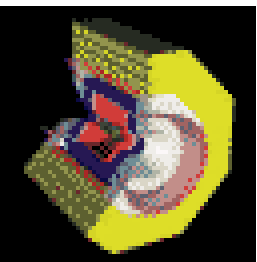


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# Measurements of $D^+$ & $D_s$ decay constants at CLEO

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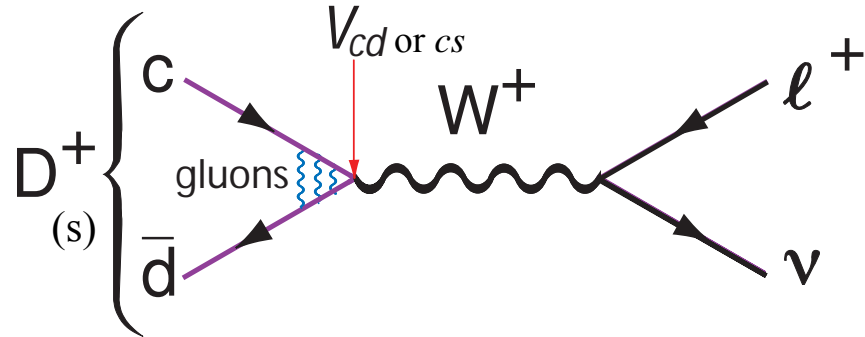
Liming Zhang  
Syracuse University



# Leptonic Decays: $D \rightarrow \ell^+ \nu$

c and  $\bar{q}$  can annihilate, probability is proportional to wave function overlap

Standard Model  
decay diagram:



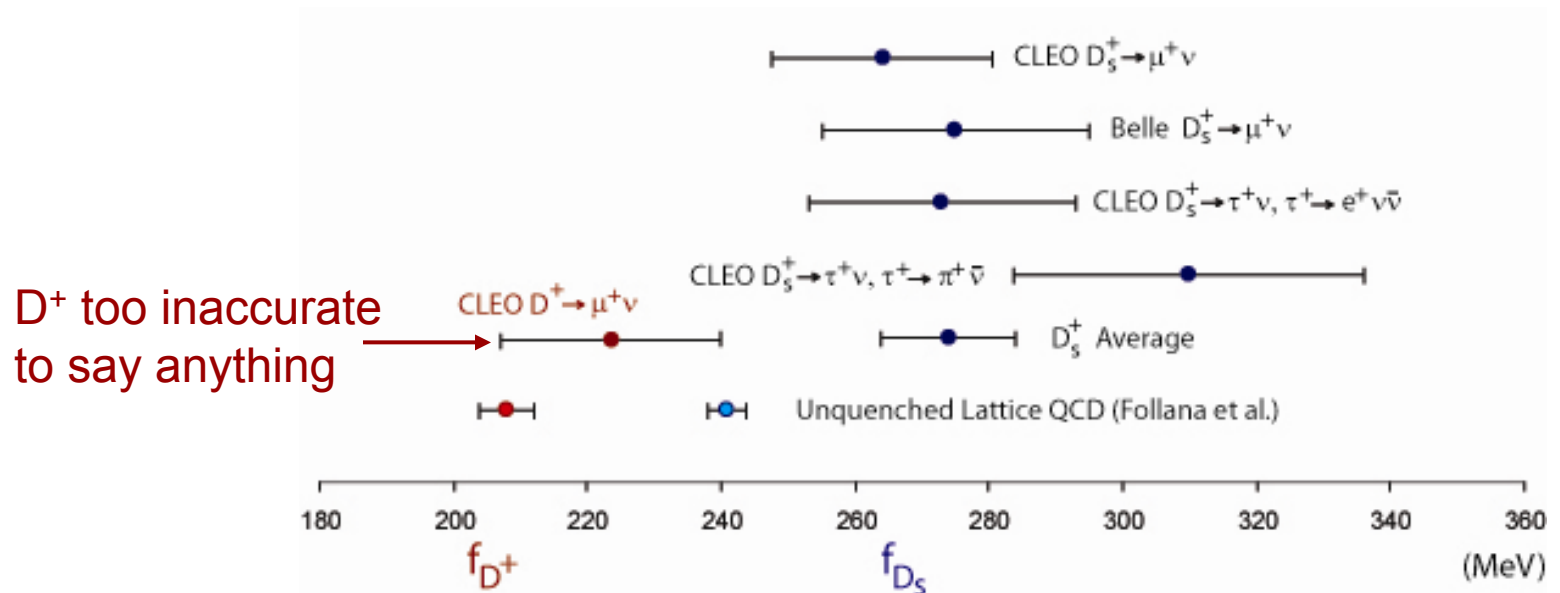
In general for all pseudoscalars:

$$\Gamma(P^+ \rightarrow \ell^+ \nu) = \frac{1}{8\pi} G_F^2 f_P^2 m_\ell^2 M_P \left(1 - \frac{m_\ell^2}{M_P^2}\right)^2 |V_{Qq}|^2$$

- $f_P$  is decay constant, related to the overlap of the heavy and light quark wave-functions at zero spatial separation.
- $V_{Qq}$  is known, here take  $V_{cd} = V_{us} = 0.2256$ ,  $V_{cs} = V_{ud} = 0.9742$

# A Window to New Physics?

- CLEO's previous measurement of  $f_{D_s}$  + Belle's (see Rosner & Stone arXiv:0802.1043) give  $f_{D_s}=274\pm 10$  MeV as compared with  $241\pm 3$  MeV 2+1 unquenched lattice QCD calculation of Follana et.al (PRL 100, 062002 (2008))
- CLEO's previous measurement of  $f_{D^+}$  was too inaccurate to challenge Follana et al., theory  $207\pm 4$  versus  $223\pm 17$  MeV (CLEO)
- Dobrescu & Kronfeld (arXiv:0803.0512) argue that this can well be the effect of NP, either charged Higgs (their own model) or leptoquarks



# CLEO's Technique for $D^+ \rightarrow \mu^+ \nu$

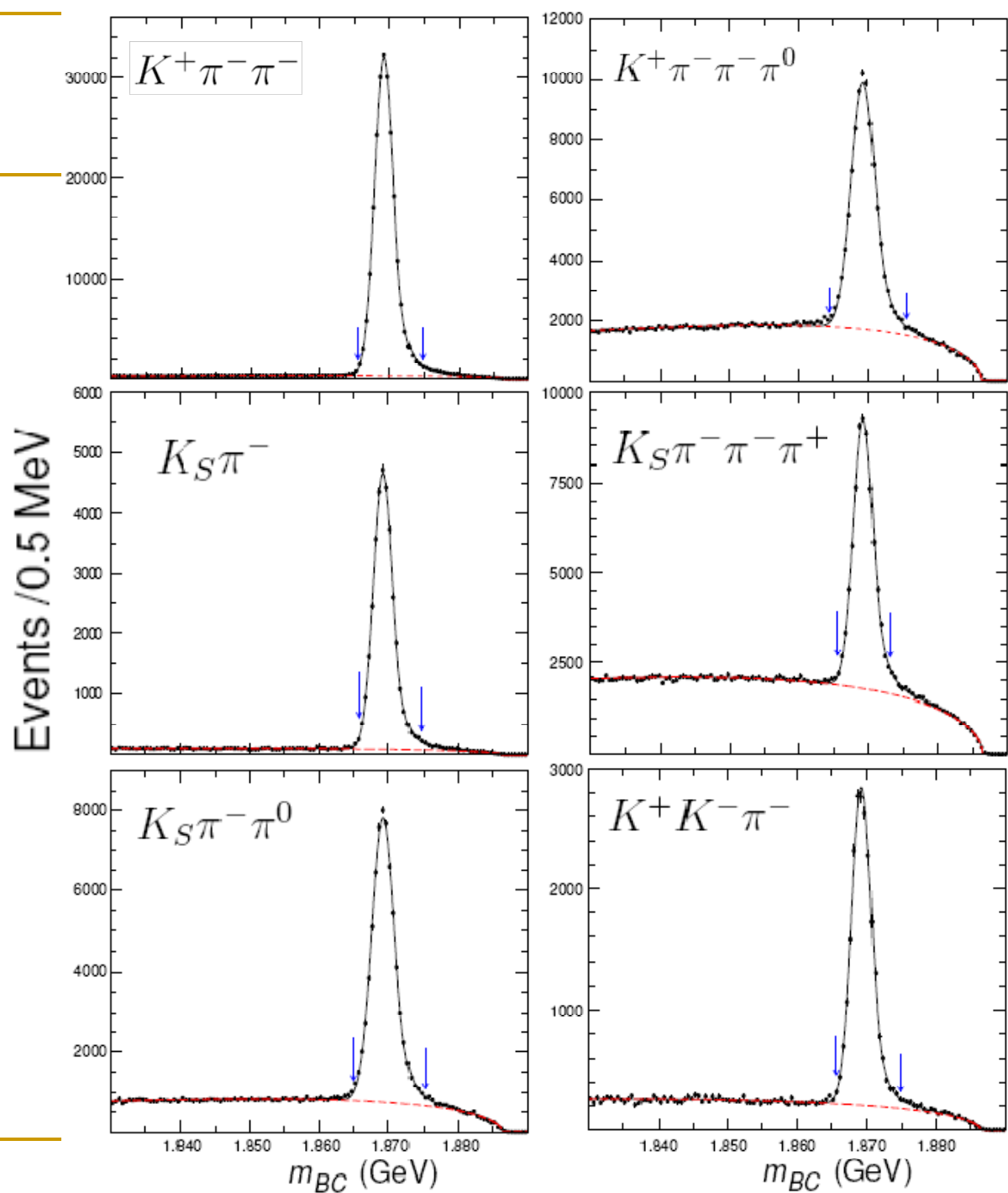
- 818 pb<sup>-1</sup> of data at  $\psi(3770)$
- Fully reconstruct a  $D^-$ , and count total # of tags
- Seek events with only one additional oppositely charged track within  $|\cos\theta| < 0.9$  & no additional photons  $> 250$  MeV (to veto  $D^+ \rightarrow \pi^+ \pi^0$ )
- Charged track must deposit only minimum ionization in calorimeter [ $E < 300$  MeV: case (i)]
- Compute  $MM^2$ . If close to zero then almost certainly we have a  $\mu^+ \nu$  decay.

$$MM^2 = (E_{D^+} - E_{\ell^+})^2 - (\vec{p}_{D^+} - \vec{p}_{\ell^+})^2$$

We know  $E_{D^+} = E_{\text{beam}}$ ,  $\mathbf{p}_{D^+} = -\mathbf{p}_{D^-}$

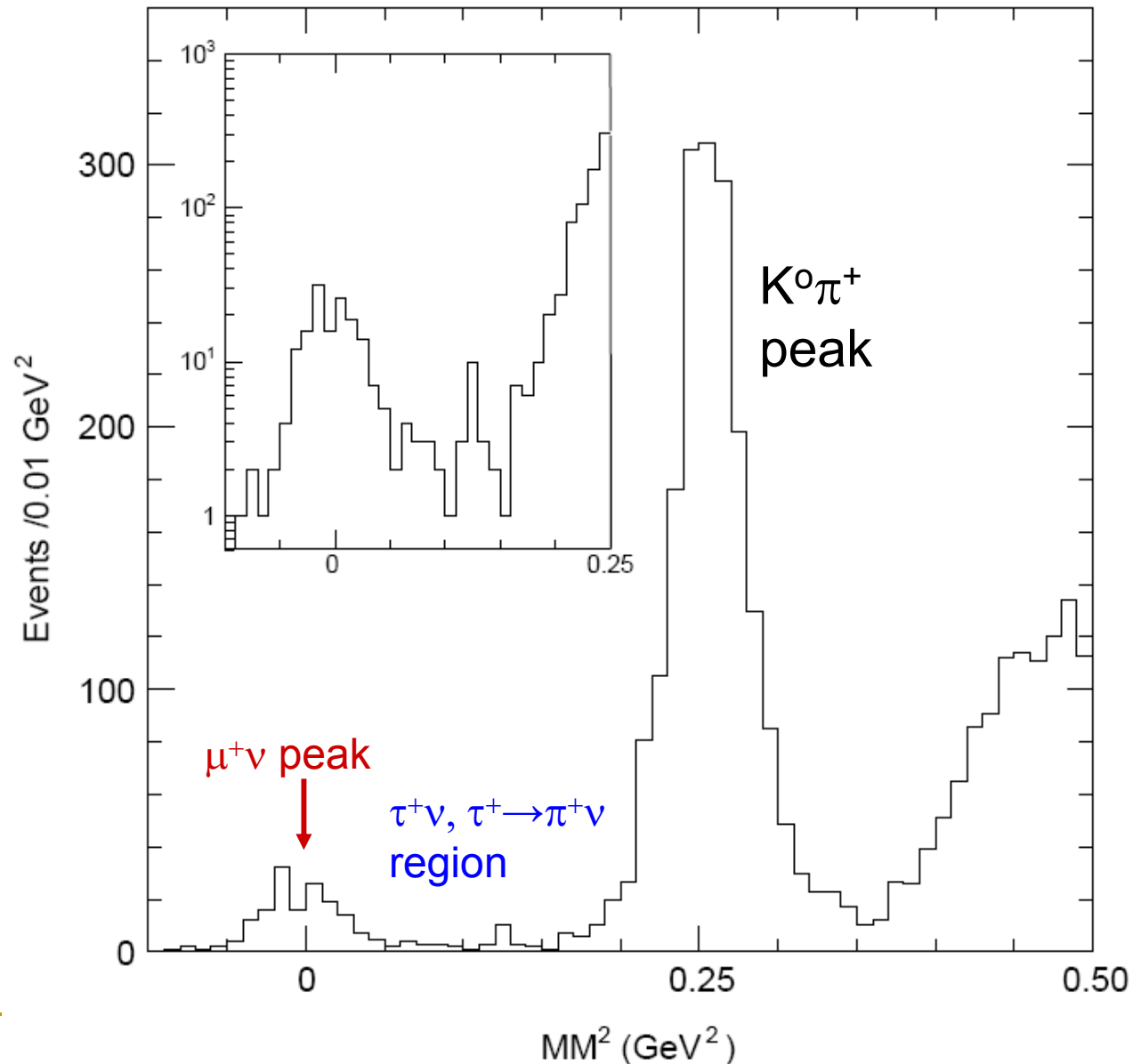
# Tags

- Total of 460,000
- Background 89,400



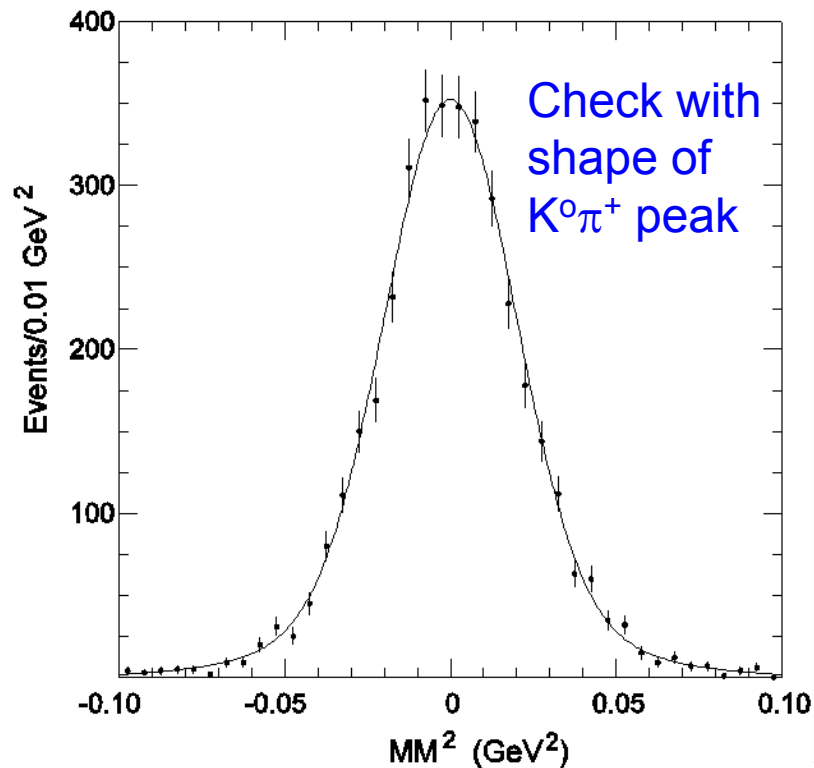
# The $MM^2$ Distribution

- For  $E < 300$  MeV in CsI

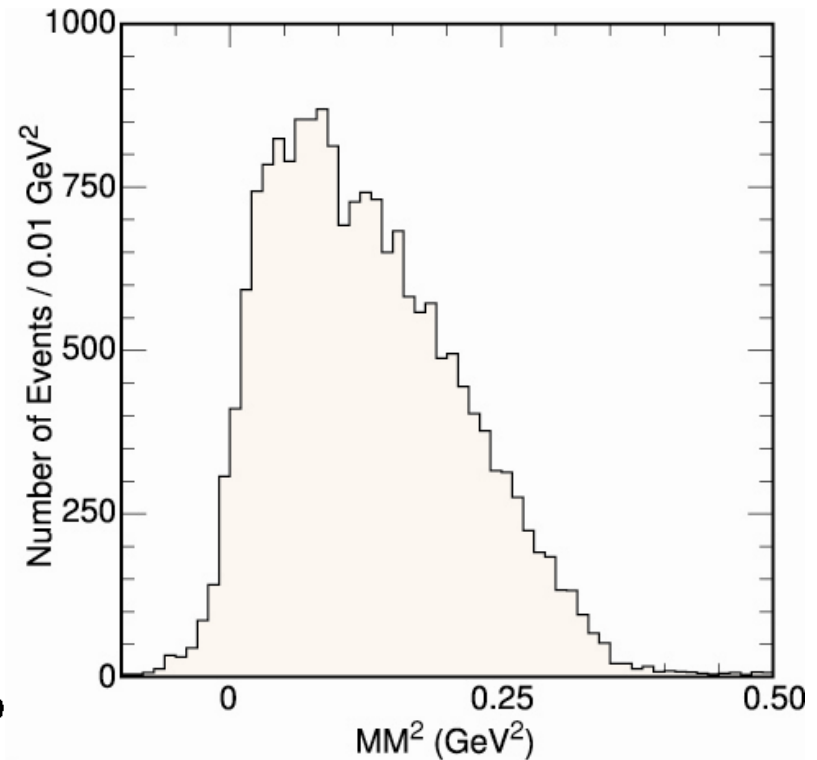


# MM<sup>2</sup> Signal Shapes

$$MM^2 = (E_{Beam} - E_{\ell^+})^2 - (-\vec{p}_{D^-} - \vec{p}_{\ell^+})^2$$



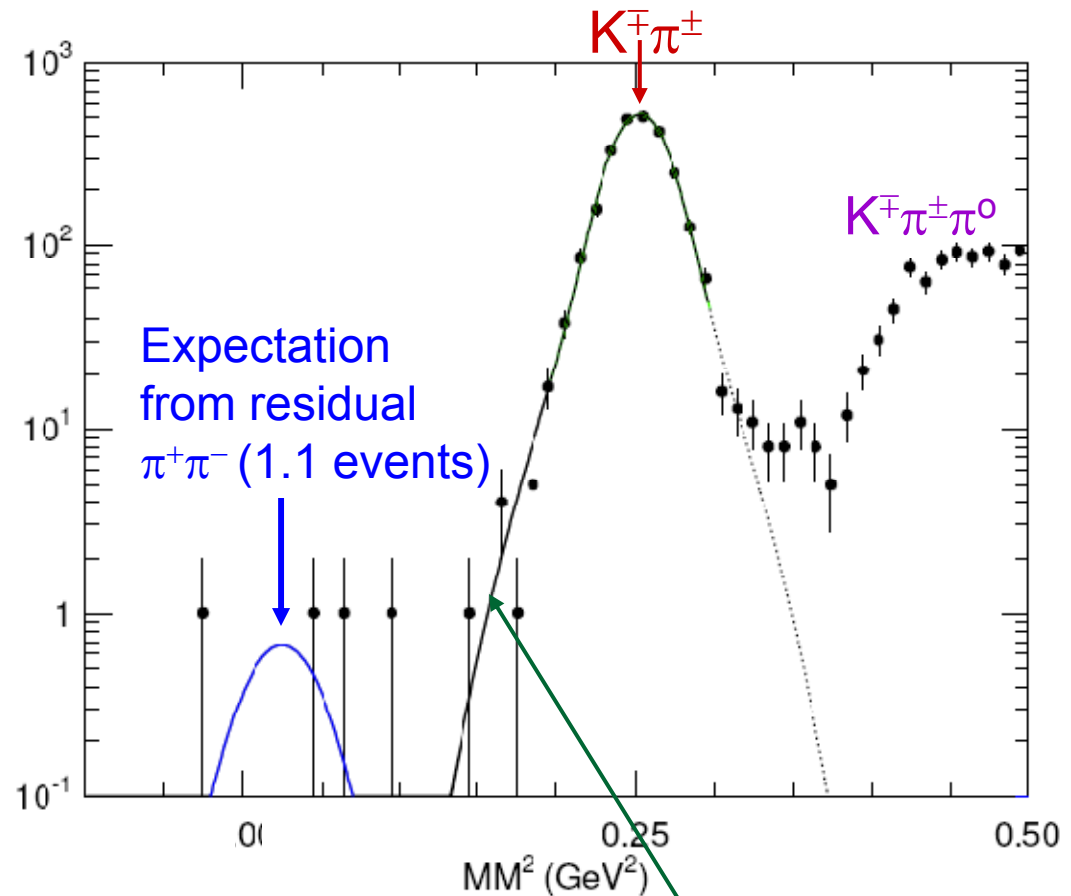
Monte Carlo Signal  $\mu\nu$



Monte Carlo Signal  $\tau\nu, \tau \rightarrow \pi\nu$

# Model of $K^0\pi^+$ Tail

- Use double tag  $D^0$   $\bar{D}^0$  events, where both  $D^0 \rightarrow K^{\mp}\pi^{\pm}$
- Make loose cuts on 2<sup>nd</sup>  $D^0$  so as not to bias distribution: require only 4 charged tracks in the event



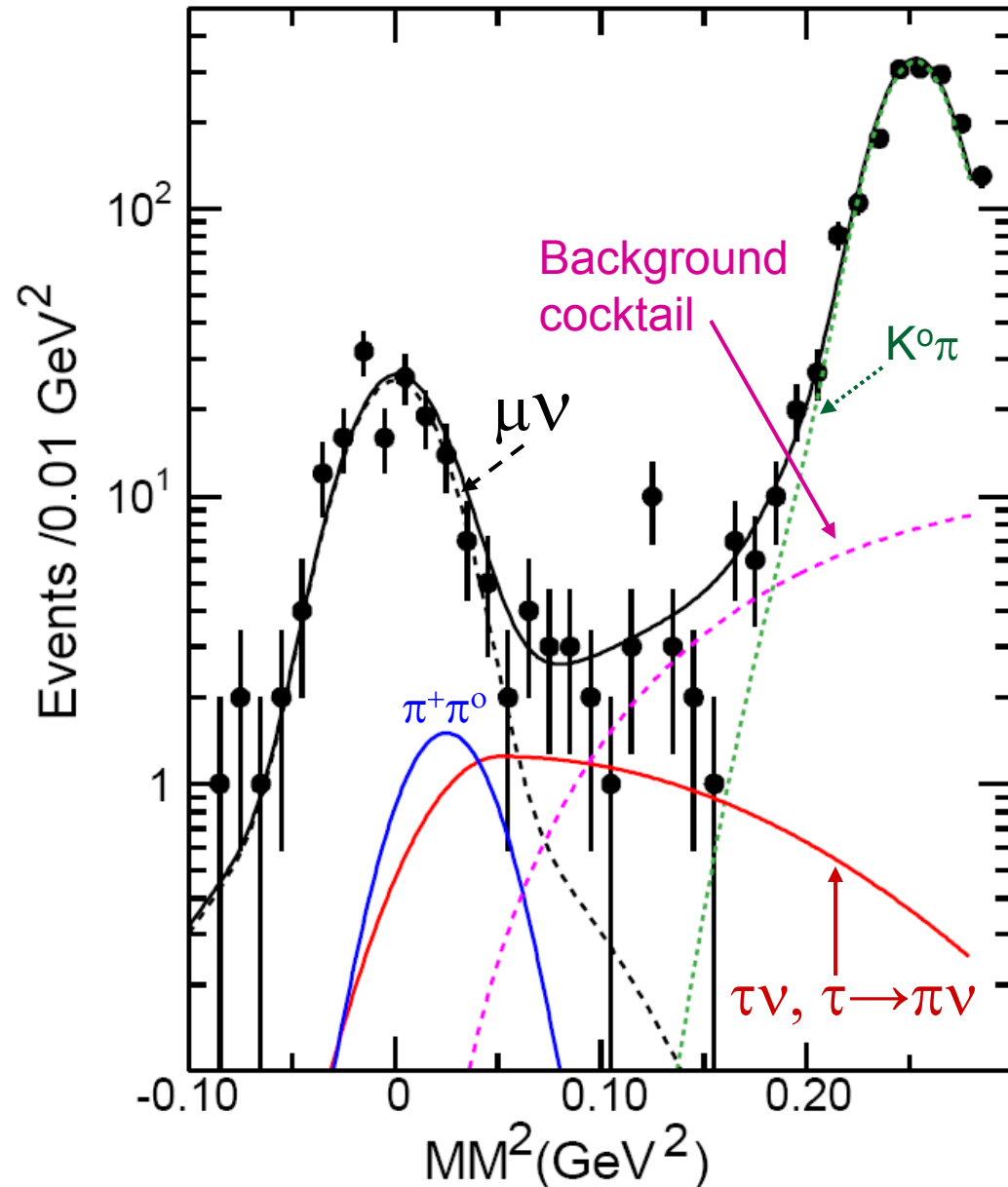
Computed ignoring charged kaon

Gives an excellent description of shape of low mass tail  
“Extra” 1.3 event background in signal region



# Fit $MM^2$ to sum of signal & bkgd

- Case(i)  $E < 300$  MeV where  $\tau^+\nu/\mu^+\nu$  is **fixed** to SM ratio 2.65
  - $149.7 \pm 12.0 \mu\nu$
  - $25.8 \tau\nu$
- Case(ii)  $E < 300$  MeV where  $\tau^+\nu/\mu^+\nu$  is allowed to **float**
  - $153.9 \pm 13.5 \mu\nu$
  - $13.5 \pm 15.3 \tau\nu$



# Residual Backgrounds for $\mu\nu$

- Monte Carlo of Continuum,  $D^0$ , radiative return and other  $D^+$  modes, in  $\mu\nu$  signal region

Mode	# of events
Continuum	$0.8 \pm 0.4$
$\bar{K}^0 \pi^+$	$1.3 \pm 0.9$
$D^0$ modes	$0.3 \pm 0.3$
Sum	$2.4 \pm 1.0$

- This we subtract off the fitted yields

# Branching Fractions & $f_{D^+}$

- Fix  $\tau_{\nu}/\mu_{\nu}$  at SM ratio of 2.65
  - $\mathcal{B}(D^+ \rightarrow \mu^+ \nu) = (3.82 \pm 0.32 \pm 0.09) \times 10^{-4}$
  - $f_{D^+} = (205.8 \pm 8.5 \pm 2.5) \text{ MeV}$
  - This is best number in context of SM
- Float  $\tau_{\nu}/\mu_{\nu}$ 
  - $\mathcal{B}(D^+ \rightarrow \mu^+ \nu) = (3.93 \pm 0.35 \pm 0.09) \times 10^{-4}$
  - $f_{D^+} = (207.6 \pm 9.3 \pm 2.5) \text{ MeV}$
  - This is best number for use with Non-SM models
- The branching fractions have been reduced by 1% to count for radiative correction
- See arXiv:0806.2112v3, accepted by PRD

# CLEO Improved Measurement of $f_{D_s}$

- CLEO has two methods of measuring  $f_{D_s}$ 
  - Measure  $\mu^+\nu$  &  $\tau^+\nu$ ,  $\tau^+ \rightarrow \pi^+\nu$  using similar MM<sup>2</sup> technique used for  $D^+$ . Update result using new analysis & 30% more data ( $\sim 400 \text{ pb}^{-1}$ )
  - Measure  $\tau^+ \rightarrow e^+\nu\nu$  by using missing energy. This result has not been updated ( $\sim 300 \text{ pb}^{-1}$ ) **PRL 100, 161801 (2008)**

# Use $e^+e^- \rightarrow D_S D_S^*$ at 4170 MeV

- Reconstruct  $D_S^-$
- Find the  $\gamma$  from the  $D_S^*$  & compute  $MM^2$  from  $D_S^-$  &  $\gamma$

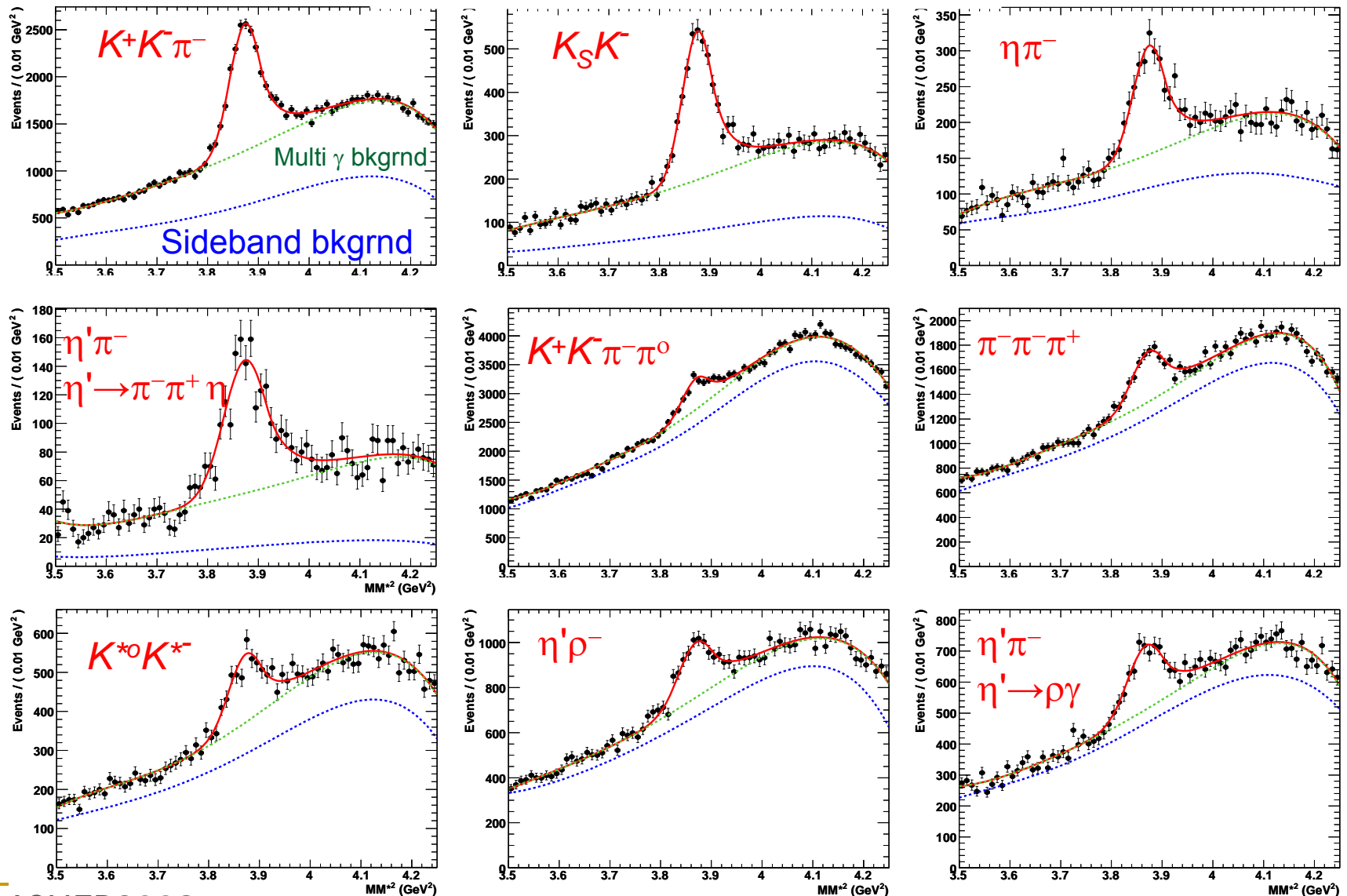
$$MM^{*2} = (E_{\text{CM}} - E_{D^-} - E_{\gamma})^2 - (-\vec{p}_{D^-} - \vec{p}_{\gamma})^2$$

- Select combinations consistent with a missing  $D_S^+$  & count the number
- Find  $MM^2$  from candidate muon for (i)  $< 300$  MeV in Ecal, (ii)  $E > 300$  MeV or (iii)  $e^-$  cand.

$$MM^2 = (E_{\text{CM}} - E_{D^-} - E_{\gamma} - E_{\mu})^2 - (-\vec{p}_{D^-} - \vec{p}_{\gamma} - \vec{p}_{\mu})^2$$

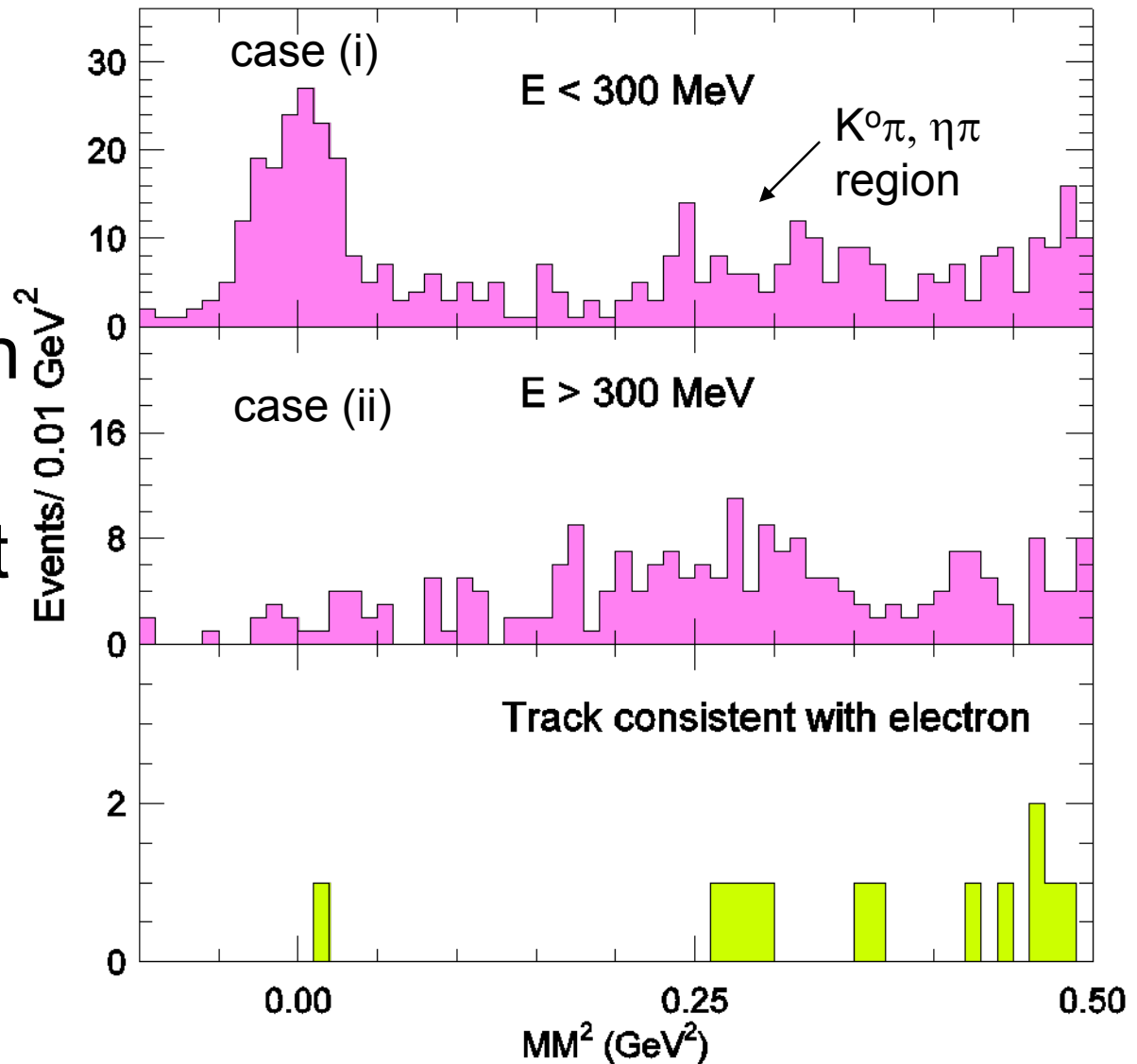
# MM<sup>\*2</sup> Distributions From D<sub>S</sub><sup>-</sup> + γ

in D<sub>S</sub><sup>-</sup> invariant mass signal region

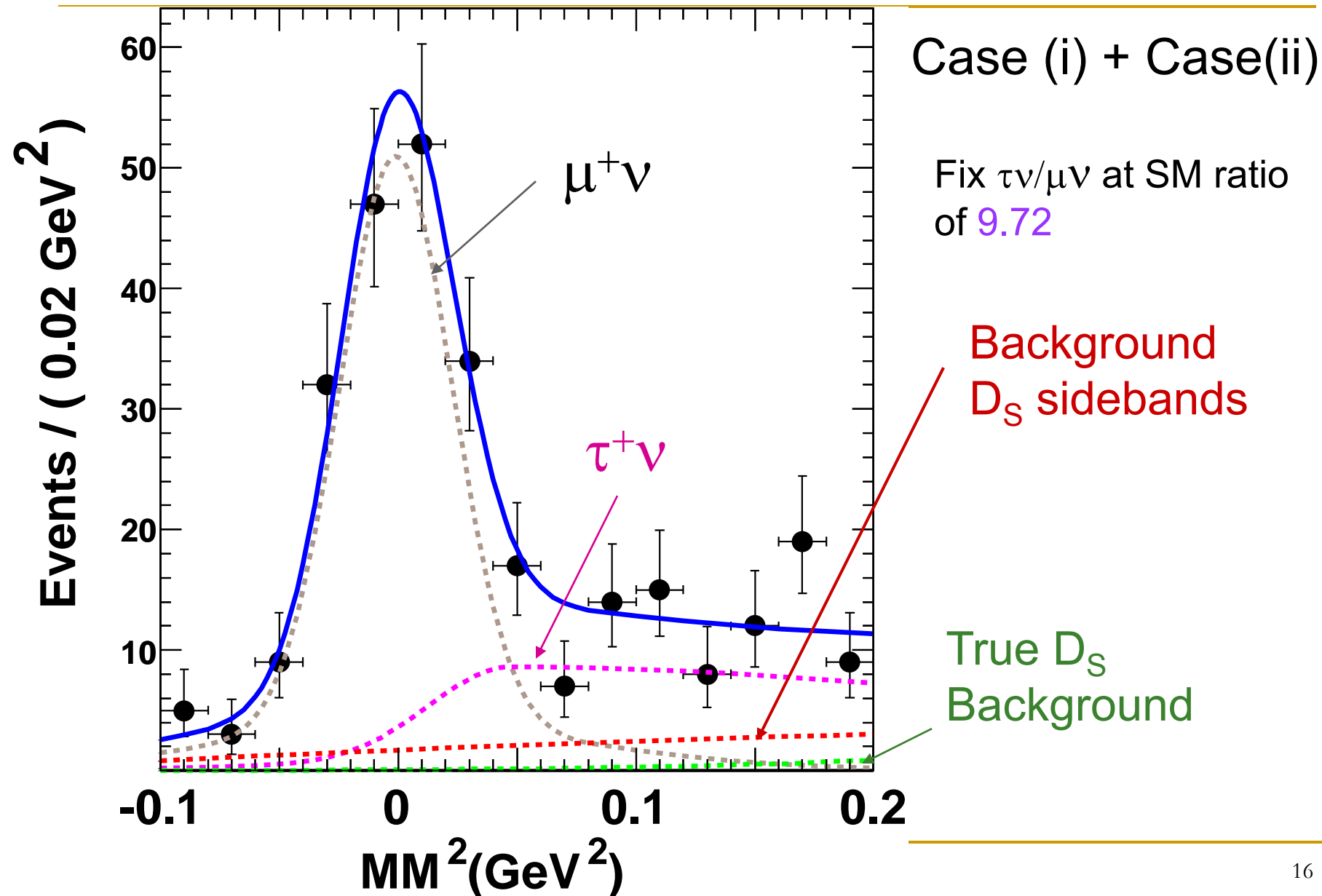


# MM<sup>2</sup> data for D<sub>S</sub>

- Total of 30848±695 tags
- ~99% of  $\mu^+\nu$  in  $E < 300$  MeV
- 55%/45% split of  $\tau^+\nu$ ,  $\tau^+ \rightarrow \pi^+\nu$  in two cases
- Small  $e^-$  background



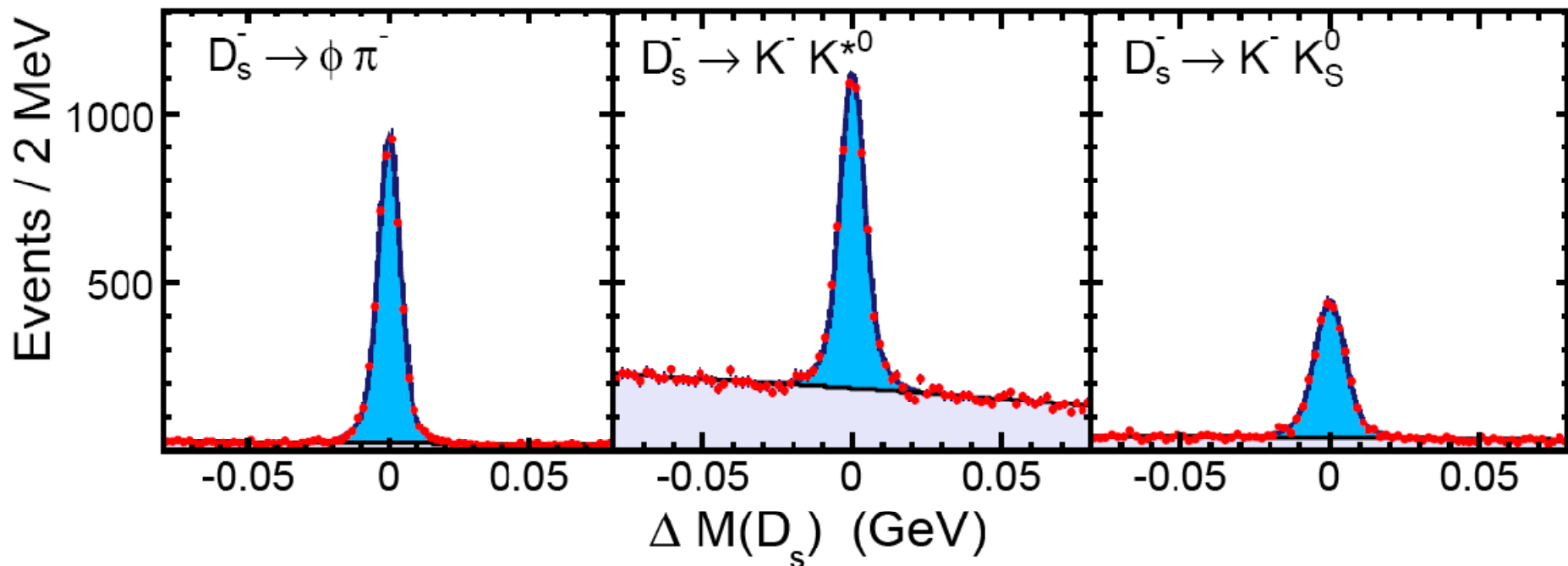
# Fit to signal & background





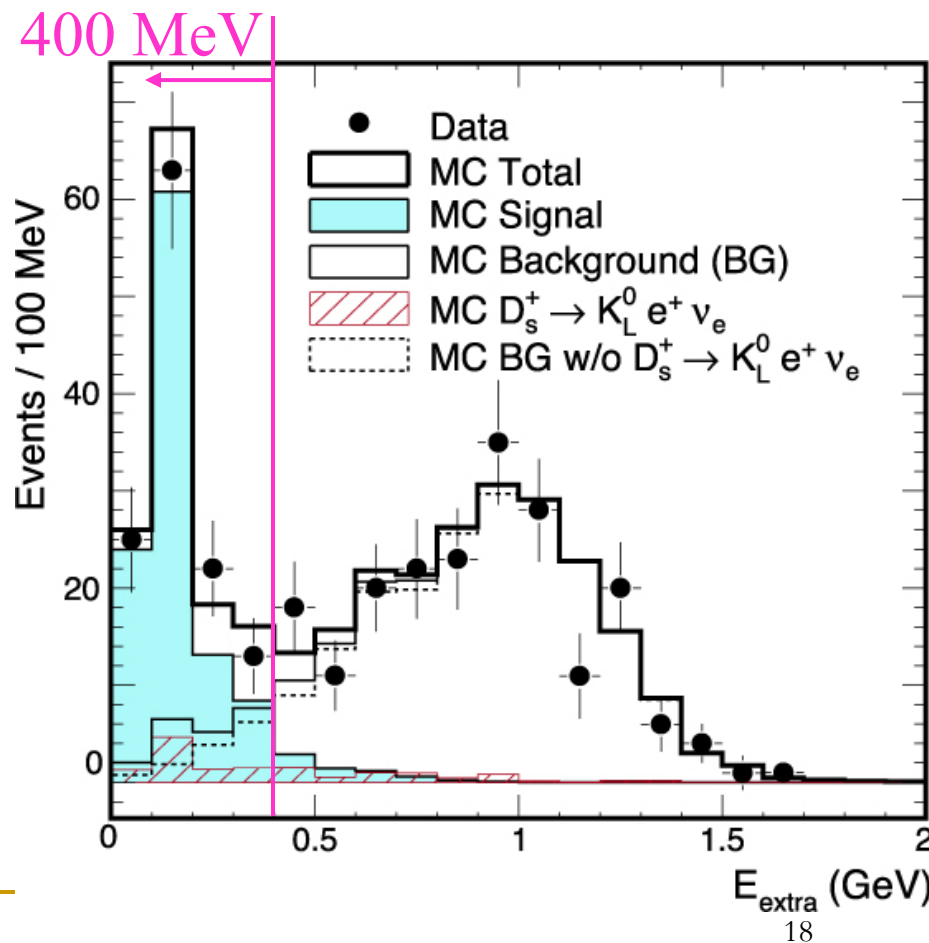
# CLEO: $D_S^+ \rightarrow \tau^+ \nu$ , $\tau^+ \rightarrow e^+ \nu \nu$

- $\mathcal{B}(D_S^+ \rightarrow \tau^+ \nu) \cdot \mathcal{B}(\tau^+ \rightarrow e^+ \nu \nu) \sim 1.3\%$  is “large” compared with expected  $\mathcal{B}(D_S^+ \rightarrow X e^+ \nu) \sim 8\%$
- We will be searching for events opposite a tag with one electron and not much other energy
- Opt to use only a subset of the cleanest tags



# Measuring $D_S^+ \rightarrow \tau^+ \nu$ , $\tau^+ \rightarrow e^+ \nu \nu$

- Technique is to find events with an  $e^+$  opposite  $D_S^-$  tags & no other tracks, with  $\Sigma$  calorimeter energy  $< 400$  MeV
- No need to find  $\gamma$  from  $D_S^*$
- $\mathcal{B}(D_S^+ \rightarrow \tau^+ \nu)$   
 $= (6.17 \pm 0.71 \pm 0.36)\%$
- $f_{D_S} = 273 \pm 16 \pm 8$  MeV

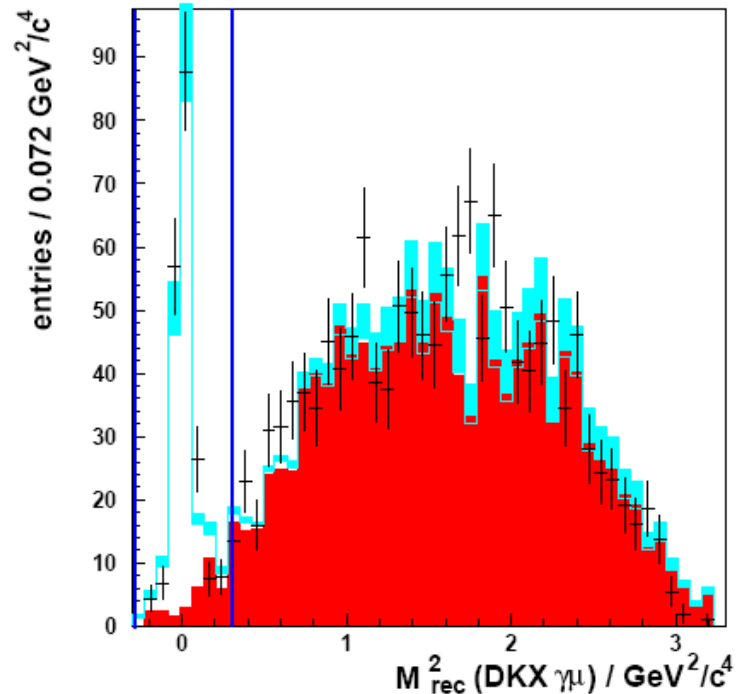
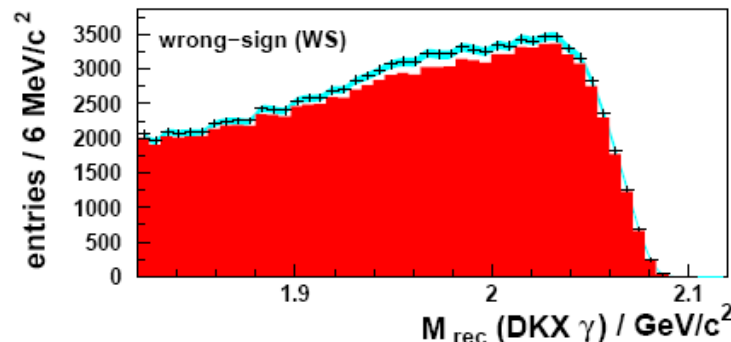
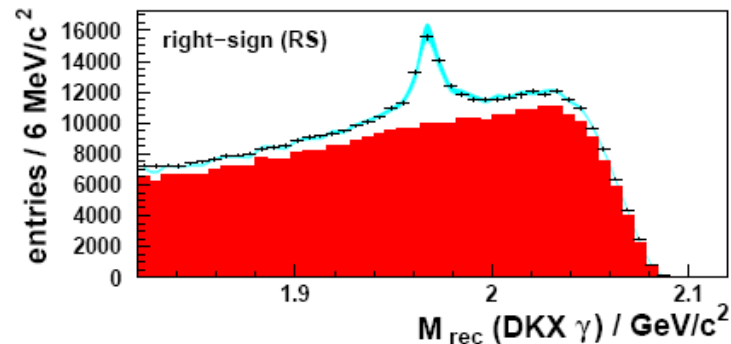


# Branching Ratio & $f_{D_s}$ (*preliminary*)

Mode	$\mathcal{B}$ (%)	$f_{D_s}$ (MeV)
(1) $\mu\nu + \tau\nu$ (fix SM ratio)	$\mathcal{B}^{\text{eff}}(D_s \rightarrow \mu\nu) =$ ( $0.613 \pm 0.044 \pm 0.020$ )	$268.2 \pm 9.6 \pm 4.4$
(2) $\mu\nu$ only	$\mathcal{B}(D_s \rightarrow \mu\nu) =$ ( $0.600 \pm 0.054 \pm 0.020$ )	$265.4 \pm 11.9 \pm 4.4$
(3) $\tau\nu, \tau \rightarrow \pi\nu$	$\mathcal{B}(D_s \rightarrow \tau\nu) =$ ( $6.1 \pm 0.9 \pm 0.2$ )	$271 \pm 20 \pm 4$
(4) $\tau\nu, \tau \rightarrow e\nu\nu$ PRL 100, 161801 (2008)	$\mathcal{B}(D_s \rightarrow \tau\nu) =$ ( $6.17 \pm 0.71 \pm 0.36$ )	$273 \pm 16 \pm 8$
CLEO Average of (1) & (4)	1% Rad. corr.	$269.4 \pm 8.2 \pm 3.9$
		$267.9 \pm 8.2 \pm 3.9$

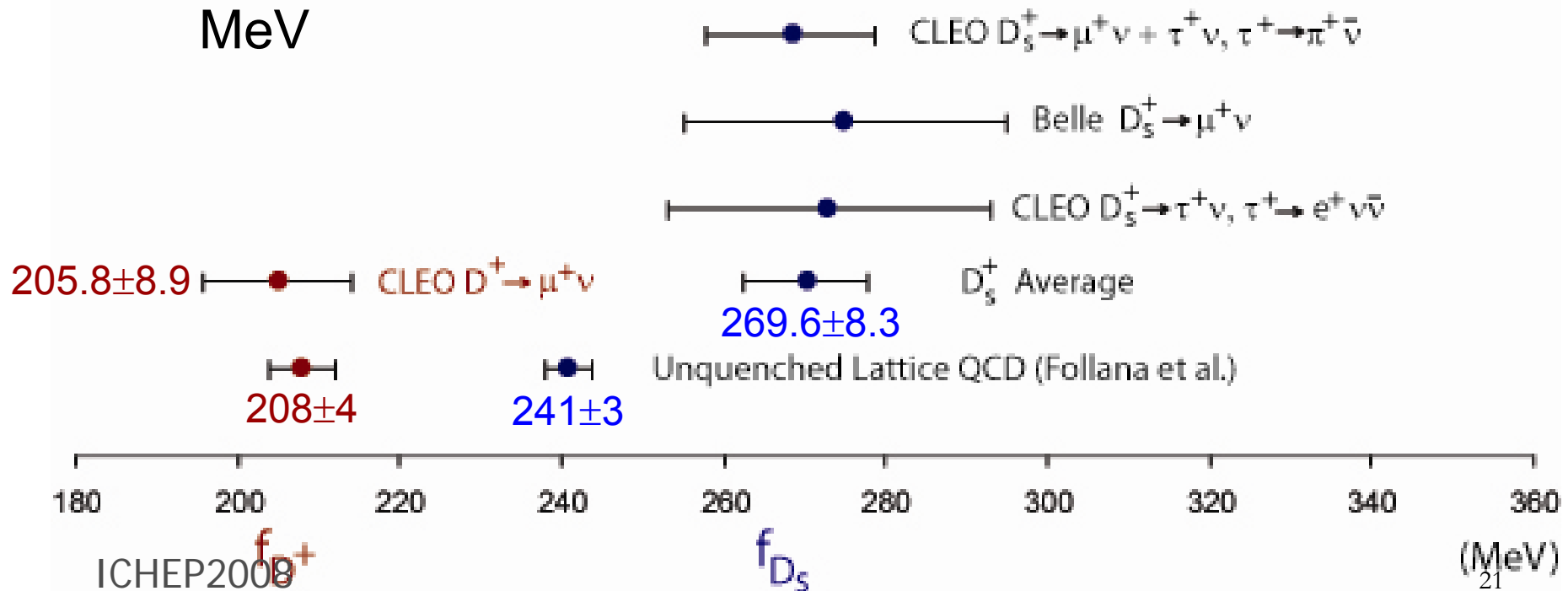
# Belle: $D_S^+ \rightarrow \mu^+ \nu$

- Look for  $e^+e^- \rightarrow DKX\gamma(D_S)$ , where  $X=n\pi$  & the  $D_S$  is not observed but inferred from calculating the MM
- Then add a candidate  $\mu^+$  and compute  $MM^2$
- $\mathcal{B}(D_S^+ \rightarrow \mu^+ \nu) = (0.644 \pm 0.076 \pm 0.057)\%$
- $f_{D_S} = 275 \pm 16 \pm 12 \text{ MeV}$   
arXiv:0709.1340v2 [hep-ex]



# Conclusions (I)

- We are in close agreement with the Follana et al calculation for  $f_{D^+}$ . This gives credence to their methods
- The disagreement on  $f_{D_s}$  is  $3.2 \sigma$ 
  - Weighted Average CLEO + Belle:  $f_{D_s} = 269.6 \pm 7.3 \pm 3.7$  MeV



# Conclusions (II)

## ■ Possibilities

- An unlikely statistical fluctuation in experiments
- Or systematic uncertainty that is not understood in the LQCD calculation
- Or NP

- Fits to the CKM matrix parameters use theoretical predictions of  $f_{B_s}/f_{B_d}$ . As similar calculations are used for  $f_{B_s}^*/f_{B_d}^*$ , we need to be concerned with them.

# Future Improvements

- CLEO will further update  $f_{D_s}$  using at total of  $\sim 600 \text{ pb}^{-1}$ 
  - 50% increase in data for  $\mu\nu$
  - 100% increase in data for  $\tau\nu, \tau \rightarrow e\nu\nu$
- $f_{D^+}$  will not see any major improvements until BES

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*The End*

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# New Physics Possibilities III

- Leptonic decay rate is modified by  $H^\pm$
- Can calculate in SUSY as function of  $m_q/m_c$ ,
- In 2HDM predicted decay width is x by

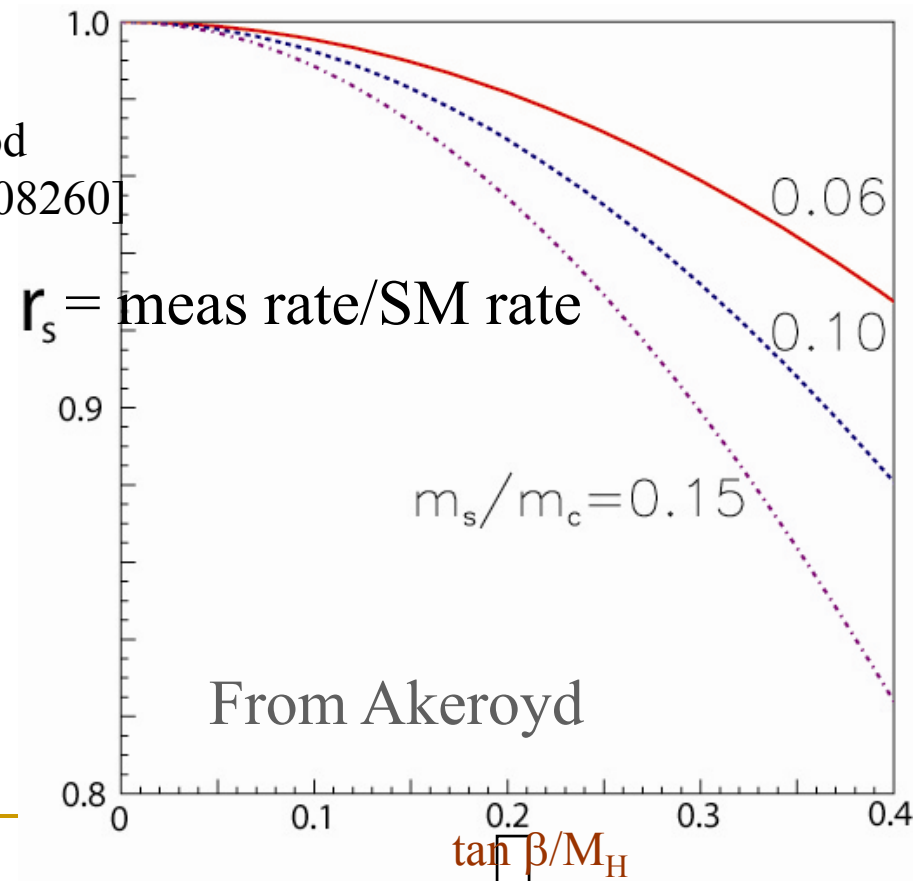
$$r_q = \left[ 1 - M_D^2 \left( \frac{\tan \beta}{M_{H^\pm}} \right)^2 \left( \frac{m_q}{m_c + m_q} \right) \right]^2$$

See Akeryod [hep-ph/0308260]

- Corrected

$$r_q = \left[ 1 + \left( \frac{M_D^2}{m_c + m_q} \right) \left( \frac{1}{M_{H^\pm}} \right)^2 (m_c - m_q \tan^2 \beta) \right]^2$$

- Since  $m_d$  is  $\sim 0$ , effect can be seen only in  $D_s$



# New Physics Possibilities

- Ratio of leptonic decays could be modified e.g. in Standard Model

$$\frac{\Gamma(P^+ \rightarrow \tau^+ \nu)}{\Gamma(P^+ \rightarrow \mu^+ \nu)} = m_\tau^2 \left(1 - \frac{m_\tau^2}{M_P^2}\right)^2 / m_\mu^2 \left(1 - \frac{m_\mu^2}{M_P^2}\right)^2$$

- If  $H^\pm$  couple proportional to  $M^2 \Rightarrow$  no effect

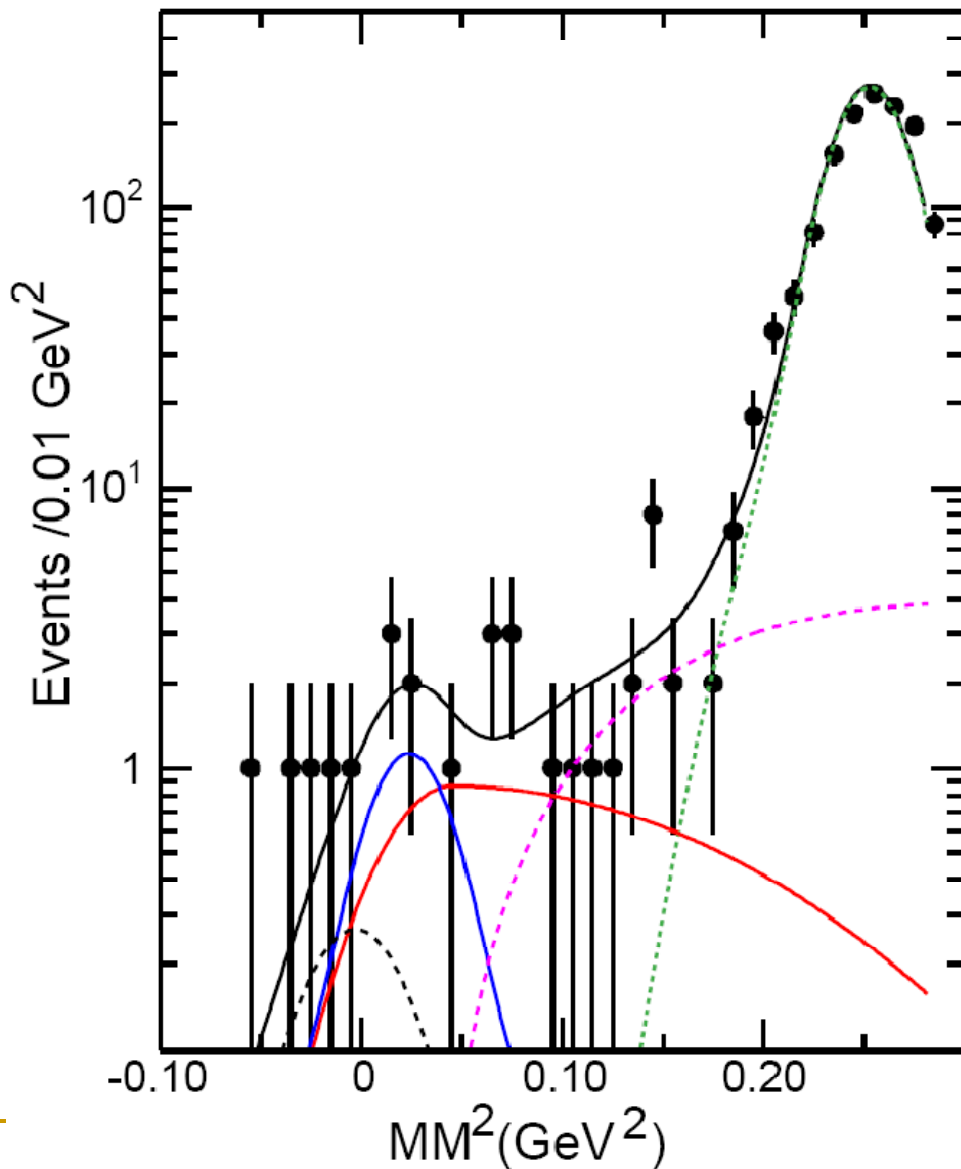
See Hewett [hep-ph/9505246] & Hou, PRD 48, 2342 (1993).

# Improvements in Analysis

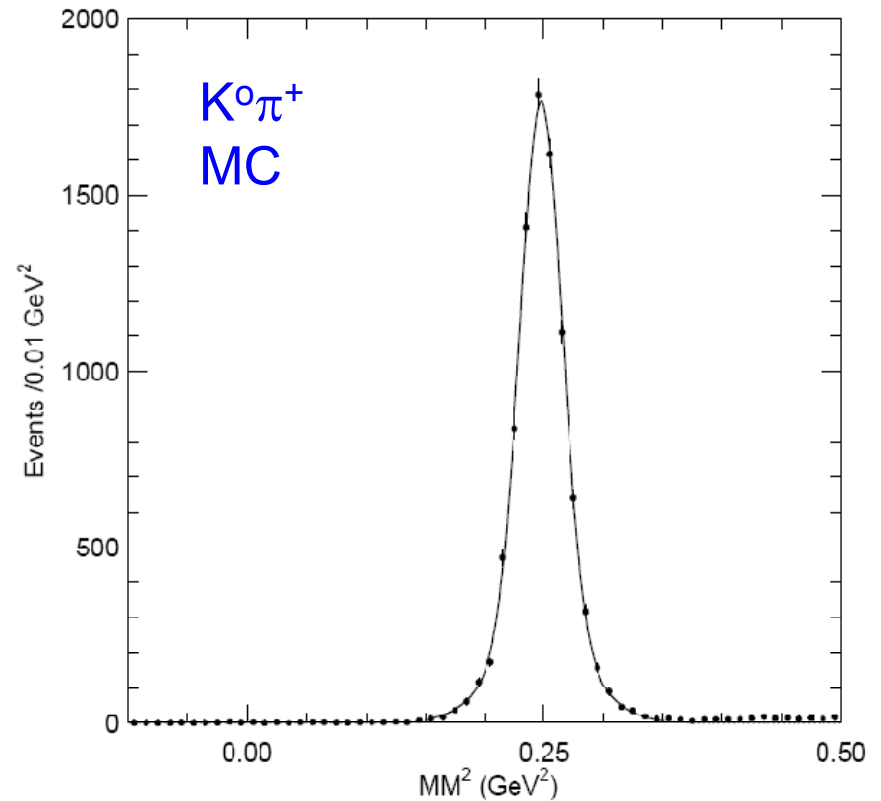
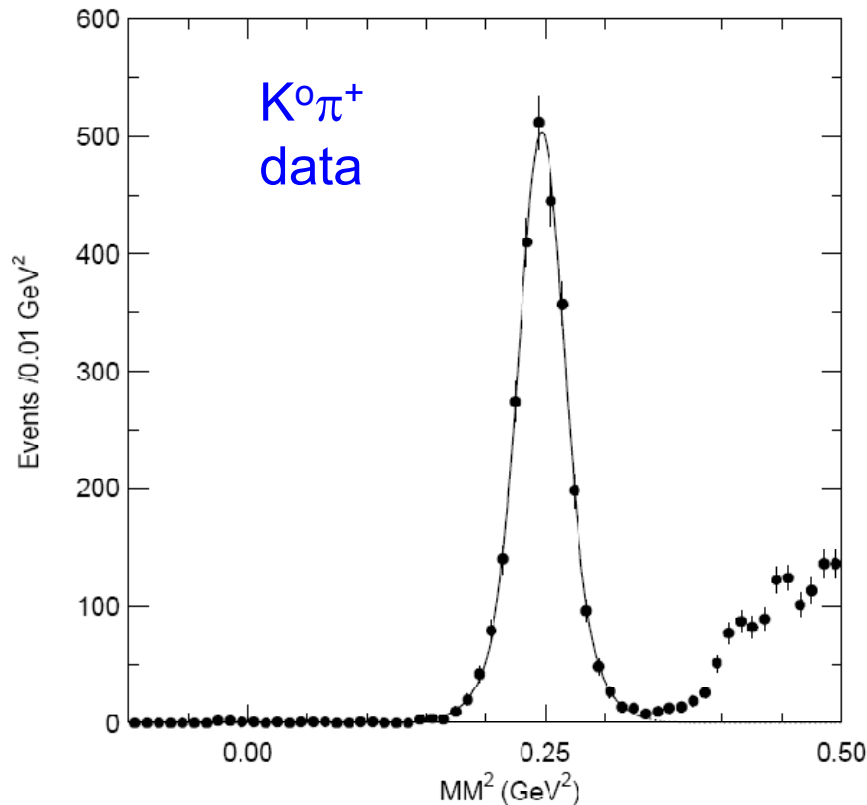
- Increase solid angle to  $|\cos\theta| < 0.9$  (+11%)
- Now we fit the muon candidate distribution to extract  $\mu^+\nu$  &  $\tau^+\nu$ , to extract yield, improves efficiency by  $\sim 5\%$ , & also allows us to quote a  $\mathbb{E}$  independent of assuming SM  $\tau^+\nu/\mu^+\nu$  ratio
  - Requires signal shapes for  $\mu^+\nu$  &  $\tau^+\nu$
  - Requires background shapes for  $K^0\pi^+$  low  $MM^2$  tail,  $\pi^+\pi^0$  & residual 3 body modes, e.g.  $\tau^+ \rightarrow \mu^+\nu\nu$ ,  $\rho^+\nu$ ,  $\pi^0\mu^+\nu$ .
  - Requires small residual background subtraction from continuum, etc...
- Backgrounds are now well understood especially from  $K^0\pi^+$  peak

# Background Check

- Use case(ii)  $E > 300$  MeV
- Fix  $\tau\nu$  from case(i)  $\mu\nu$ .
- Consider signal region  $|MM^2| < 0.05 \text{ GeV}^2$ .  
Expect  $1.7 \mu\nu + 5.4 \pi^+\pi^0 + 4.0 \tau\nu = 11.1$
- Find 11 events
- Extra bkgnd =  $-0.1 \pm 3.3$  events



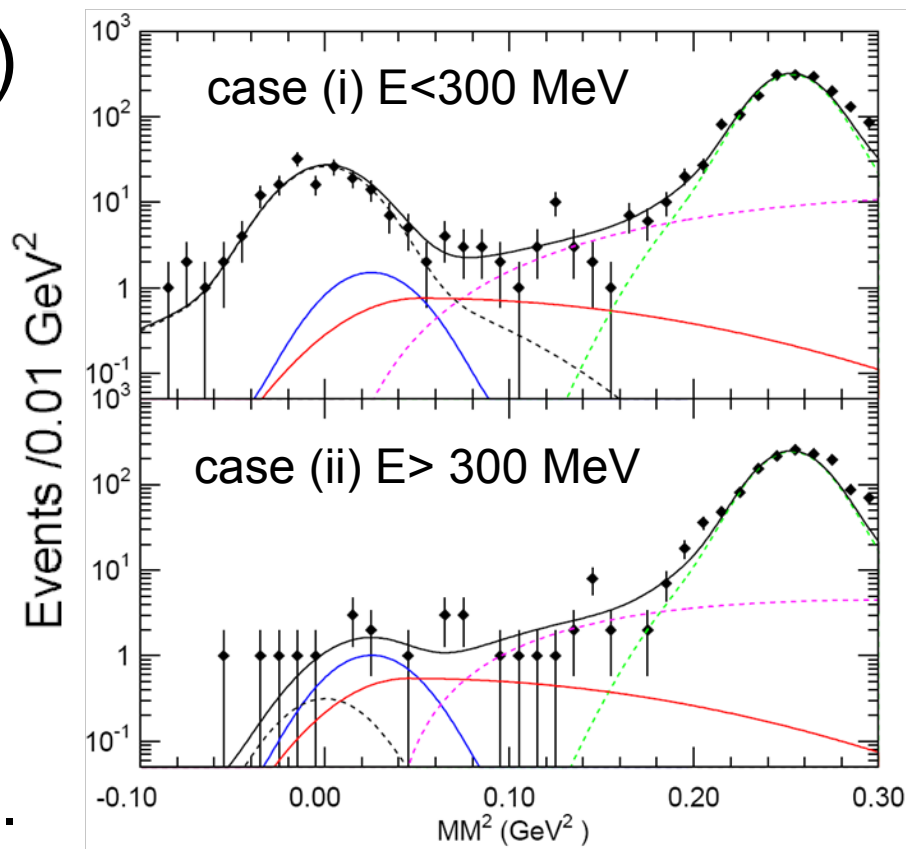
# $\mu\nu$ Signal Shape Checked



- Data  $\sigma=0.0247\pm 0.0012$  GeV<sup>2</sup>
- MC  $\sigma=0.0235\pm 0.0007$  GeV<sup>2</sup>
- Both average of double Gaussians

# Upper limits on $\tau\nu$ & $e\nu$

- Here we fit both case(i) & case(ii) constraining the relative  $\tau\nu$  yield to the pion acceptance, 55/45.
- Find
  - $\mathcal{B}(D^+ \rightarrow \tau^+ \nu)$   
<  $1.2 \times 10^{-3}$ , @ 90% c.l.
  - $\mathcal{B}(D^+ \rightarrow \tau^+ \nu) / 2.65 \mathcal{B}(D^+ \rightarrow \mu^+ \nu) < 1.2$  @ 90% c. l.
- Also  $\mathcal{B}(D^+ \rightarrow e^+ \nu) < 8.8 \times 10^{-6}$ , @ 90% c.l.



# CP Violation

- $D^+$  tags  $228,945 \pm 551$
- $D^-$  tags  $231,107 \pm 552$
- $\mu^- \nu$  events  $64.8 \pm 8.1$
- $\mu^+ \nu$  events  $76.0 \pm 8.6$

$$A_{CP} \equiv \frac{\Gamma(D^+ \rightarrow \mu^+ \nu) - \Gamma(D^- \rightarrow \mu^- \nu)}{\Gamma(D^+ \rightarrow \mu^+ \nu) + \Gamma(D^- \rightarrow \mu^- \nu)} = 0.08 \pm 0.08$$

- $-0.05 < A_{CP} < 0.21$  @ 90% c. l.

# Efficiencies

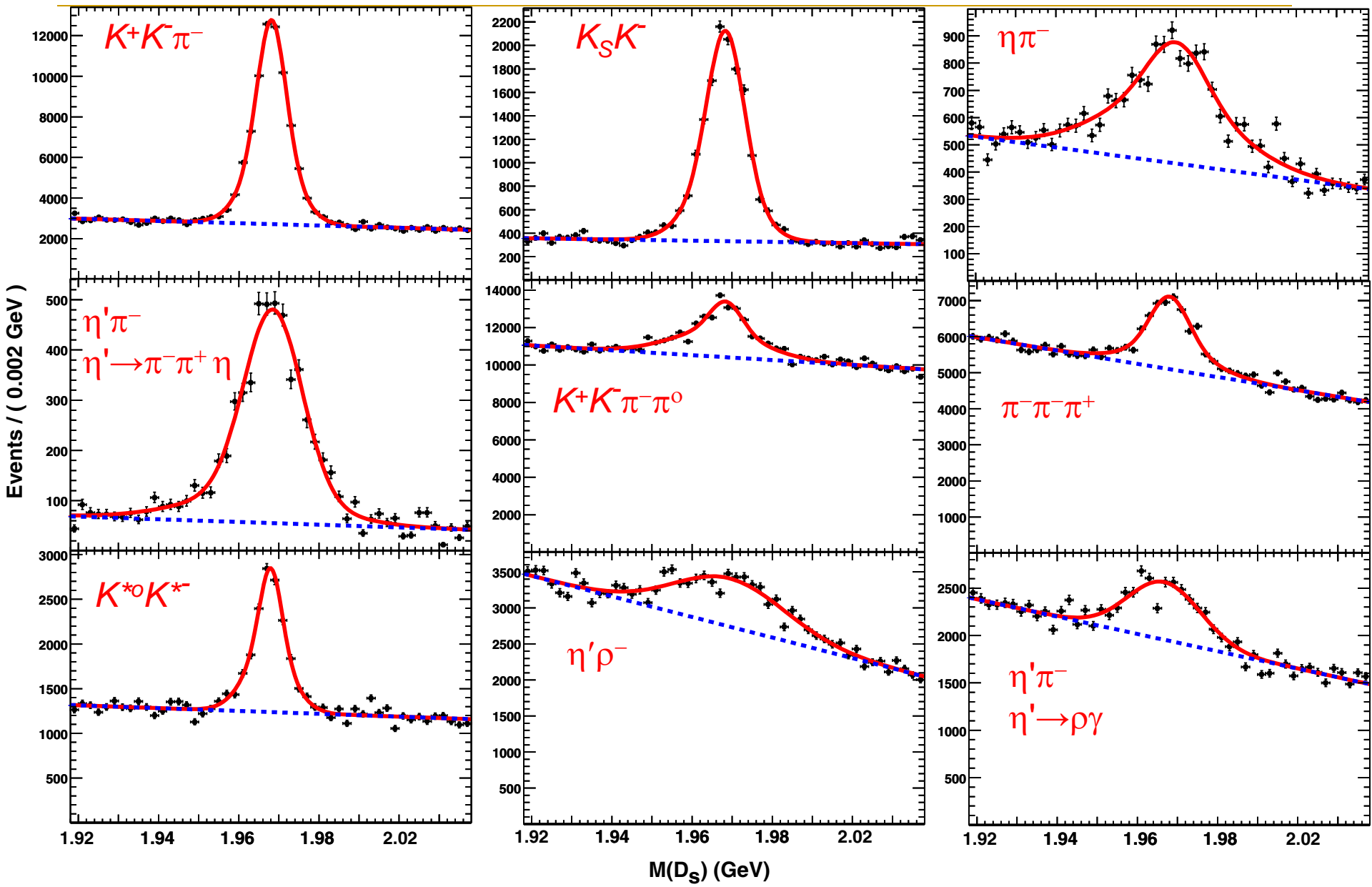
- Tracking, particle id,  $E < 300$  MeV (determined from  $\mu$ -pairs) = 85.3%
- Not having an unmatched shower  $> 250$  MeV 95.9%, determined from double tag, tag samples
- Easier to find a  $\mu\nu$  event in a tag than a generic decay (tag bias) (1.53%)



# Systematic Errors of $f_D$

Source of Error	%
Finding the $\mu^+$ track	0.7
Minimum ionization of $\mu^+$ in EM cal	1.0
Particle identification of $\mu^+$	1.0
MM <sup>2</sup> width	0.2
Extra showers in event > 250 MeV	0.4
Background	0.7
Number of single tag $D^+$	0.6
<b>Total</b>	<b>2.2</b>

# $D_s^-$ Tags: Invariant Mass

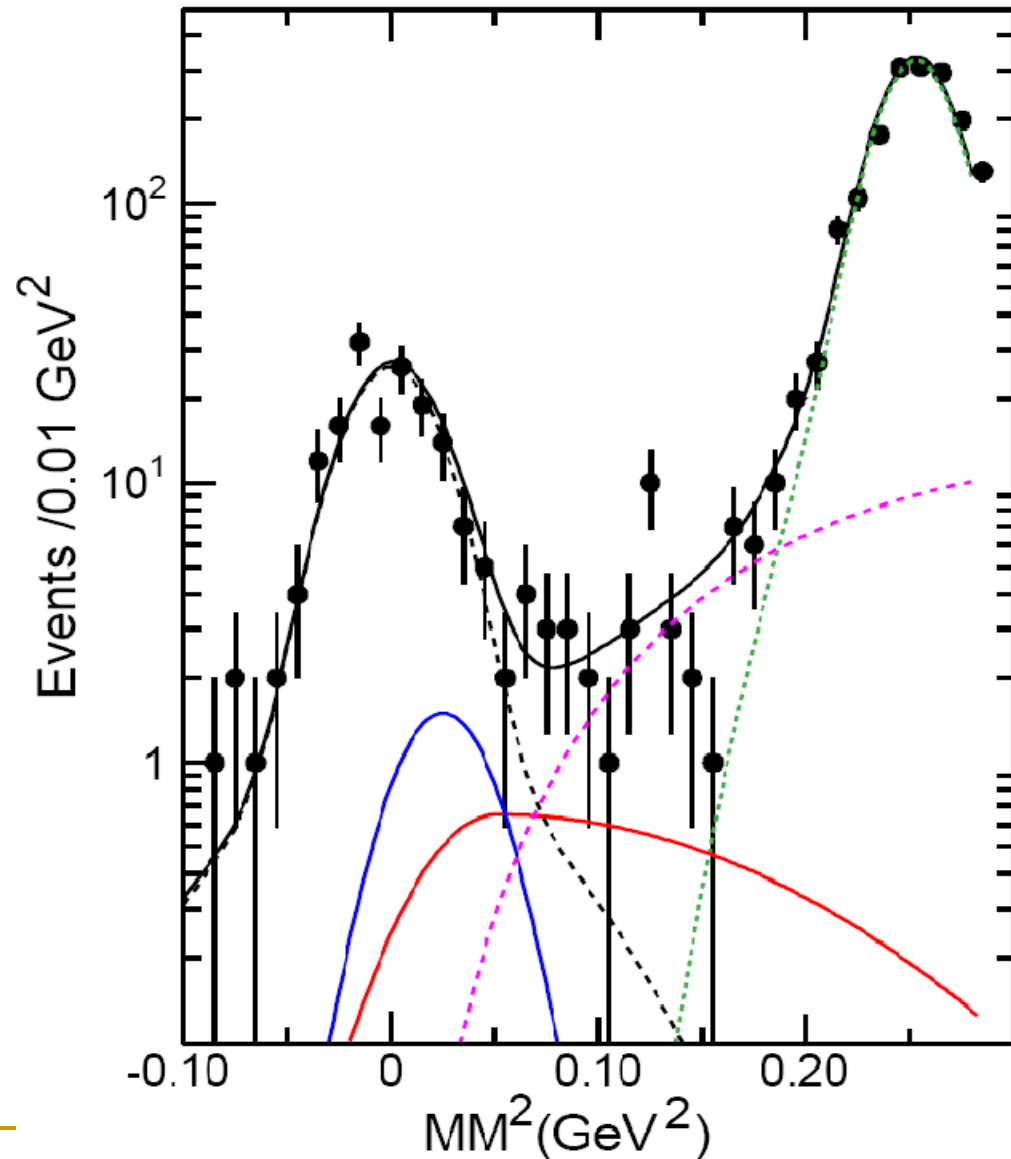


$$f_{D_s} \quad \& \quad f_{D_s} / f_{D^+}$$

- **Weighted Average CLEO + Belle:**  
 $f_{D_s} = 269.6 \pm 7.3 \pm 3.7$  MeV, the systematic error is uncorrelated between the measurements
  - **Using  $f_{D^+} = (205.8 \pm 8.5 \pm 2.5)$  MeV**
  - $f_{D_s} / f_{D^+} = 1.31 \pm 0.06 \pm 0.02$  Much larger than models
  - $\Gamma(D_s^+ \rightarrow \tau^+ \nu) / \Gamma(D_s^+ \rightarrow \mu^+ \nu) = 10.3 \pm 1.1$ ,  
SM=9.72
- Consistent with lepton universality

# Case(i) With $\tau^+\nu/\mu^+\nu$ Floating

- Fixed
  - $149.7 \pm 12.0 \mu\nu$
  - $28.5 \tau\nu$
- Floating
  - $153.9 \pm 13.5 \mu\nu$
  - $13.5 \pm 15.3 \tau\nu$



# Systematic Errors of $f_{D_S}$

Source of Error	%
Finding the $\mu^+$ track	0.7
Particle identification of $\mu^+$	1.0
MM <sup>2</sup> width	0.2
Extra showers in event > 300 MeV	0.4
Background	0.5
Number of single tag $D_S^-$	3.0
<b>Total</b>	<b>3.3</b>

# Other Non-absolute Measurements

Exp.	mode	$\mathcal{B}$	$\mathcal{B}(D_S \rightarrow \phi\pi)$ (%)	$f_{D_S}$ (MeV)
CLEO [11]	$\mu^+\nu$	$(6.2 \pm 0.8 \pm 1.3 \pm 1.6) \cdot 10^{-3}$	$3.6 \pm 0.9$	$273 \pm 19 \pm 27 \pm 33$
BEATRICE [12]	$\mu^+\nu$	$(8.3 \pm 2.3 \pm 0.6 \pm 2.1) \cdot 10^{-3}$	$3.6 \pm 0.9$	$312 \pm 43 \pm 12 \pm 39$
ALEPH [13]	$\mu^+\nu$	$(6.8 \pm 1.1 \pm 1.8) \cdot 10^{-3}$	$3.6 \pm 0.9$	$282 \pm 19 \pm 40$
ALEPH [13]	$\tau^+\nu$	$(5.8 \pm 0.8 \pm 1.8) \cdot 10^{-2}$		
L3 [14]	$\tau^+\nu$	$(7.4 \pm 2.8 \pm 1.6 \pm 1.8) \cdot 10^{-2}$		$299 \pm 57 \pm 32 \pm 37$
OPAL [15]	$\tau^+\nu$	$(7.0 \pm 2.1 \pm 2.0) \cdot 10^{-2}$		$283 \pm 44 \pm 41$
BaBar [16]	$\mu^+\nu$	$(6.74 \pm 0.83 \pm 0.26 \pm 0.66) \cdot 10^{-3}$	$4.71 \pm 0.46$	$283 \pm 17 \pm 7 \pm 14$

See arXiv:0802.1043 for references

# Questions

- Pick your favorite of the two:
  - If theoretical predictions of  $f_{D_S}/f_{D^+}$  do not agree with the data, why should we believe  $f_{B_S}/f_B$  from theory? What does this do to the CKM fits?
  - If there is New Physics affecting leptonic  $D_S$  decays, how does it affect  $B_S$  mixing and other  $B_S$  decays? (See A. Kundu & S. Nandi, “R-parity violating supersymmetry,  $B_S$  mixing, &  $D_S^+ \rightarrow \ell^+ \nu$ ” [arXiv:0803.1898])

# Radiative Correction

- FSR of the muon has been corrected in the MC simulation.
- However, another process where the  $D^+ \rightarrow \gamma D^{*+} \rightarrow \gamma \mu^+ \nu$ , where the  $D^{*+}$  is a virtual vector or axial-vector meson.