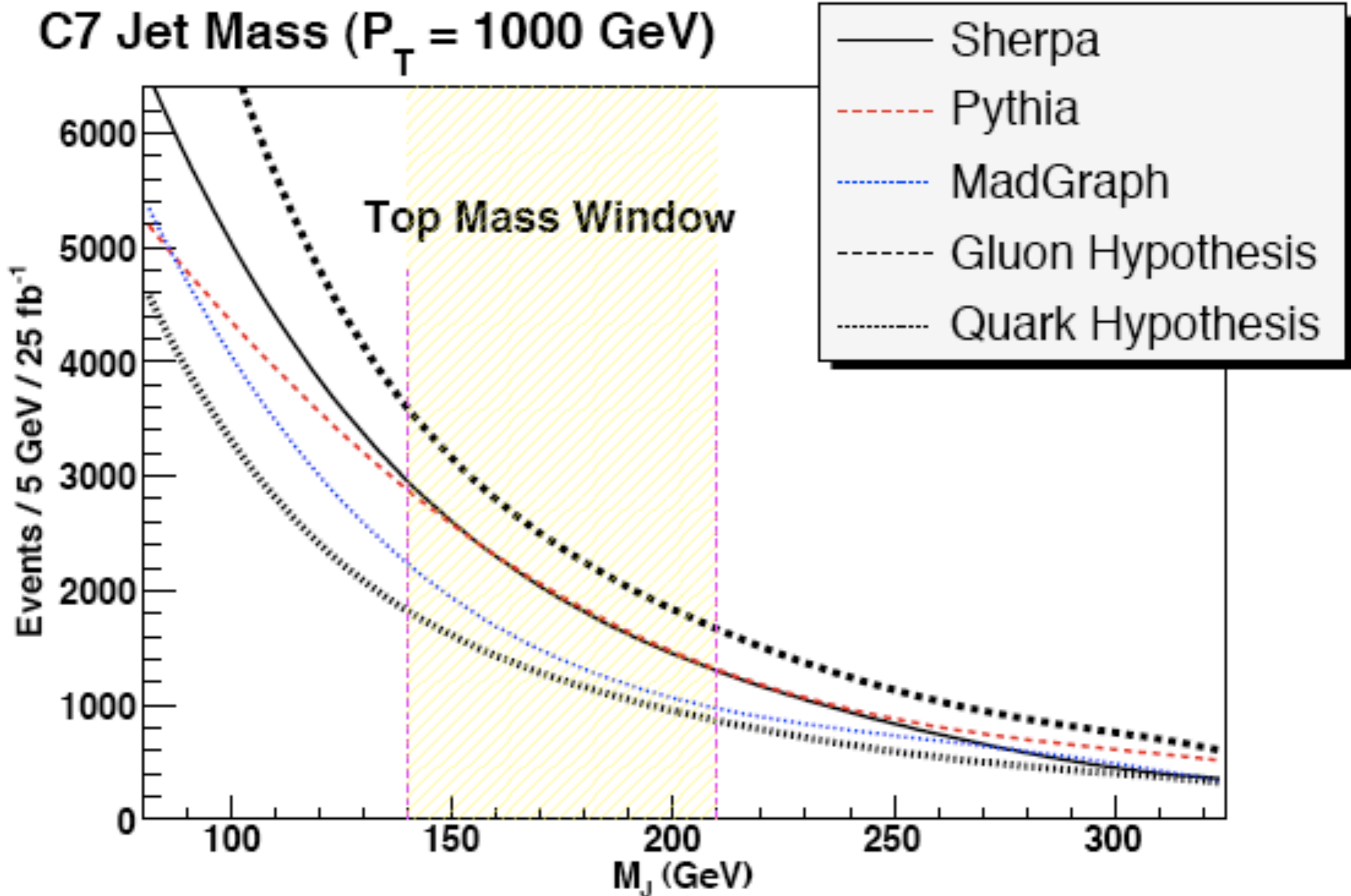
# Jet mass distribution theory vs. MC

## Sherpa, jet function convolved



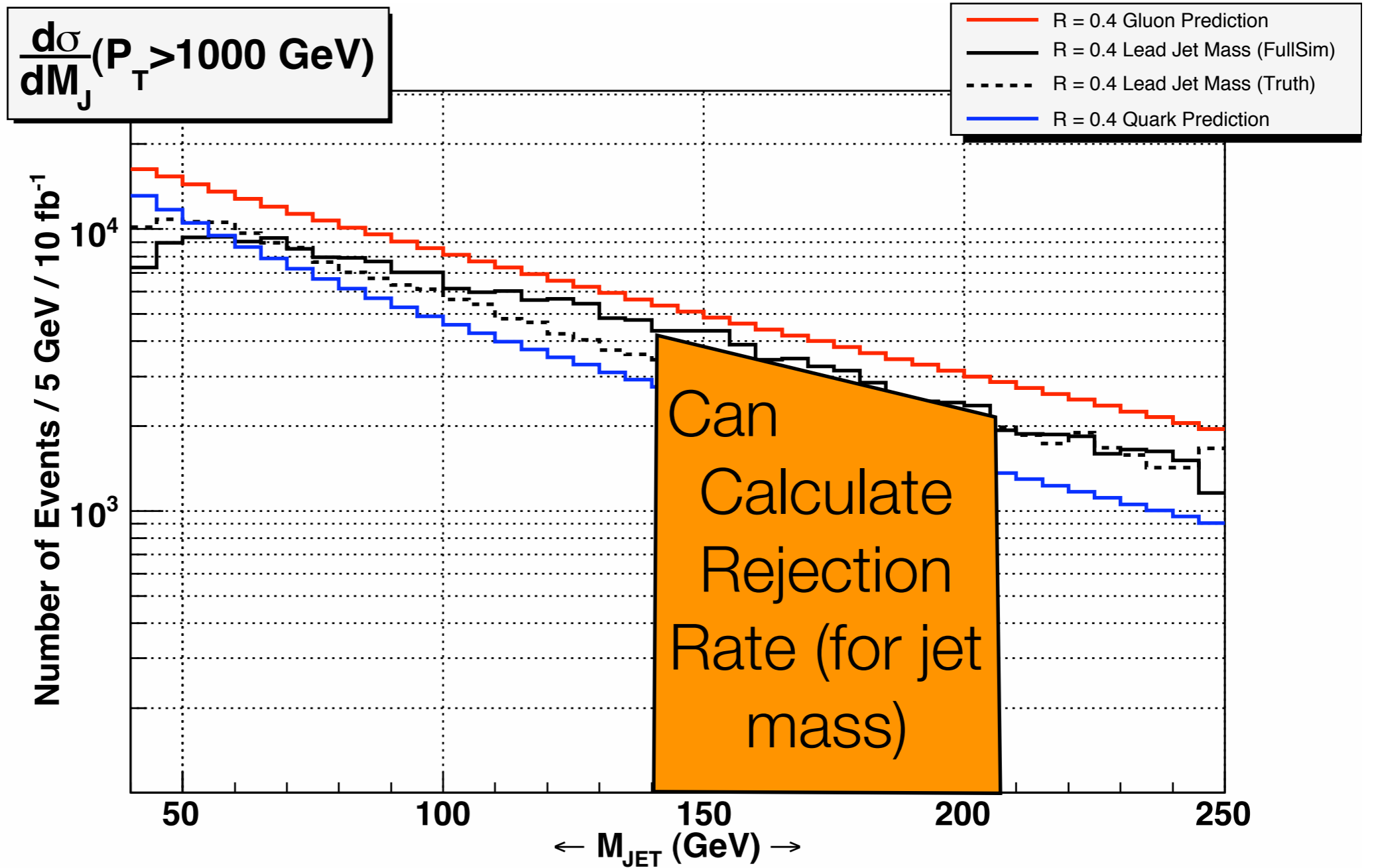


# Jet mass distribution theory vs. MC



# QCD jet mass dist' under control!

Sherpa (CKKW)  
With Full Detector  
Simulation



# QCD jet mass dist' under control!

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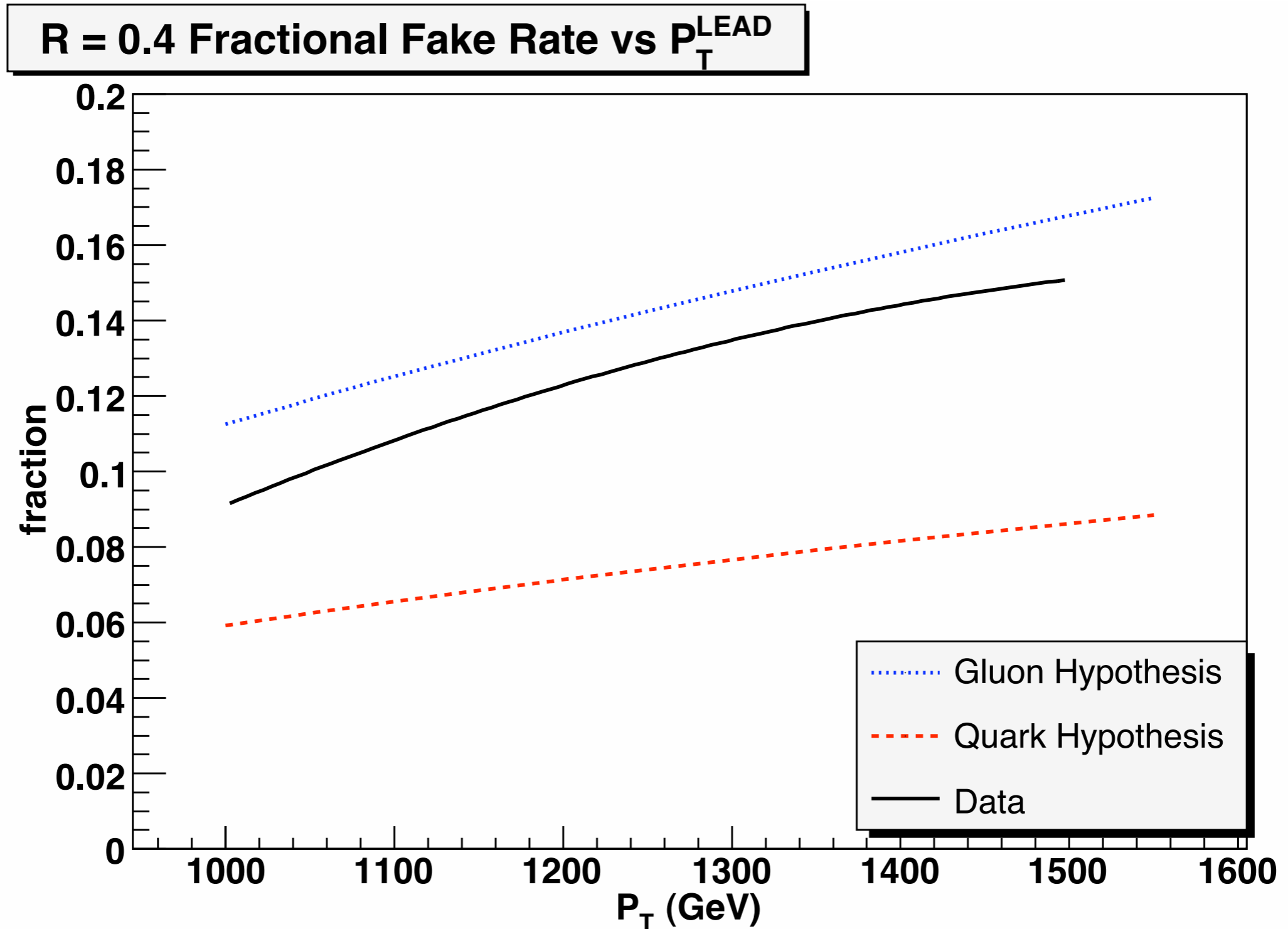
◆ **Rejection Ratio**: (#of events for  $m_t - \Delta < m_J < m_t + \Delta$ ) / (total # of events)

- Can use our jet function to calculate it:

$$\begin{aligned}\sigma(R)_{upper\ bound} &= \int_{p_T^{min}}^{\infty} dp_T \sum_c \left( \frac{d\sigma^c(R)}{dp_T} \right)_{MC} \int_{140\ GeV}^{210\ GeV} J^g(m_J, p_T, R) dm_J \\ \sigma(R)_{lower\ bound} &= \int_{p_T^{min}}^{\infty} dp_T \sum_c \left( \frac{d\sigma^c(R)}{dp_T} \right)_{MC} \int_{140\ GeV}^{210\ GeV} J^q(m_J, p_T, R) dm_J\end{aligned}$$

- Matches well with MC simulation (within 10%)
- For QCD dijet background, double mass tagging will reduce the background (typically,  $\epsilon_r \sim 15\%$ )

# QCD jet mass dist' under control!

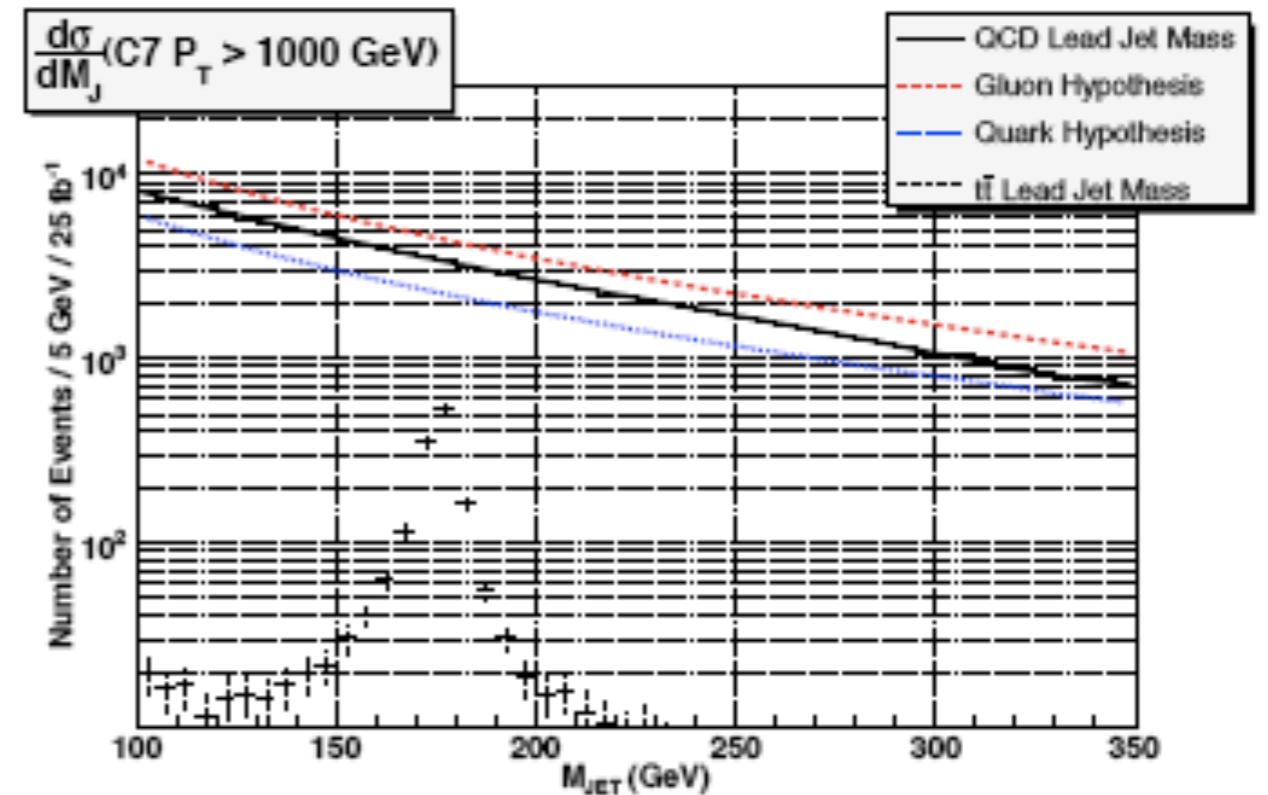
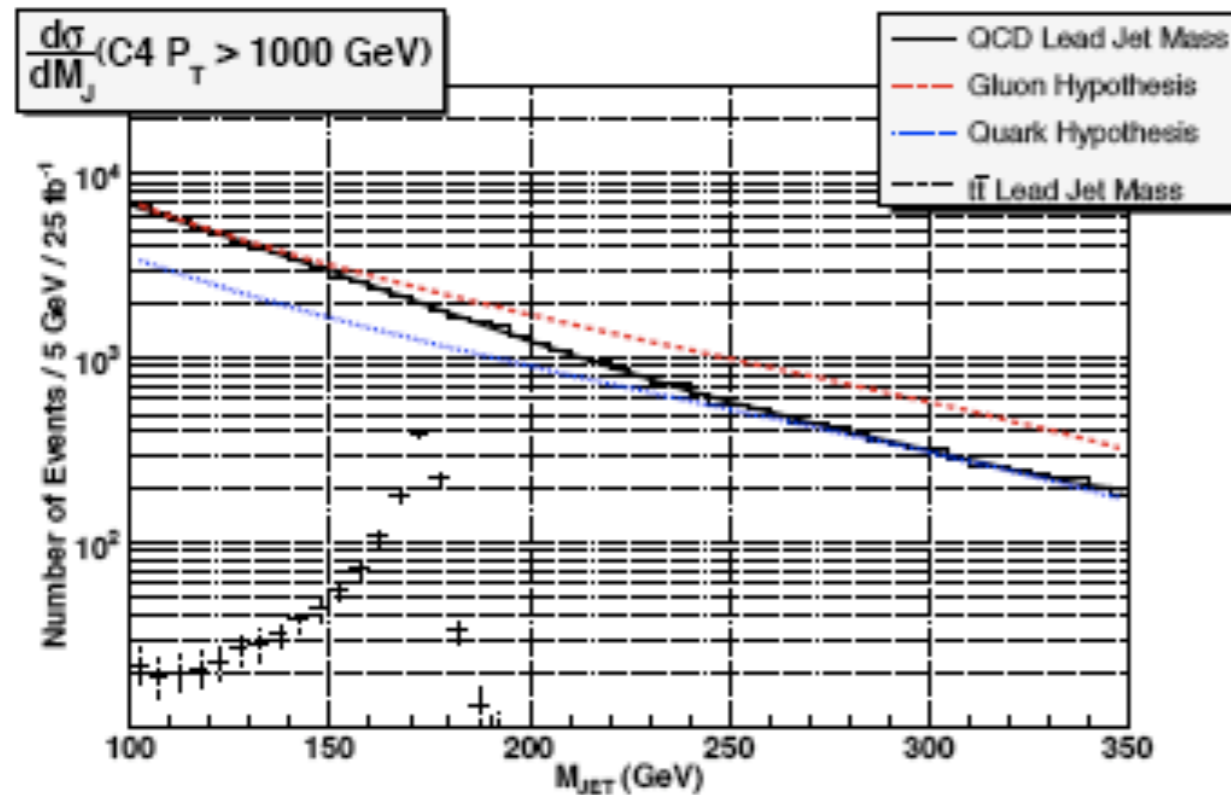


# Cross Section Uncertainty

Process	Generator	PDF	Matching	Cross Section
$pp \rightarrow t\bar{t}(j)$	SHERPA 1.0.9	CTEQ6M	CKKW	141 fb
$pp \rightarrow t\bar{t}(j)$	SHERPA 1.1.2	CTEQ6M	CKKW	149 fb
$pp \rightarrow t\bar{t}(j)$	SHERPA 1.1.2	CTEQ6L	CKKW	281 fb
$pp \rightarrow t\bar{t}(j)$	MG/ME 4	CTEQ6M	MLM	68 fb
$pp \rightarrow t\bar{t}(j)$	MG/ME 4	CTEQ6L	MLM	56 fb
$pp \rightarrow t\bar{t}$	Pythia 6	CTEQ6L	-	157 fb
$pp \rightarrow t\bar{t}$	Pythia 8	CTEQ6M	-	174 fb
$pp \rightarrow jj(j)$	SHERPA 1.1.0	CTEQ6M	CKKW	10.2 pb
$pp \rightarrow jj(j)$	SHERPA 1.1.2	CTEQ6M	CKKW	21.3 pb
$pp \rightarrow jj(j)$	SHERPA 1.1.2	CTEQ6M	CKKW	15.8 pb
$pp \rightarrow jj(j)$	MG/ME 4	CTEQ6L	MLM	8.54 pb
$pp \rightarrow jj(j)$	MG/ME 4	CTEQ6M	MLM	9.93 pb
$pp \rightarrow jj$	Pythia 6	CTEQ6L	-	13.7 pb
$pp \rightarrow jj$	Pythia 8	CTEQ6M	-	13.3 pb

Table 1: Cross sections for producing final state  $R = 0.4$  leading cone jets with  $p_T \geq 1$  TeV and  $|\eta| \leq 2$ . Generation level cuts were imposed as follows. Final state partons from the hard scatter were required to have  $p_T \geq 20$  GeV. For MG/ME, final state partons have  $|\eta| \leq 4.5$ . Processes with a trailing  $(j)$  suffix indicate that  $2 \rightarrow 2$  and  $2 \rightarrow 3$  processes are represented.

# Ex. SM $t\bar{t}b\bar{b}$ vs. di-jet background!



With transfer-functions (“full simulation”)



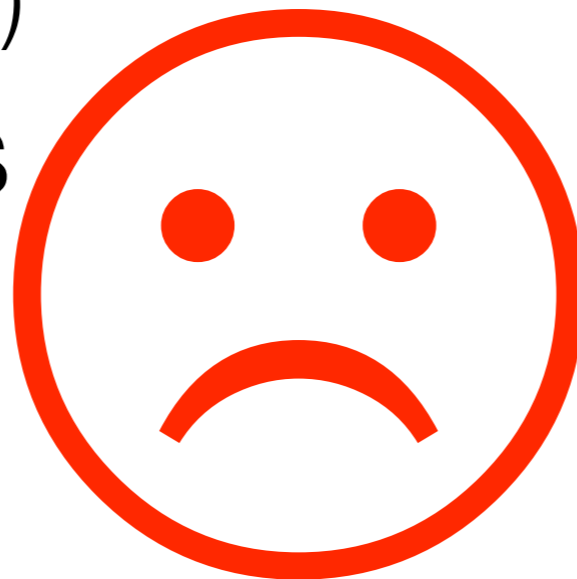
# Ex. SM ttbar vs. di-jet background!

$p_T^{lead}$ cut	Cone	$S$ (0% JES)	$\Delta_0$	+5% JES	$\Delta_5$	-5% JES	$\Delta_{-5}$
1000 GeV	C4	293	-31.5%	358	-16.4%	230	-46.3%
1000 GeV	C7	478	-33.1%	616	-13.7%	358	-49.9%
1500 GeV	C4	32	-30.4%	44	-4.3%	21	-54.3%
1500 GeV	C7	35	-34.0%	52	-1.9%	24	-54.7%
$p_T^{lead}$ cut	Cone	$B$ (0% JES)	$\Delta_0$	+5% JES	$\Delta_5$	-5% JES	$\Delta_{-5}$
1000 GeV	C4	2475	5.8%	2914	24.5%	1919	-18.0%
1000 GeV	C7	6272	7.2%	8190	40.0%	4894	-16.3%
1500 GeV	C4	294	16.7%	380	50.8%	196	-22.2%
1500 GeV	C7	496	23.4%	732	82.1%	330	-17.9%

Double mass tagging at  $25 \text{ fb}^{-1}$  with detector resolution and Jet Energy Scale (JES)

look hopeless

b-tagging



without high efficiency!

**S/B~0.11**

$$\Delta_{JES} = \frac{N_{JES} - N_{TRUTH}}{N_{TRUTH}}$$

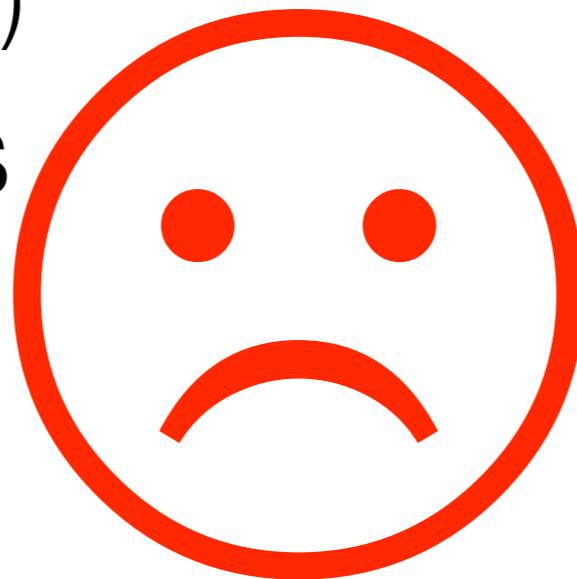
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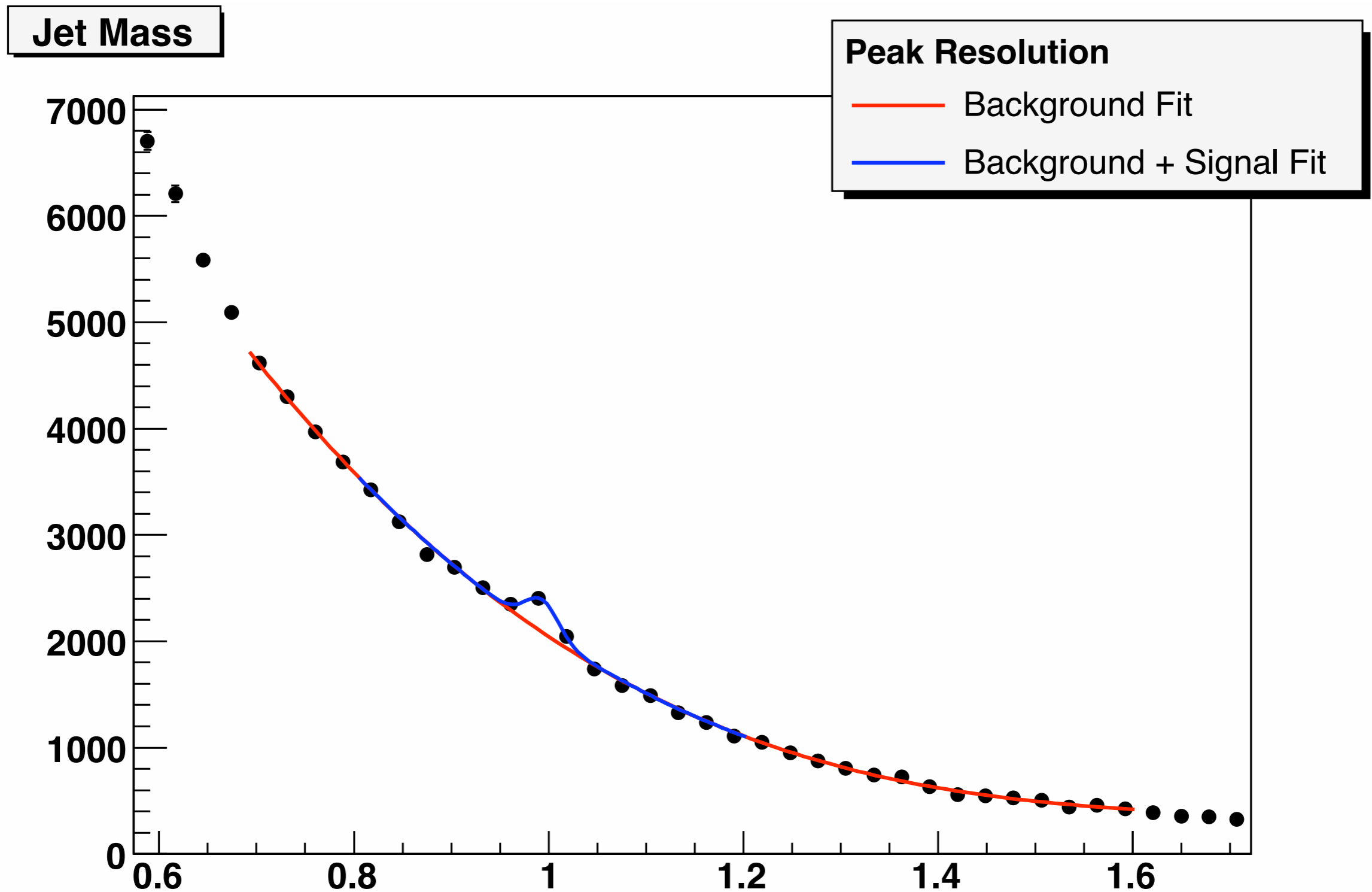
without high efficiency!

**S/B~0.11**

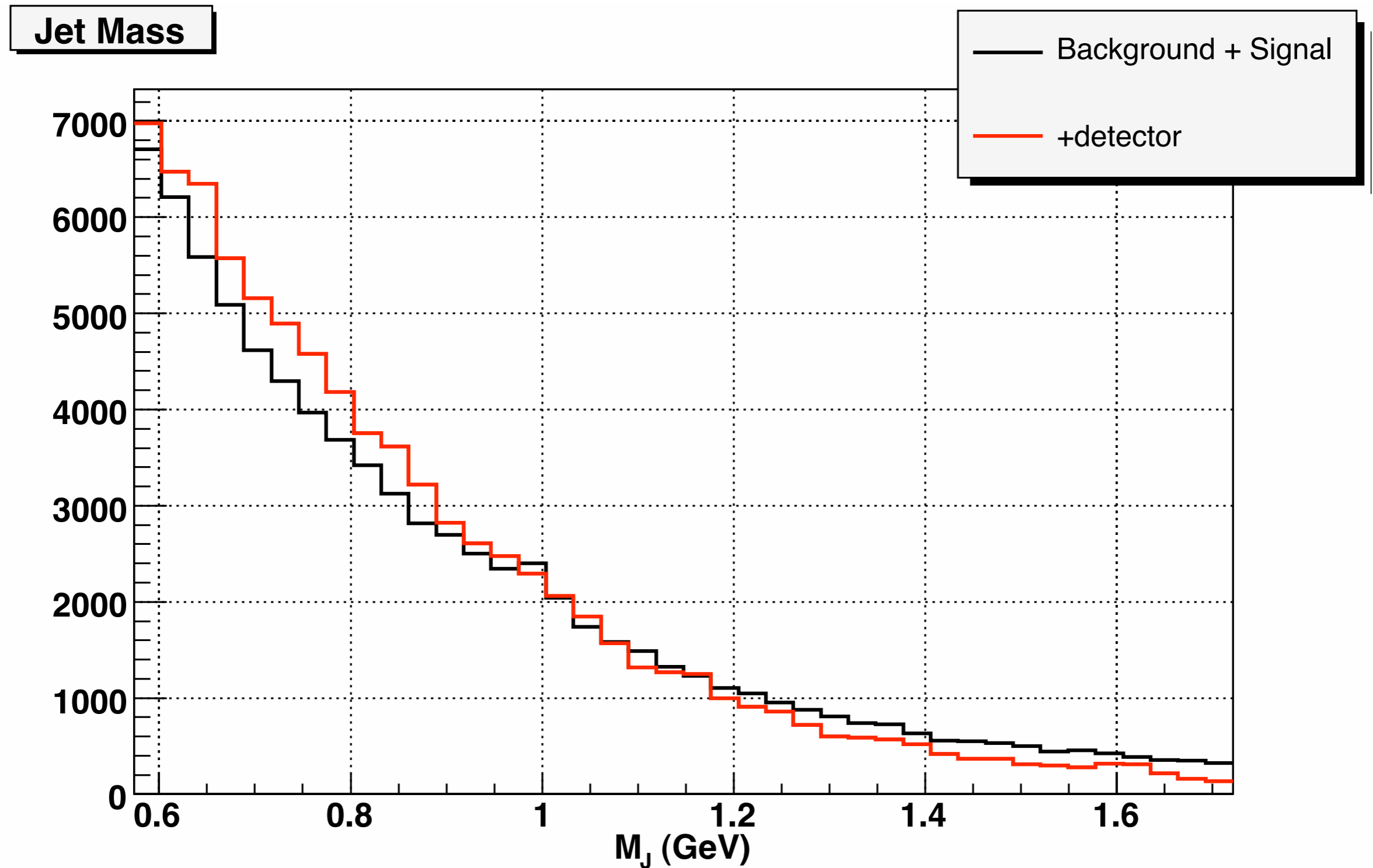
$$\Delta_{JES} = \frac{N_{JES} - N_{TRUTH}}{N_{TRUTH}}$$



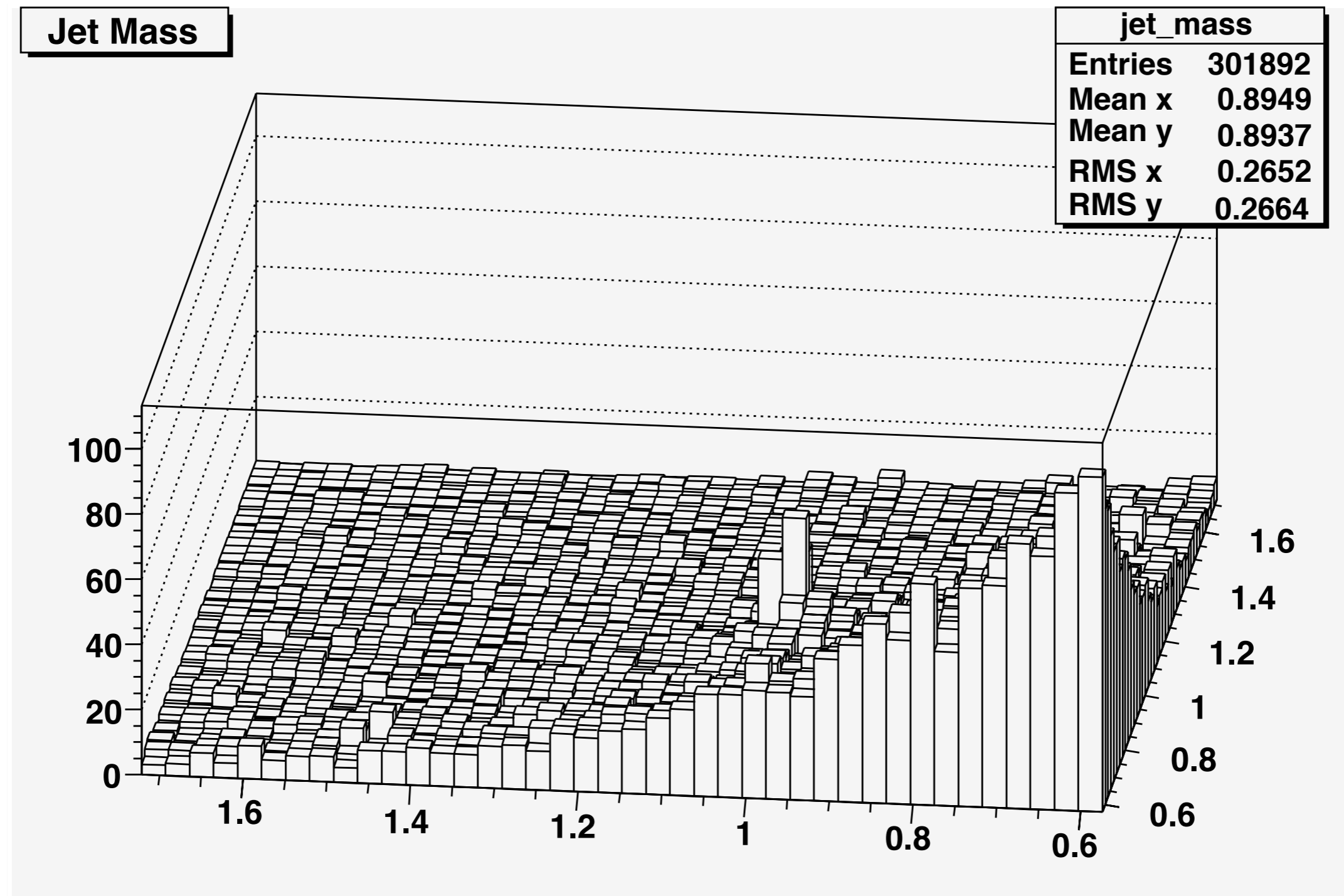
# Ex. SM $t\bar{t}b\bar{b}$ vs. di-jet background!



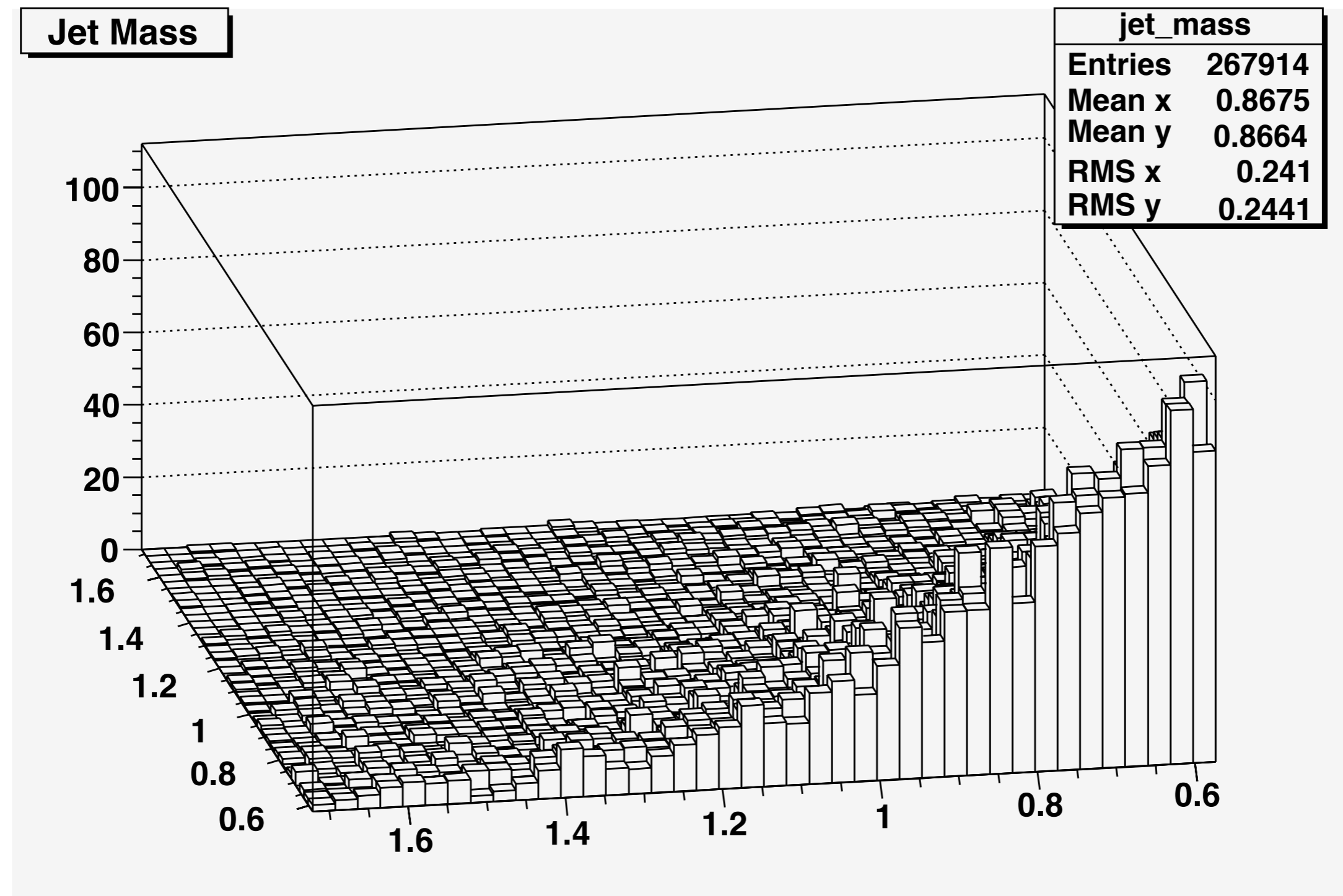
# Ex. SM $t\bar{t}b\bar{b}$ vs. di-jet background!



# Ex. SM ttbar vs. di-jet background!



# Ex. SM ttbar vs. di-jet background!



# Ex. SM $t\bar{t}b\bar{b}$ vs. di-jet background!

Jet Mass

jet\_mass

Entries 267914

Mean 0.8675

StdDev 0.8664

Min 0.241

Need Extra Handles  
to distinguish Signal  
from Background!

0.8

0.6

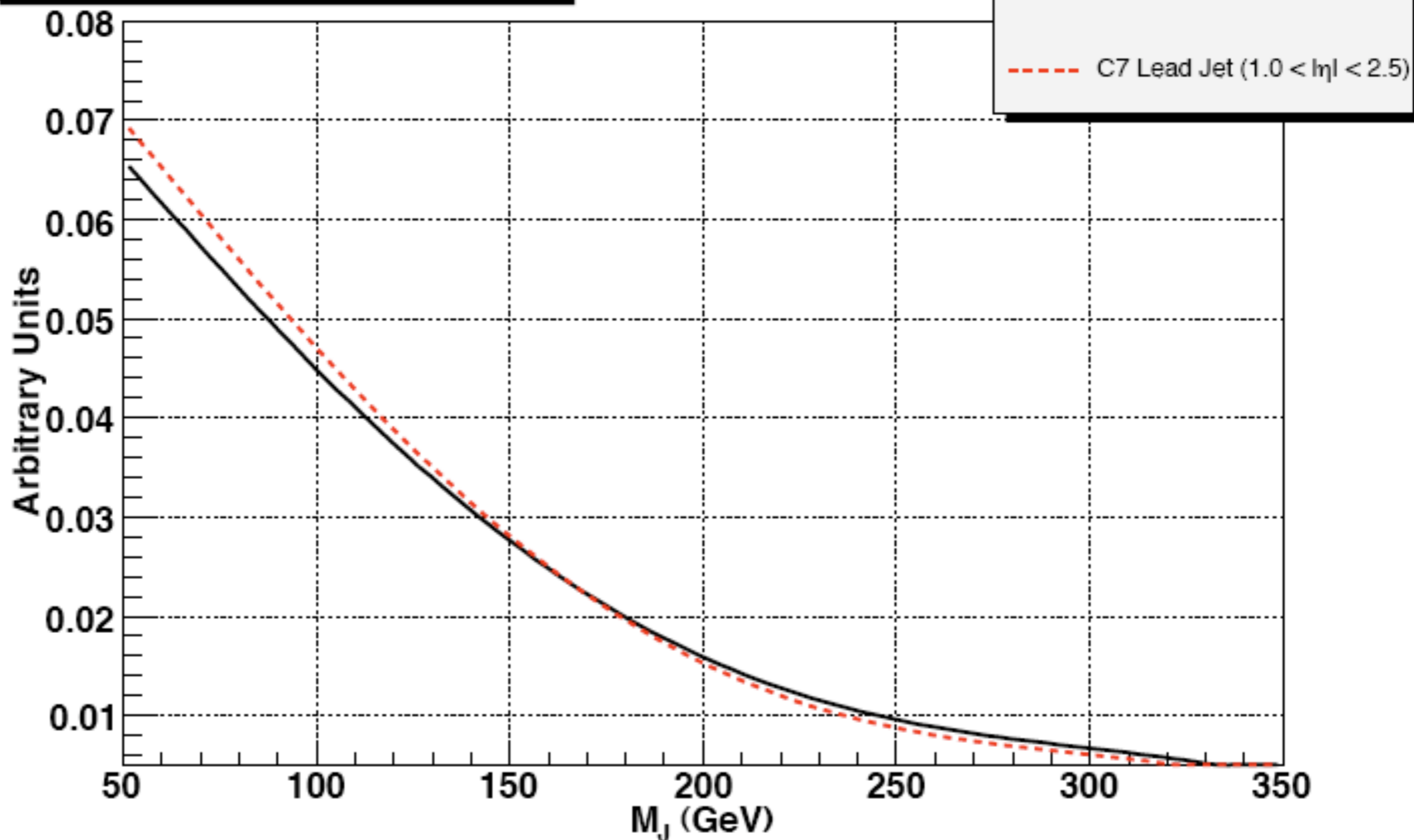
1.6

0.8

0.6

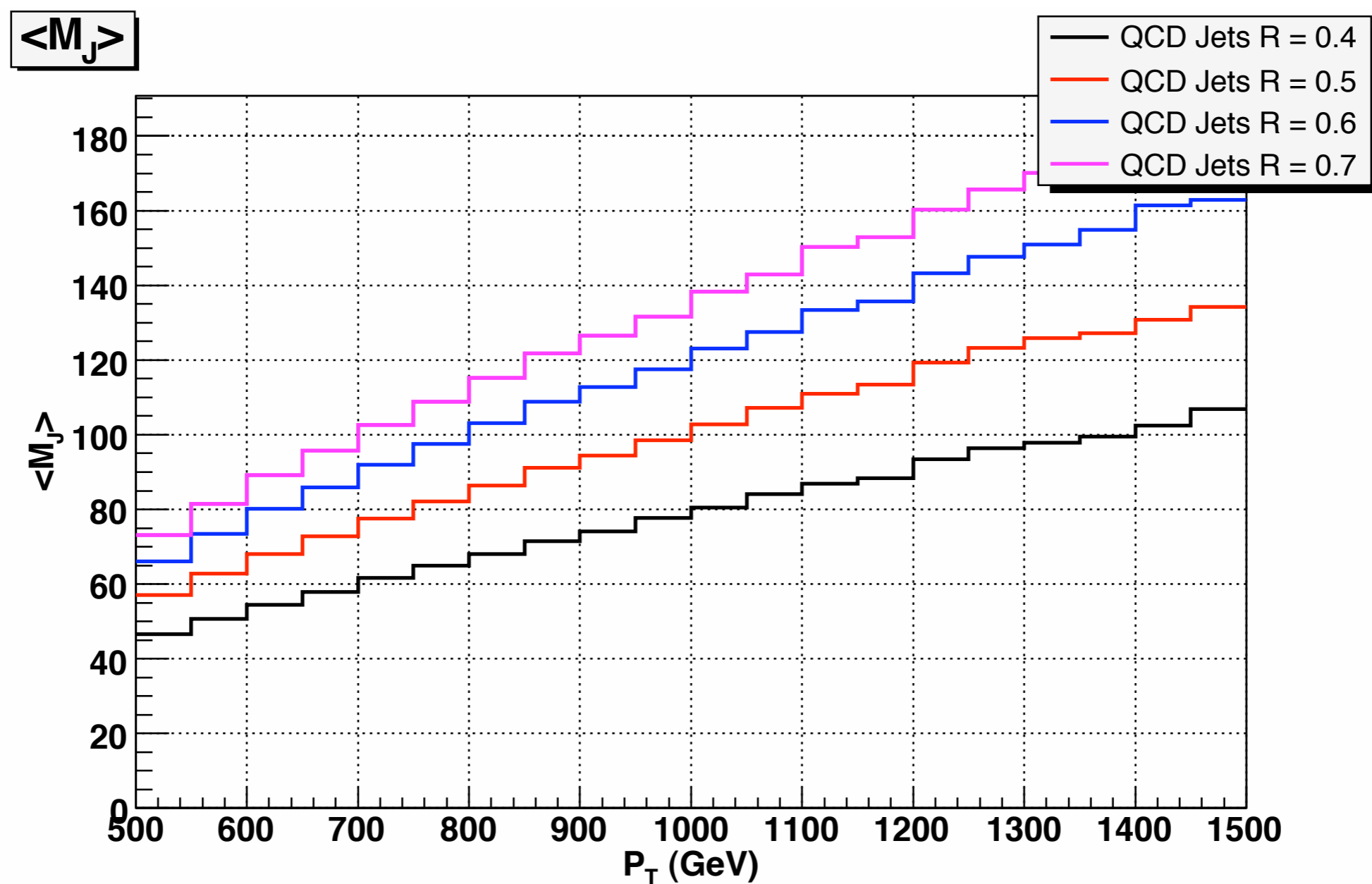
# Pseudo-rapidity independence

QCD Jet Mass ( $P_T > 1$  TeV)



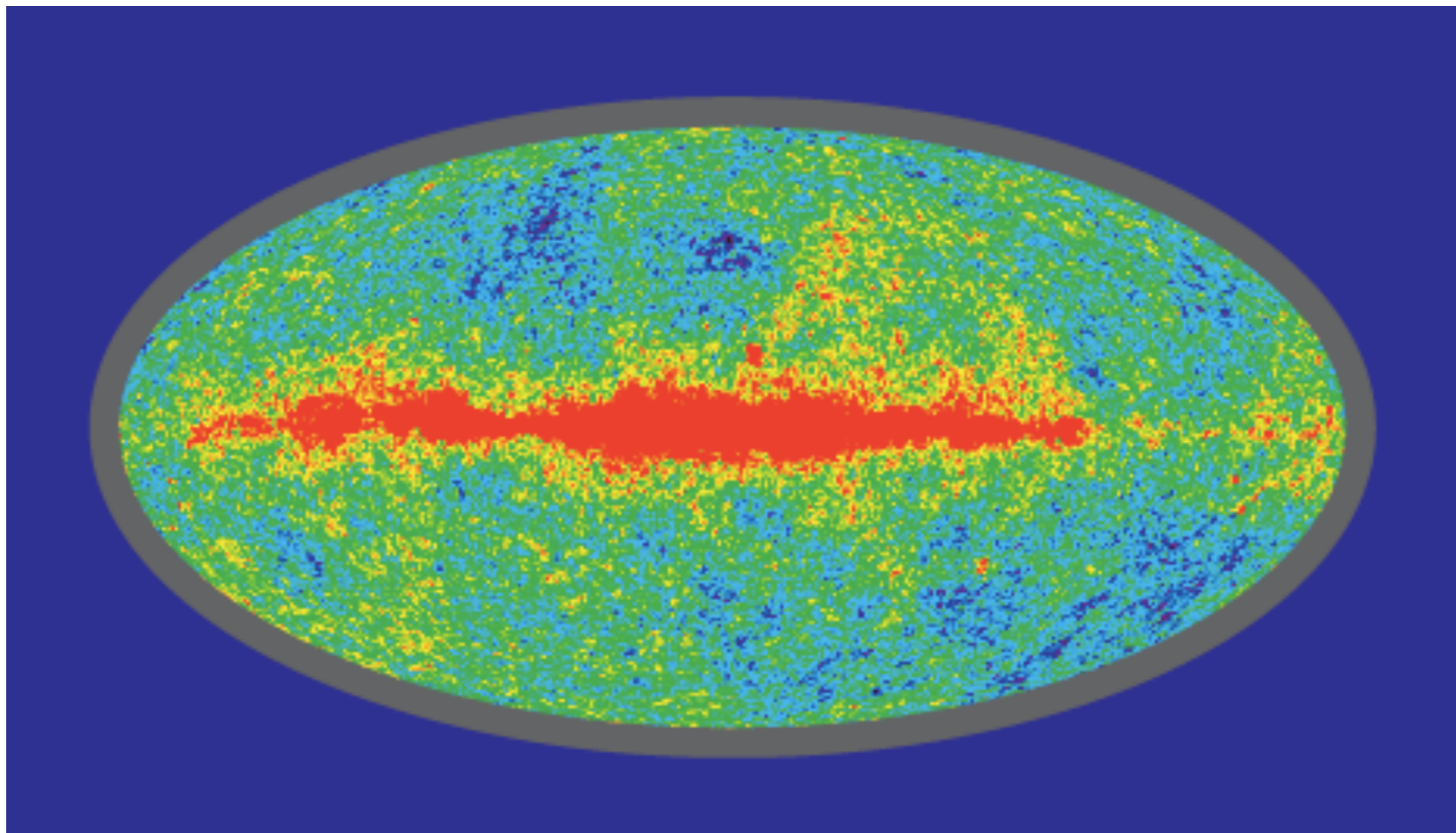
# Average Jet Mass (IR Mass cut needed)

$$\langle M_J \rangle \propto P_T, R$$





# Jet sub-structure





# Why jets? What else?

---

- ◆ QCD amplitudes have soft-collinear singularity
- ◆ Observable: IR safe, smooth function of E flow  
*Sterman & Weinberg, PRL (77)*
- ◆ Jet is a very inclusive object, defined via direction +  $p_T$  (+ mass)
- ◆ Even  $R=0.4$  contains  $O(100)$  had-cells => huge amount of info' is lost

# Jet-shapes

---

- ◆ “Jet-shapes” = inclusive observables dependent on energy flow within individual jets
- ◆ Once jet mass is fixed at a high scale
  - ➔ Large class of jet-shapes become perturbatively calculable
  - ➔ IR safe jet-shapes combined with IR safe jet algorithm provide a bridge between  
Direct theory prediction ↔ Data/MC output

# Jet-shapes

---

- ◆ “Jet-shapes” variables depend on the shape of the actual jets

Can analyze a single event by a variety of jet shapes  
=> the resolution associated with each one need not be dramatic!

Direct the data/MC output

# IR-safe jet-shapes which know top from QCD jets?

---

◆ Successes in high jet mass => jet function is well described by single gluon radiation

◆ QCD, top: **linear**, **planar** E-deposition in the cone

*Almeida, SJL, Perez, Sterman, Sung, & Virzi,  
arXiv:0807.0234*

*c.f. Wang, Thale: similar event shape, "sphericity tensor"  
arXiv:0806.0023*

◆ IR-safe E-flow tensor: 
$$I_w^{kl} = \frac{1}{m_J} \sum_i w_i \frac{p_{i,k}}{w_i} \frac{p_{i,l}}{w_i}$$

◆ Planar flow: 
$$Pf = \frac{4 \det(I_w)}{\text{tr}(I_w)^2} = \frac{4\lambda_1 \lambda_2}{(\lambda_1 + \lambda_2)^2}$$

# Planar flow (Pf), QCD vs top jets

---

- ◆ LO: Pf  $\sim 0$  for QCD (2-body decay)

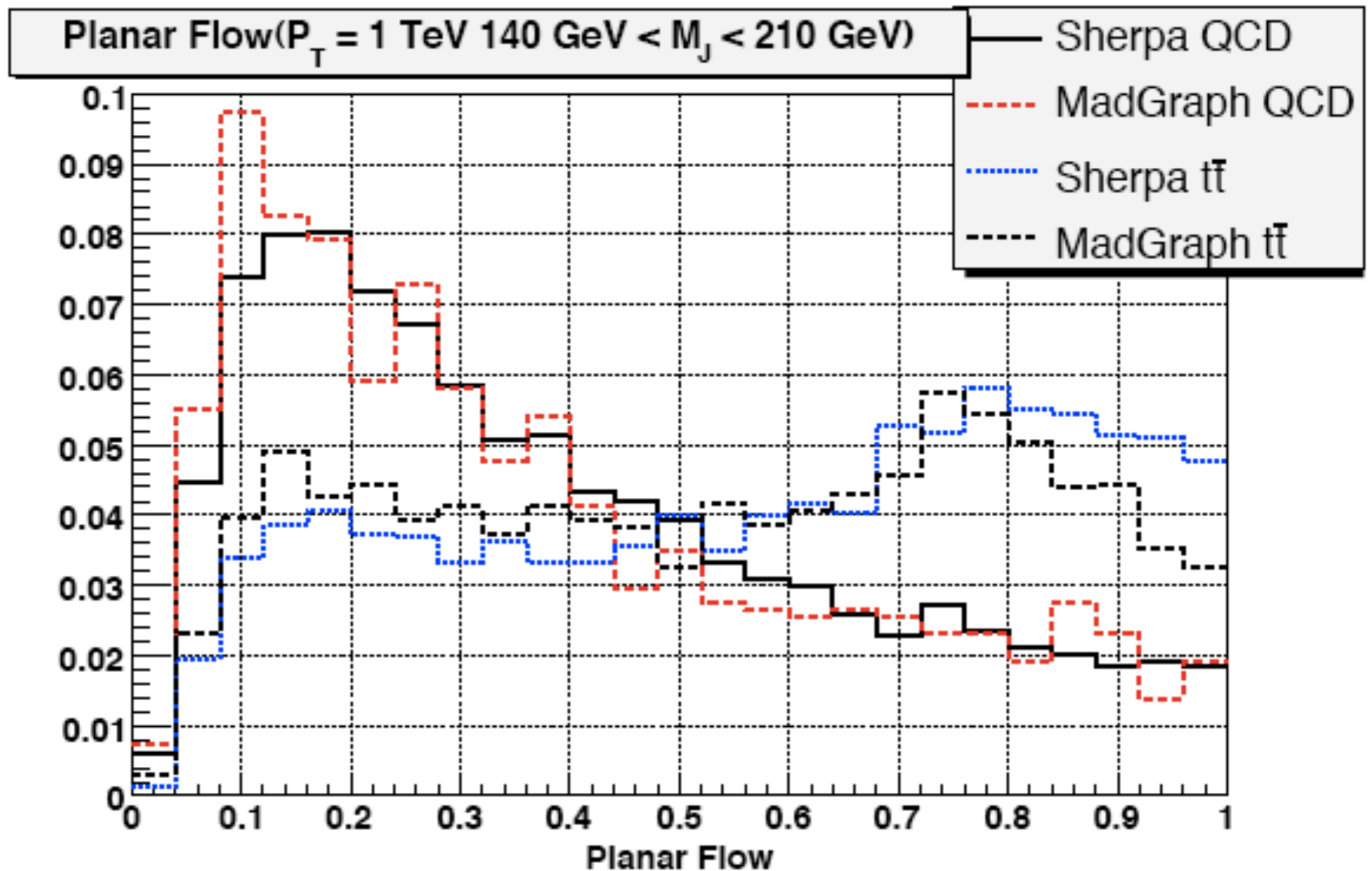
$$\frac{1}{J} \left( \frac{dJ}{dPf} \right)_{2\text{body}} = \delta(Pf)$$

O(1) for top: smooth

(for isotropic  $\geq 3$ -body decay, Pf  $\sim 1$ )

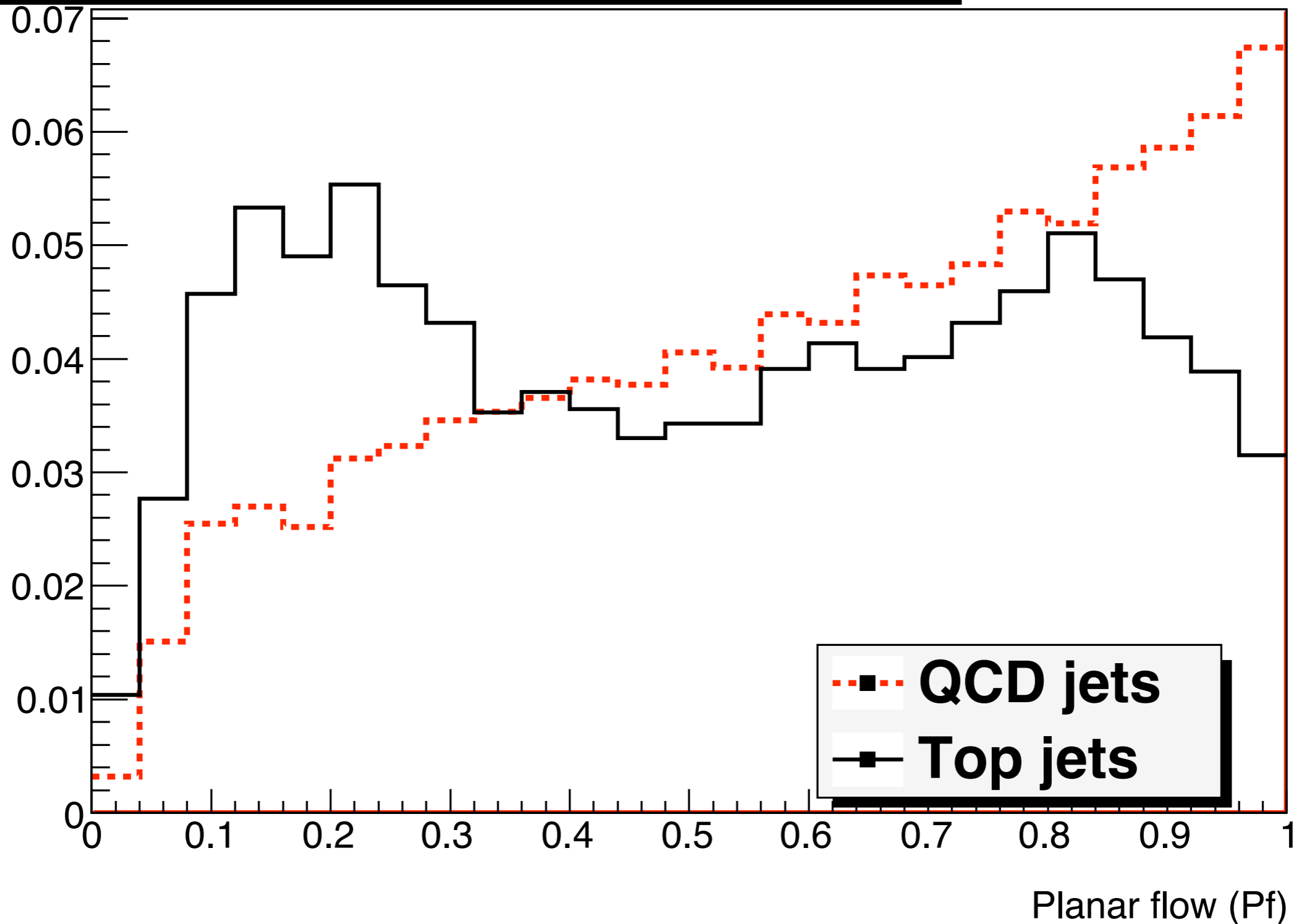
- ◆ NLO (due to large m): O( $\alpha_s$ ) for QCD  
nominal for top

# Planar flow (Pf), QCD vs top jets



# Planar flow (Pf), QCD vs top jets

Planar flow, Pf ( $P_T = 1$  TeV,  $R = 0.4$ , "no mass cuts")



# What about 2 body jet, Z/W/h

Berger, Kucs and Sterman (03): introduced for e+e- annihilation

◆ Angularities on a cone: *Almeida, SJL, Perez, Sterman, Sung, & Virzi, arXiv:0807.0234*

$$\tilde{\tau}_a(R, p_T) = \frac{1}{m_J} \sum_{i \in \text{jet}} \omega_i \sin^a \left( \frac{\pi \theta_i}{2R} \right) \left[ 1 - \cos \left( \frac{\pi \theta_i}{2R} \right) \right]^{1-a}$$

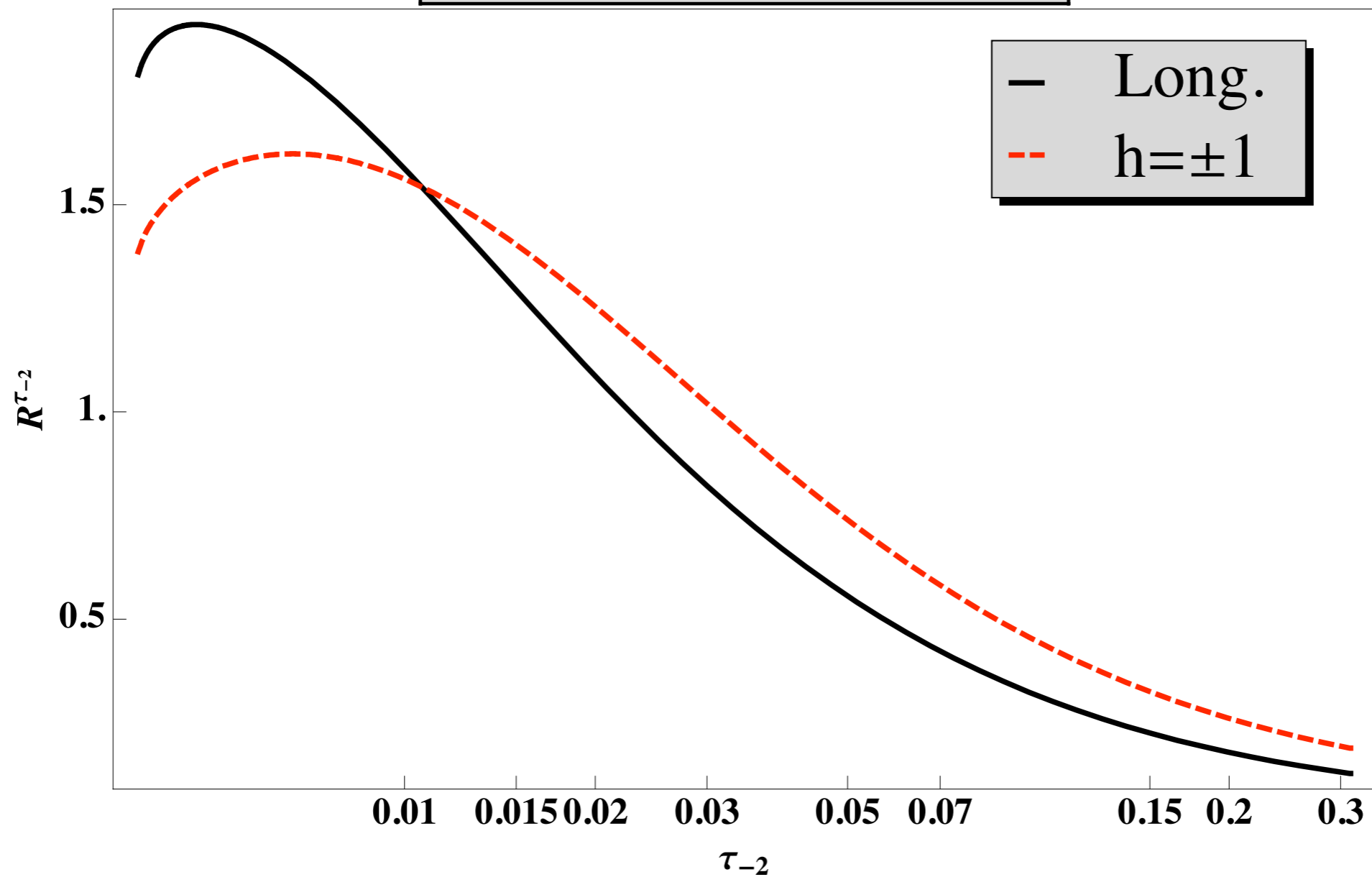
$$P^x(\theta_s) = (dJ^x / d\theta_s) / J^x \Rightarrow P^x(\tilde{\tau}_a)$$

$$R(\tilde{\tau}_a) = \frac{P^{\text{sig}}(\tilde{\tau}_a)}{P^{\text{QCD}}(\tilde{\tau}_a)}$$



# Theory: angularity, QCD vs Z

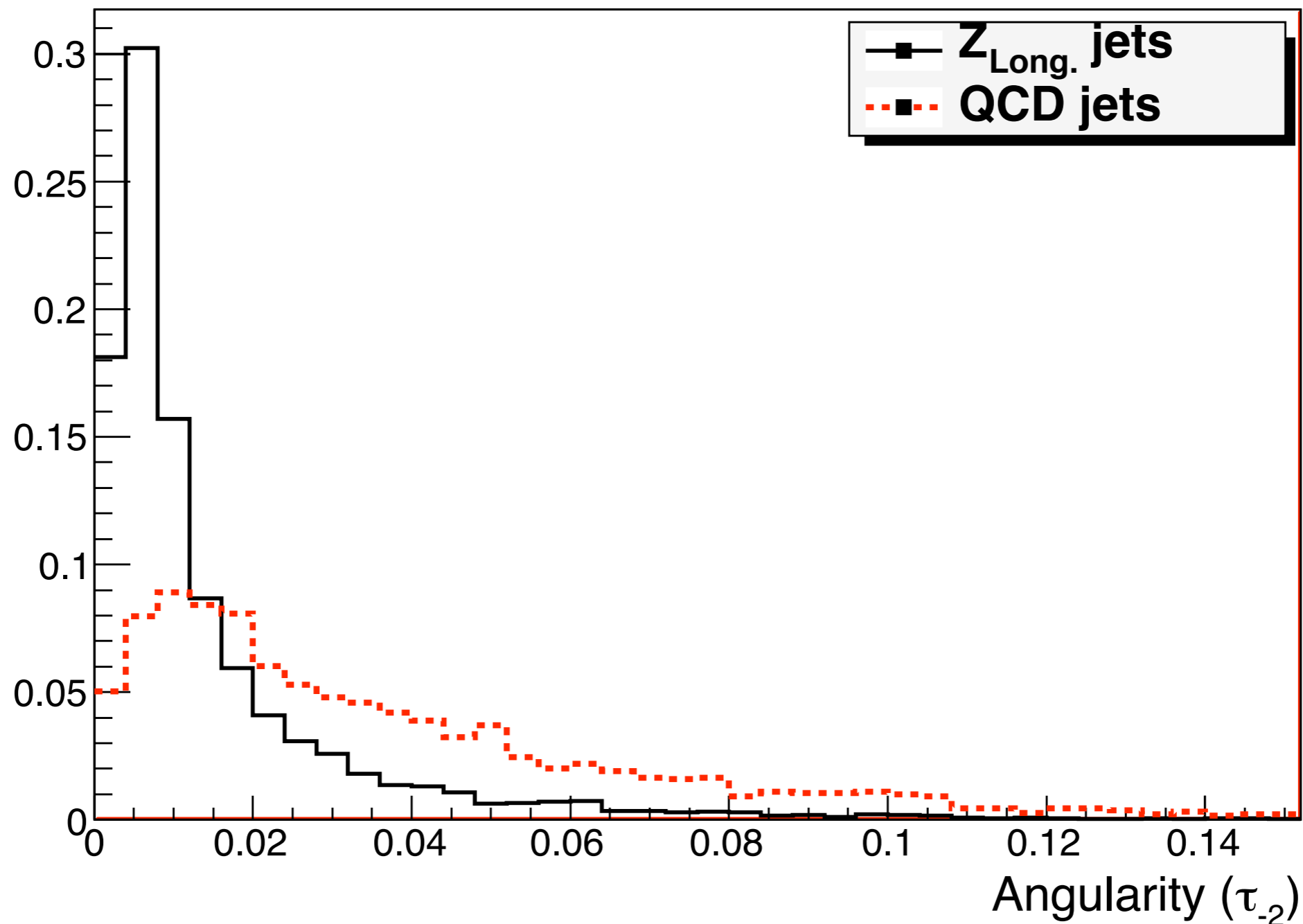
$R^{\tau_{-2}}$  vs.  $\tau_{-2}$  for  $z=0.05$



MG/ME

# Madgraph: angularity, QCD vs Z

Angularity,  $\tau_a$  ( $a = -2, z = 0.05, R = 0.4$ )



MG/ME

# Top Polarization

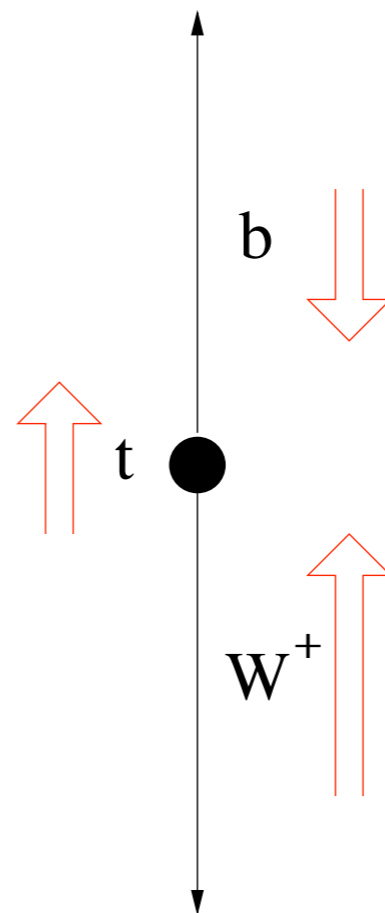
---

- ◆ Daughter particles remember top polarization
- ◆ For Urel' top: **helicity=chirality**
  - Can do polarization analysis like it was done for the tau
- ◆ Want to use  $P_T$  to probe top polarization:  $P_T$  is a directly measured quantity (c.f. For polarization method, need to use derived quantities with biases, like center of mass boost etc.)
  - Different from spin-spin correlation where you expand in s wave (for non-relativistic top)

# Top Polarization

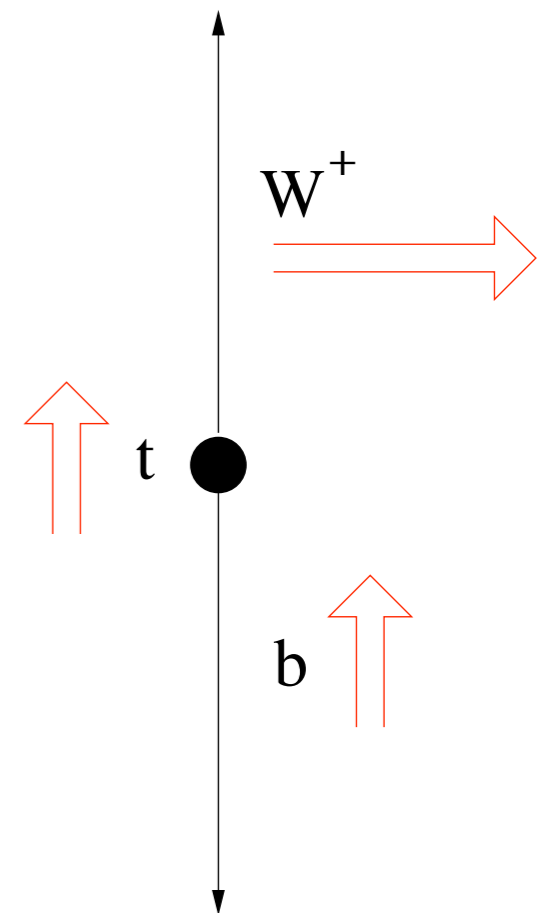
---

~30%



Left-Handed W

~70%

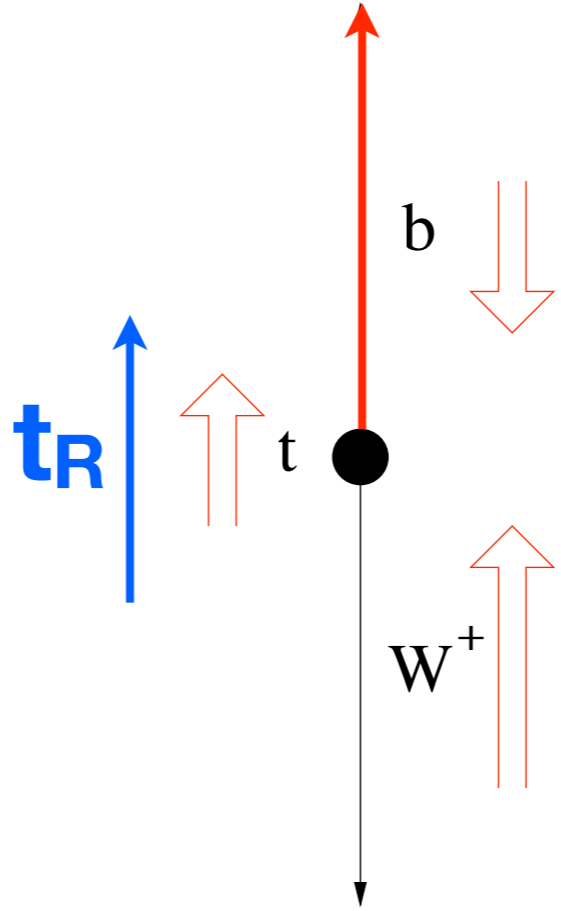


Longitudinal W

# Top Polarization

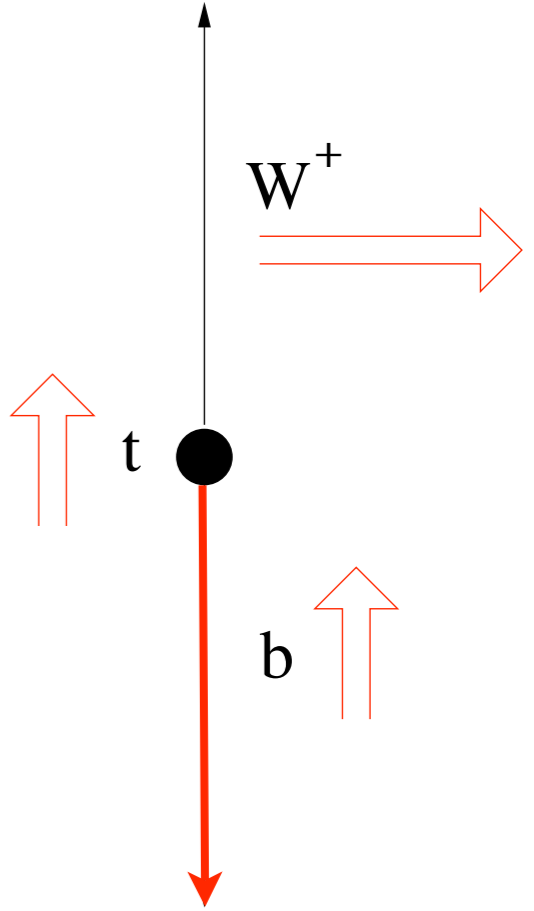
---

~30%



Left-Handed W

~70%



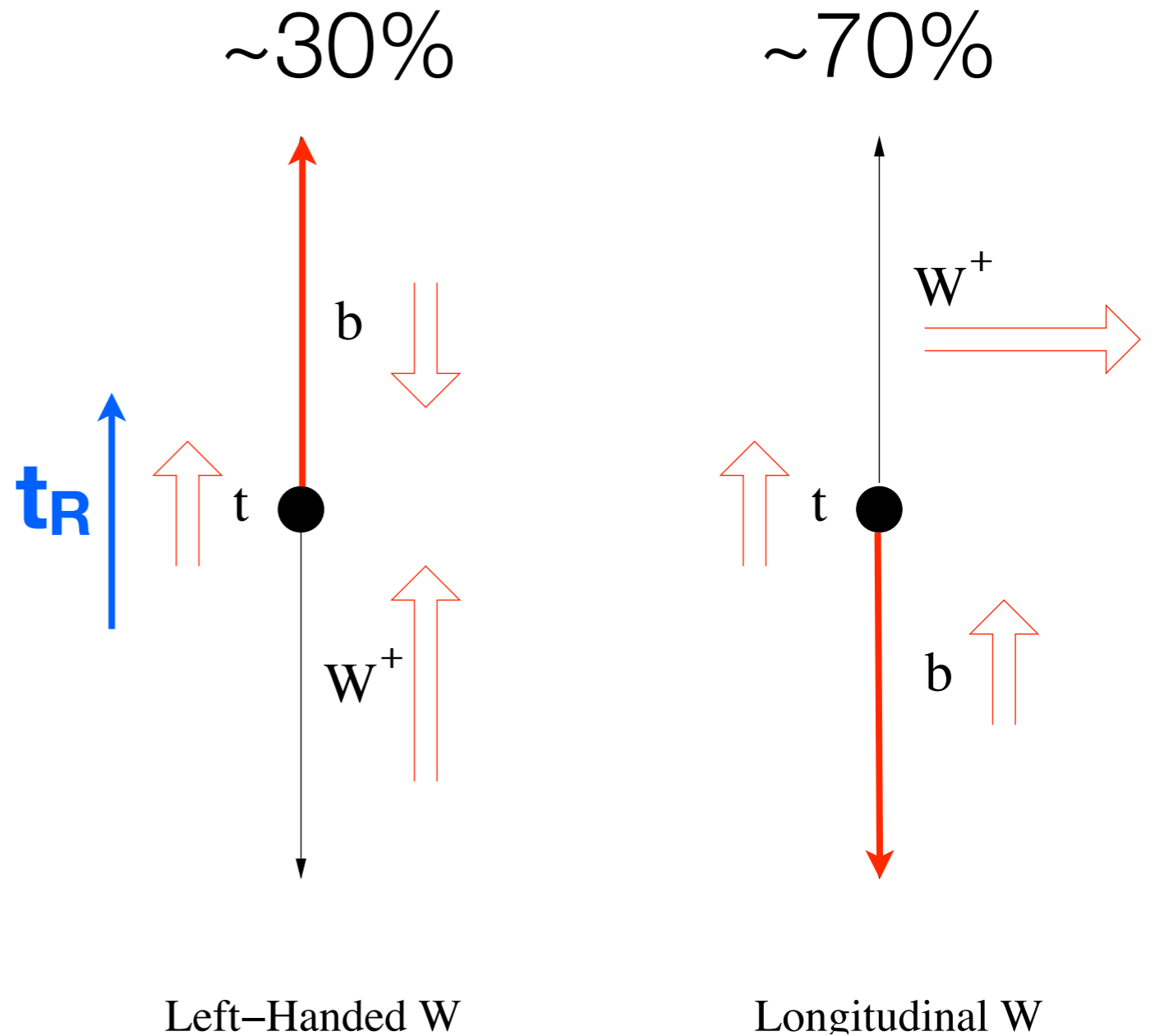
Longitudinal W

# Top Polarization

## ◆ b quark:

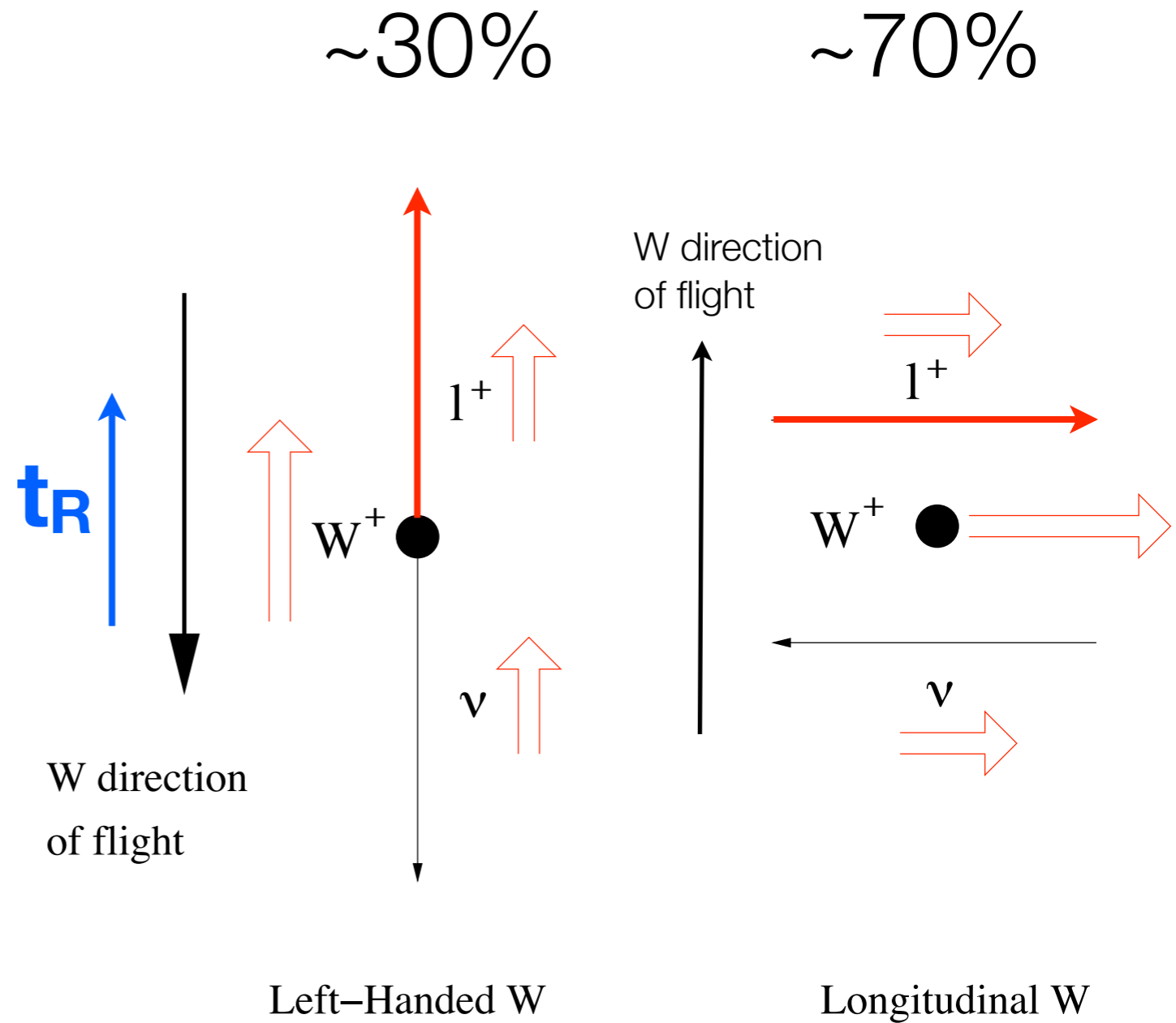
- **back-warded** (soft  $P_T$ )  
for  $t_R$
- **forwarded** (hard  $P_T$ )  
for  $t_L$

- ◆ For SM, parity even  
( $P_T$  distribution will be flat) → look for new  
Physics where parity is  
violated



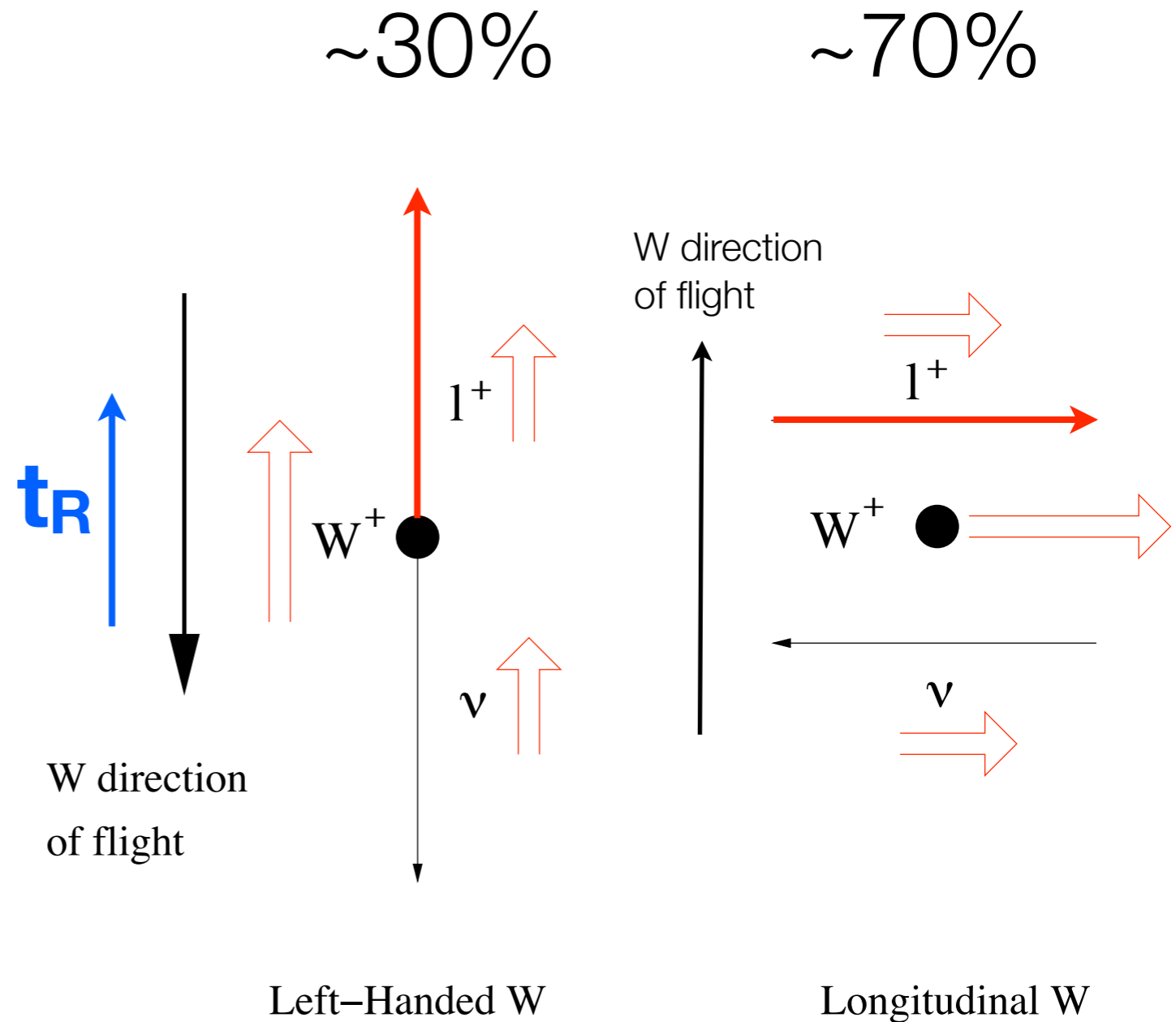
# Top Polarization

- lepton: **forwarded** for  $t_R$   
**back-warded** for  $t_L$



# Top Polarization

- lepton: **forwarded** for  $t_R$   
**back-warded** for  $t_L$



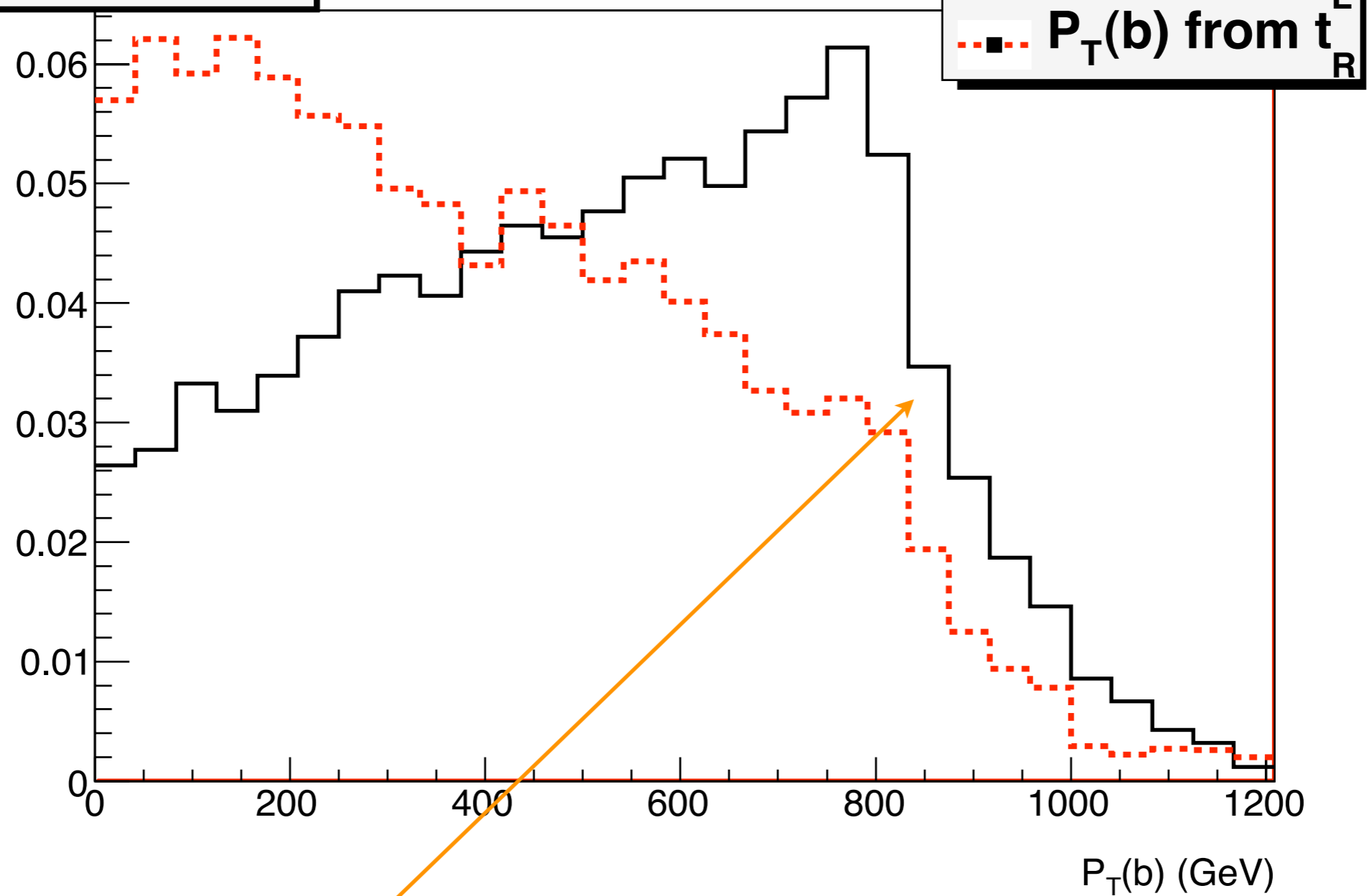
For Boosted Longitudinal W: lepton is forwarded



$p_T(\text{top}) > 1\text{TeV}$

MG/ME

$P_T(b)$  distribution



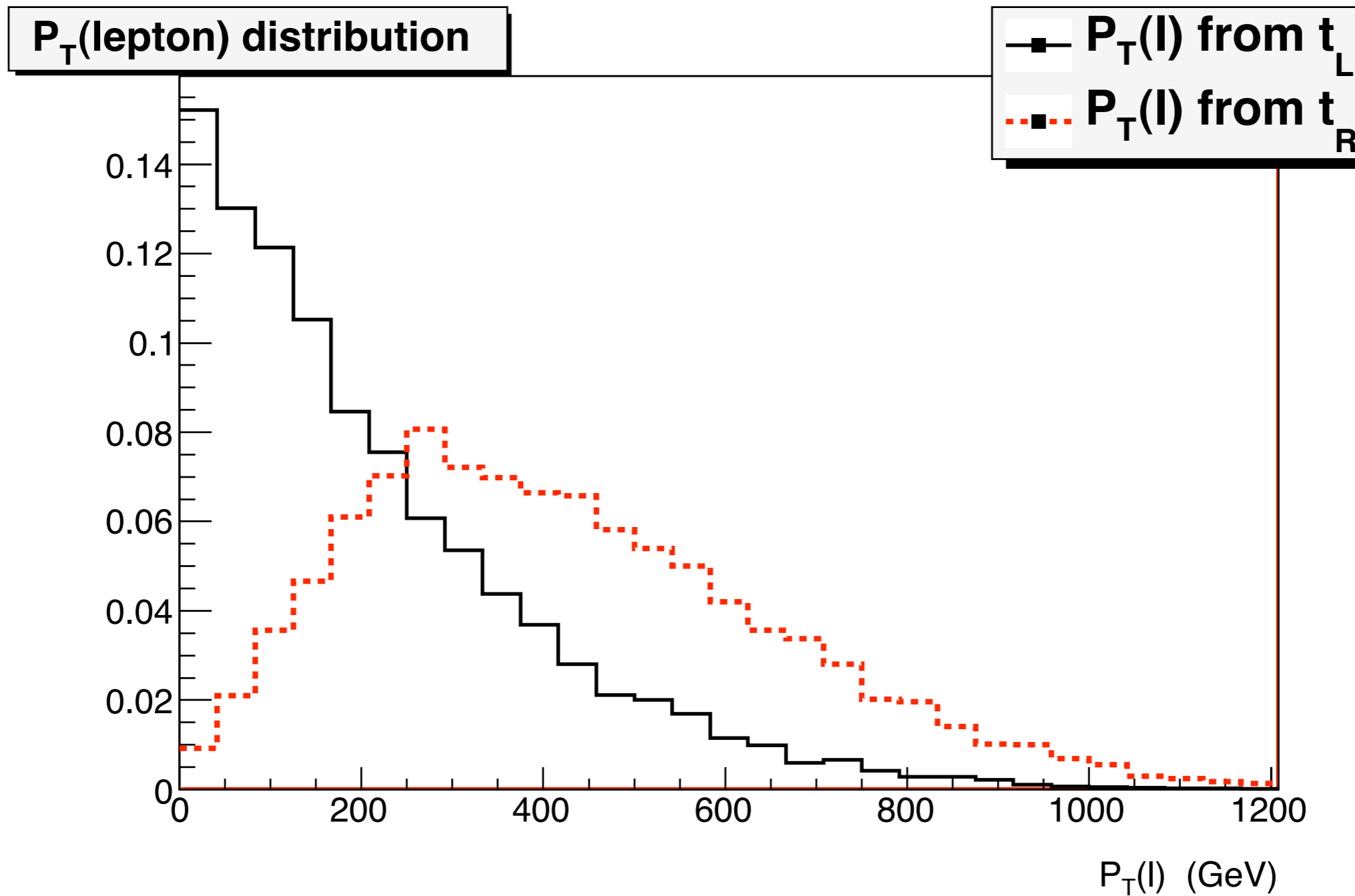
$P_T(b)$  is limited by  $W$  boson mass

**Hadronic Top**

$b$  quark as a spin analyzer

$p_T(\text{top}) > 1 \text{ TeV}$

MG/ME



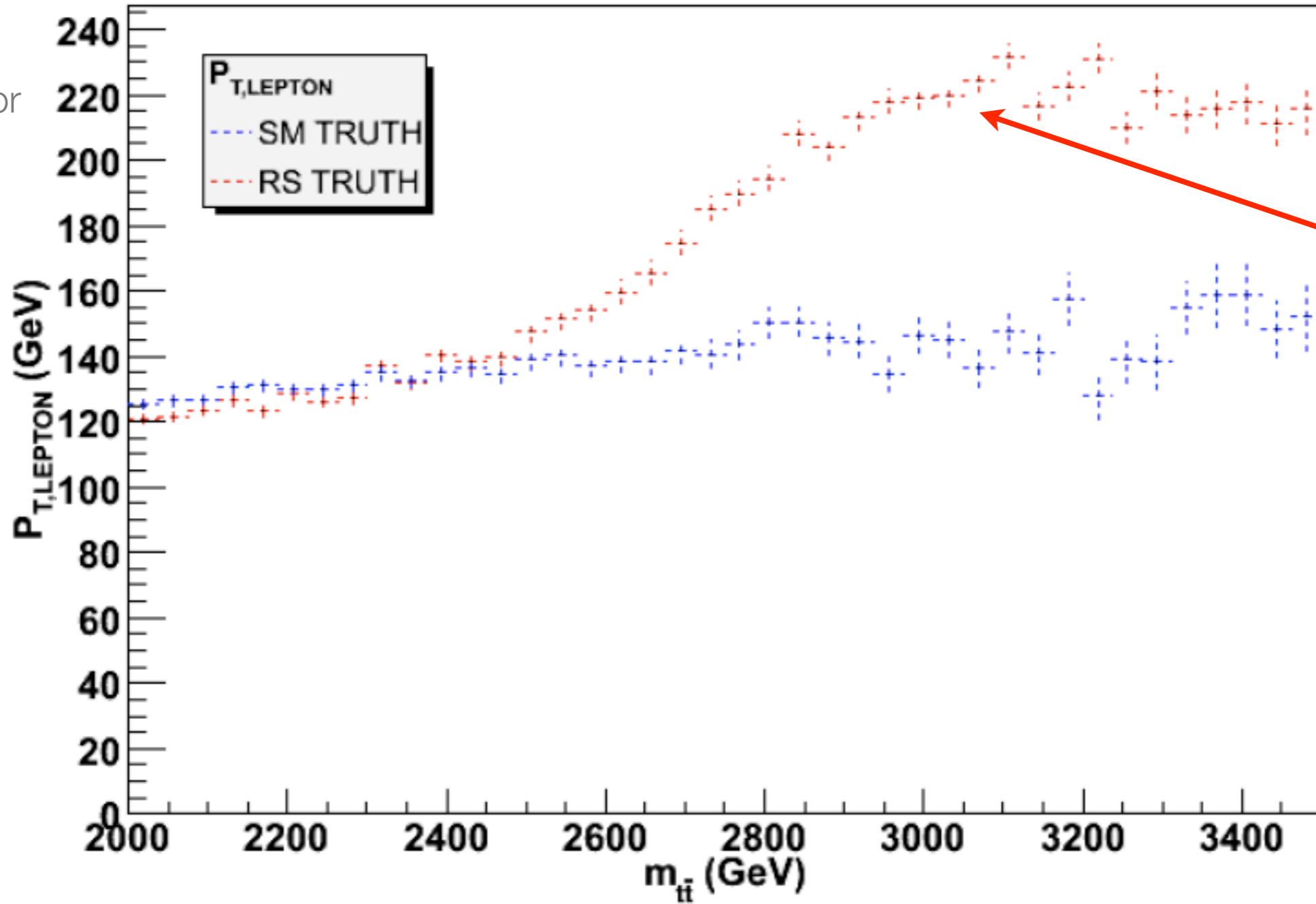
• for example with the KK gluon, you'll see suddenly only leptons/bs that follows the RH curves

**Leptonic Top**

charged lepton as a  
spin analyzer

$P_{T,LEPTON}$

Sherpa (CKKW)  
Without Detector  
Simulation

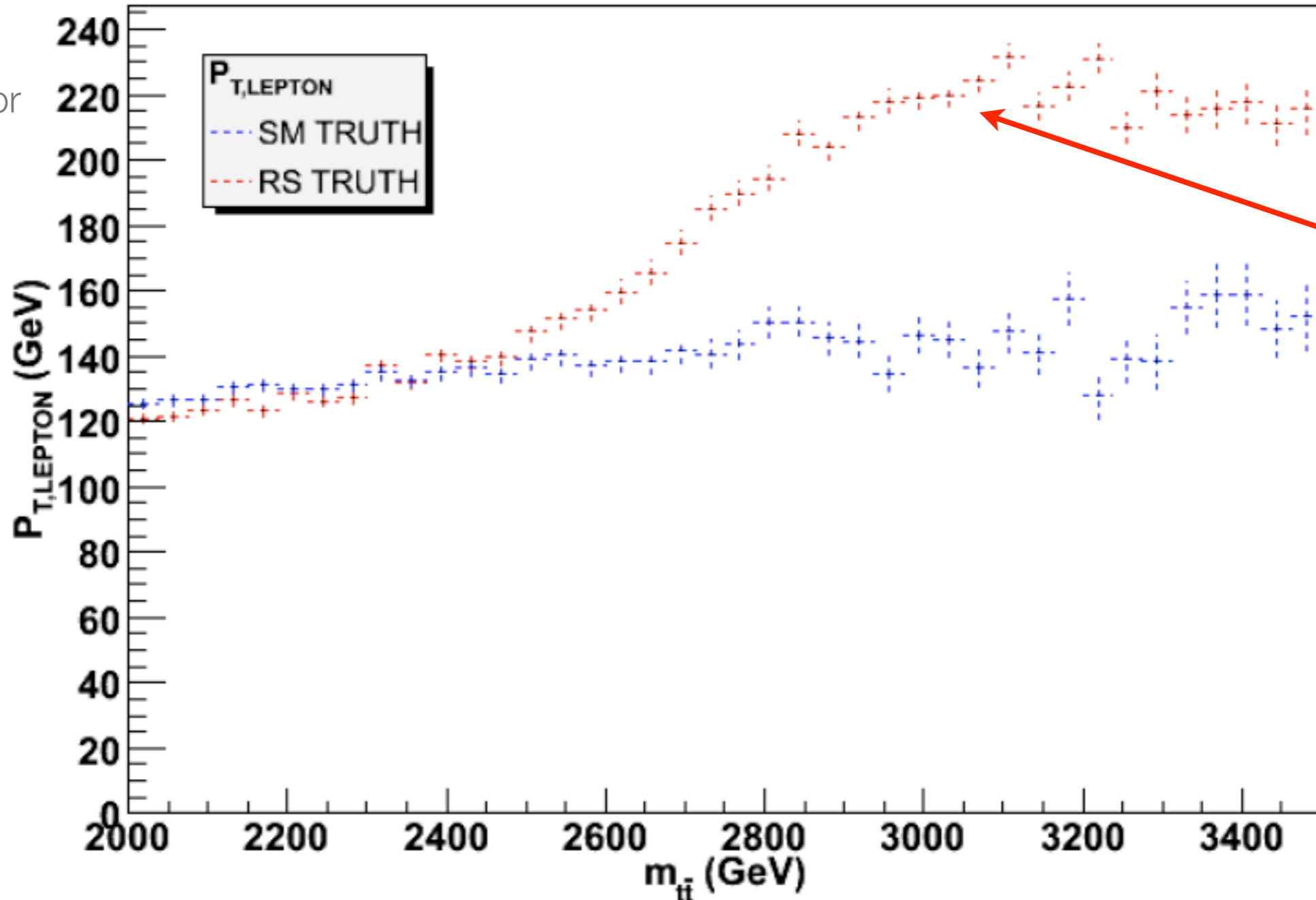


Example: KK gluon

lepton  $P_T$  is harder near  
the KK gluon plateau

$P_{T,LEPTON}$

Sherpa (CKKW)  
Without Detector  
Simulation



KK  
gluon  
bump

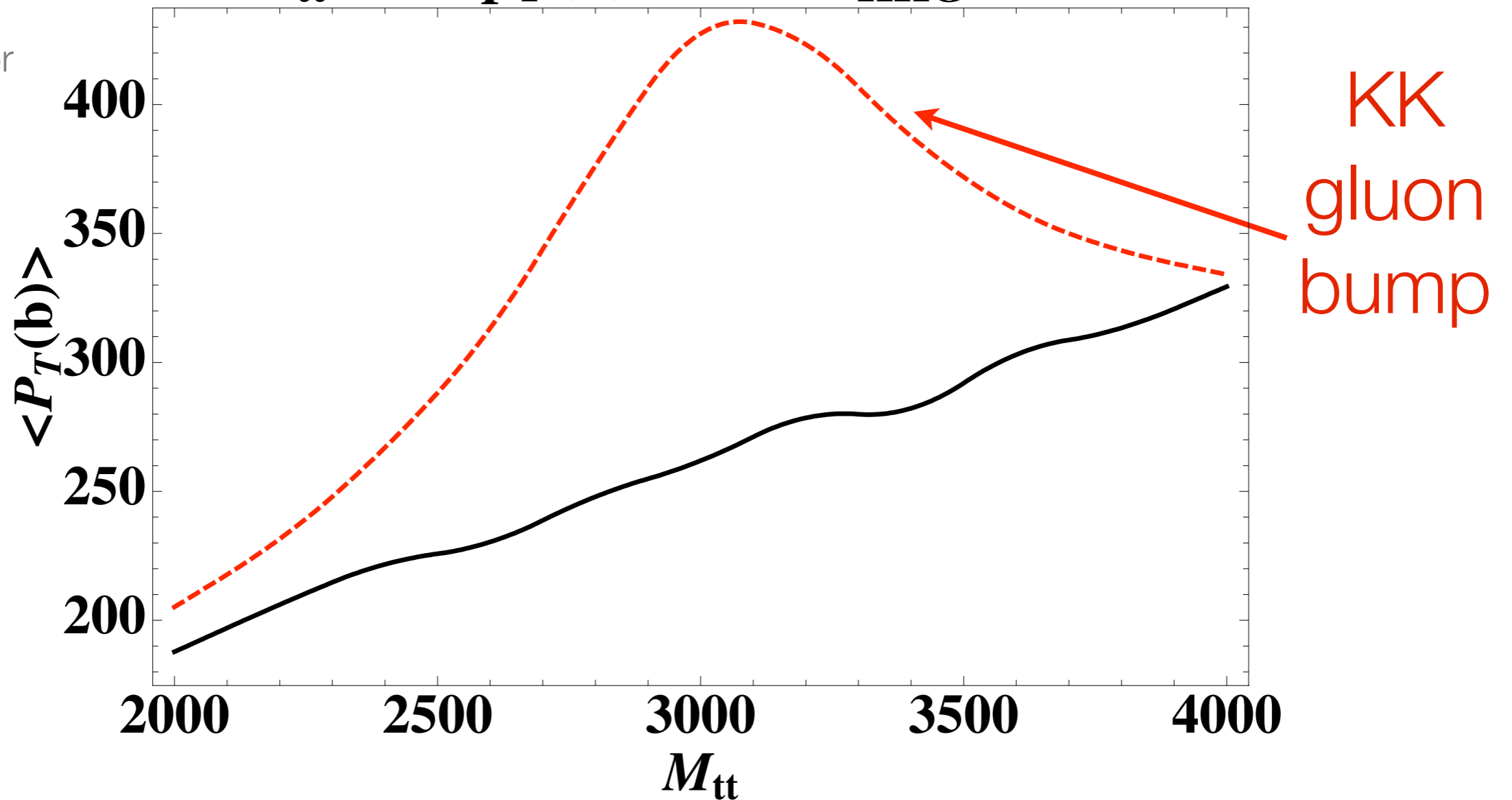
Also relevant for SUSY: heavy stop decaying into top and wino, etc...

Example: KK gluon

lepton  $P_T$  is harder near  
the KK gluon plateau

# $M_{tt}$ vs. $\langle p_T(b) \rangle$ for $M_{KKG}=3\text{TeV}$

MG/ME  
Without Detector  
Simulation

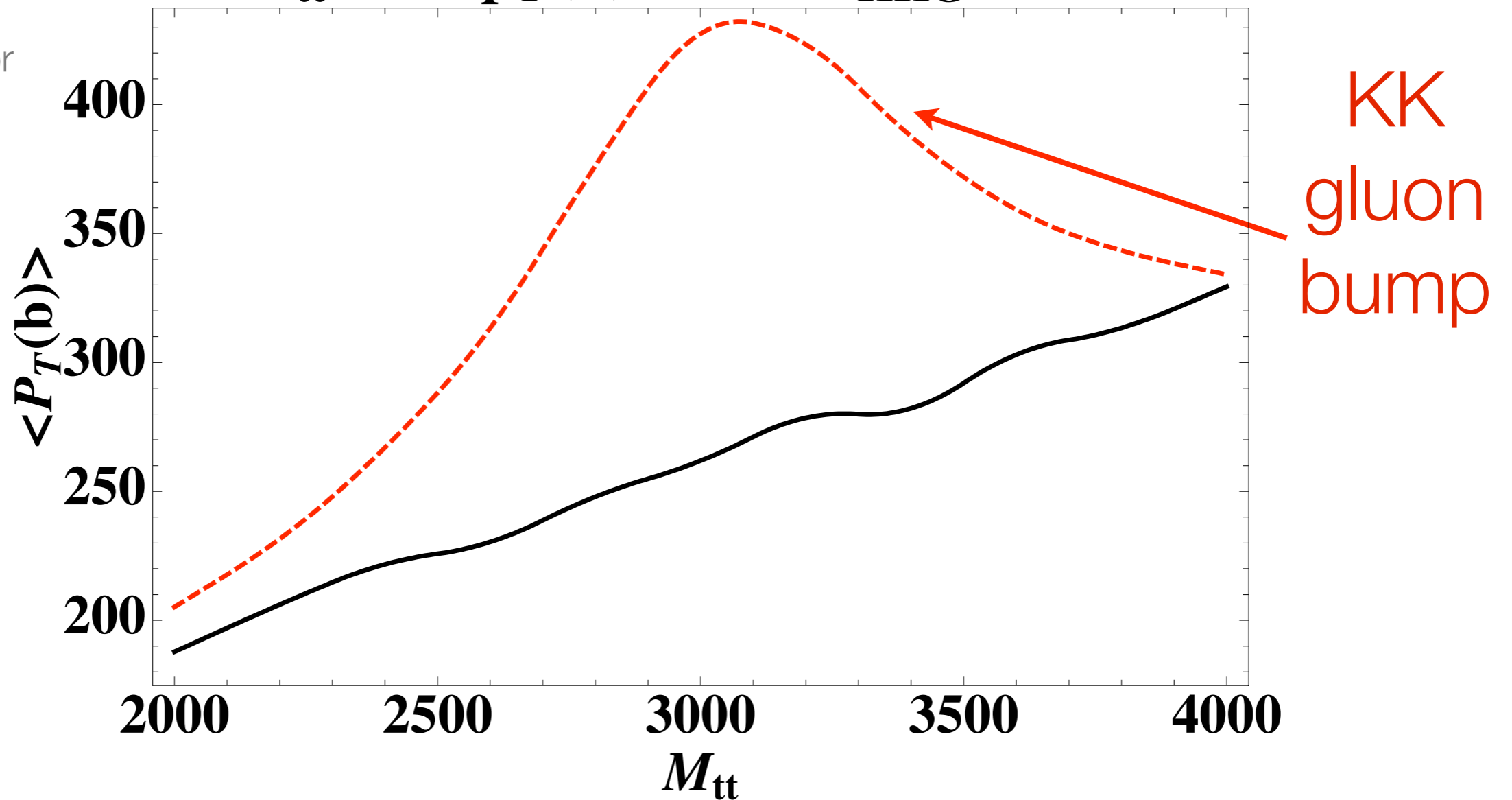


Example: KK gluon

b-quark  $P_T$  is harder near the KK gluon bump

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MG/ME  
Without Detector  
Simulation



Also relevant for SUSY: heavy stop decaying into top and wino, etc...

**Example: KK gluon**

b-quark  $P_T$  is harder near the KK gluon bump

# Summary

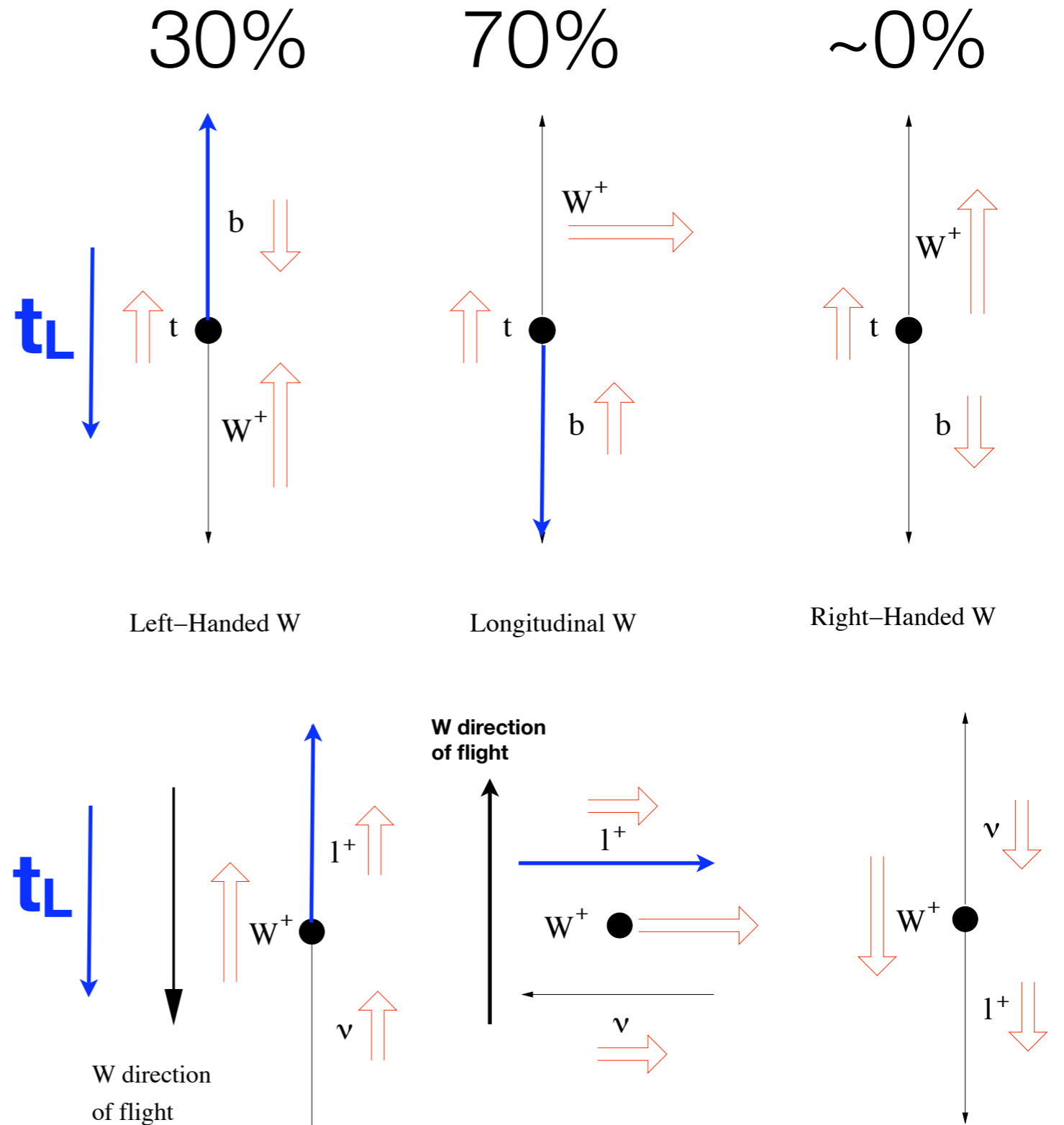
---

- ◆ LHC => new era, precision top physics
- ◆ Theory+technique to tag t/W/Z/h jets
- ◆ Understand jet mass, but it's not enough
- ◆ Introduce Jet-shapes: very useful, but more to do (exp'+analyses+theory)



# Backup: Top Polarization

- Polarization: daughter particles of top still remembers the information
- $b$  is **forwarded** for  $t_L$
- lepton is **back-warded** for  $t_L$
- lepton is in general better spin analyzer compared to  $b$ -quark, **but  $b$  can be used for the hadronic top**



# Backup: 30% B-tagging efficiency & 1% light jet

**Jet Mass**

**Peak Resolution**

- Background Fit
- Background + Signal Fit

