# Recent Results in Bottomonium Ties to Charmonium 

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## Bottom compared to Charm

Heavy quark symmetry

$$
\begin{gathered}
\mathrm{m}_{\mathrm{b}} / \mathrm{m}_{\mathrm{c}}=5 \mathrm{GeV} / 1.7 \mathrm{GeV} \approx 3 \\
\left|\mathrm{q}_{\mathrm{b}} / \mathrm{q}_{\mathrm{c}}\right|=\mathrm{e} / 3 / 2 \mathrm{e} / 3=1 / 2 \\
\mathrm{r}_{\mathrm{b}} / \mathrm{r}_{\mathrm{c}} \approx 0.3 \mathrm{fm} / 0.5 \mathrm{fm}=0.6 \\
\beta_{\mathrm{b}}^{2} / \beta_{\mathrm{c}}^{2} \approx \mathrm{~m}_{\mathrm{c}} / \mathrm{m}_{\mathrm{b}} \approx 1 / 3 \\
\alpha_{\mathrm{s}, \mathrm{~b}} / \alpha_{\mathrm{s}, \mathrm{c}} \approx 0.2 / 0.3=2 / 3
\end{gathered}
$$

Cornell potential $\sim(a / r)+b r$
Some implications ... b-bbar will differ in a calculable way ...
More Coulomb-like, less able to probe confinement region, more asymptotically free, more states below threshold, more non-relativistic, smaller M1 rates, higher decay multiplicities, less copiously produced in $\mathrm{e}^{+} \mathrm{e}^{-}$

Bottomonium a different laboratory to study the same physics

## Charmonium and Bottomonium



## Players of Note

- Direct production in $\mathbf{e}^{+} \mathbf{e}^{-:}$
- CLEO: 6 M r(3S), $9 \mathrm{M} \Upsilon(2 S)$, $21 \mathrm{M} \mathrm{r(1S)}$
- Belle: $11 \mathrm{M} \mathrm{r(3S)} \mathrm{(in} \mathrm{a} \mathrm{few} \mathrm{days'} \mathrm{run!)}$
- Belle and BaBar: 100's of M r(4S)
- ISR Production:

- Belle and BaBar: 10's of M r(1S), r(2S), r(3S)
- Belle and BaBar: 10 's of M $\Upsilon(\mathbf{1 S}), r(2)$

- Hadro-production:
- CDF $\}$ Production Ratios
- D0 $\}$ \{ Polarizations



## Polarization in Production

$\mathbf{p} \bar{p}$ production of onia can be modeled with NRQCD
Uses "universal" matrix elements with color-octet pieces, which describe production cross sections adequately
Polarization parametrized by $\alpha=\left(\sigma_{T}-2 \sigma_{\mathrm{L}}\right) /\left(\sigma_{\mathrm{T}}+2 \sigma_{\mathrm{L}}\right)$
Measured by angular distribution in di-lepton (dimuon) decays: dN/d $\cos \theta^{*} \sim\left(1+\alpha \cos ^{2} \theta^{*}\right)$
NRQCD predicts a large transverse polarization at high $\mathrm{p}_{\mathrm{T}}$ gluon fragmentation becomes dominant mechanism
$\alpha$ should approach unity at high $p_{T}$
$\mathbf{k}_{\mathrm{T}}$-factorization ("semi-hard") makes opposite prediction
large longitudinal polarizations at high $p_{T}$
$\alpha$ becomes negative at large $p_{T}$
Neither formulation works well in charmonium
New results in bottomonium from D0 with 1.3/fb, ~420K rs

## Polarization in Production



Neither phenomenology describes $\overline{\mathrm{c}}$ well

D0 observes significant polarization in $\Upsilon(1 S)$ production, inconsistent with NRQCD
$r(2 S)$ is "not inconsistent" with NRQCD
Bottomonium only deepens the puzzle for polarization in onium production


[^0]
## Dipion Transition Matrix Element



## Dipion Transition Matrix Element

Brown and Cahn [PRL 35, 1 (1975)] use PCAC and current algebra:

$$
M=A\left(\varepsilon^{\prime} \cdot \varepsilon\right)\left(q^{2}-2 m_{\pi}^{2}\right)+B\left(\varepsilon^{\prime} \cdot \varepsilon\right) E_{1} E_{2}+C\left[\left(\varepsilon^{\prime} \cdot q_{1}\right)\left(\varepsilon \cdot q_{2}\right)+\left(\varepsilon^{\prime} \cdot q_{2}\right)\left(\varepsilon \cdot q_{1}\right)\right]
$$

- CLEO fits 2-D "Dalitz" plot $\left(q^{2}=M_{\pi \pi}{ }^{2} \& M_{r \pi}{ }^{2}\right)$, for the three di-pion transitions among the $\Upsilon(n S)$ states [hep-ex/0706.2317]
- Only the two terms, with complex, constant form factor coefficients

A and B, are needed to give good fits to the data

| Initial $\Upsilon$ | Final $\Upsilon$ | $\operatorname{Re}(\mathrm{B} / \mathrm{A})$ | Im (B/A) |
| :---: | :---: | :---: | :---: |
| 3S | 1S | $-2.52 \pm 0.04$ | $\pm 1.19 \pm 0.06$ |
| 2 S | 1S | $-0.75 \pm 0.15$ | $0.00 \pm 0.11$ |
| 3S | 2 S | $-0.40 \pm 0.32$ | $0.00 \pm 1.10$ |
| Includes system. uncert's |  | $\|\mathrm{C} / \mathrm{A}\|_{\text {3to1 }} \times 1.09$ @ 90\% CL |  |

Dubynskiy/Voloshin [hep-ph/0707.1272] argue that CLEO parametrization is too naïve, $B$ cannot be constant over the Dalitz plot

Good to revisit with Belle $(Q=b)$ and CLEOc/BES $(Q=c)$ data!

## Pseudo-scalar Transitions

In charmonium $\psi(2 \mathrm{~S}) \rightarrow \eta \mathrm{J} / \psi$ is (surprisingly) large $\sim 3 \%$
Kuang [hep-ph10601044 v2] scales $\Gamma \sim\left(\mathrm{p}^{*}\right)^{3} / \mathrm{m}_{Q}{ }^{4}$ to predict

$\gamma \boldsymbol{K}$ Kinetic energy, MeV $\rightarrow$

$B(r(2 S) \rightarrow \eta r(1 S))=(8.1 \pm 0.8) \times 10^{-4}$
$B(\Upsilon(3 S) \rightarrow \eta r(1 S))=(6.7 \pm 0.7) \times 10^{-4}$

CLEO seeks $\mathrm{r}(2 \mathrm{~S}) \rightarrow \eta \mathrm{r}(1 \mathrm{~S})$ with $r(1 S) \rightarrow \mu \mu$ or ee, and $\eta \rightarrow \gamma$ or $\pi^{+} \pi \pi^{0}$
Sees preliminary $\sim 5 \sigma$ evidence
$B(\Upsilon(2 S) \rightarrow \eta r(1 S))=(2.5 \pm 0.7 \pm 0.5) \times 10^{-4}$

Also seek $\pi^{0}$, find no excess over background $\mathrm{B}\left(\mathrm{Y}(2 \mathrm{~S}) \rightarrow \pi^{0} \mathrm{Y}(1 \mathrm{~S})\right)<2.1 \times 10^{-4}$ consistent with expected ratio to $\eta$ (.16)
Also 3 events in $\eta \rightarrow \pi^{+} \pi^{-} \pi^{0}$ mode

## 〔 Decays to Invisible Particles

Onia decays to undetectable particles are a window on physics beyond the Standard Model (BSM):

- Dark matter candidate, $\chi$ ?

$$
B(\Upsilon(\mathbf{1 S}) \rightarrow \chi \chi)=0.41 \% \text { McElrath [PRD72, } 103508 \text { (2005)] }
$$

- New gauge bosons? Light gravitino? Fayet [PRD74, 054034 (2006)]
- vv via $Z^{0}$ a very small potential background

But how does one "see" such invisible decays?
Tag presence of $\Upsilon$ via $\pi \pi$ transition from higher state!
Require recoil against $\pi \pi$ be $\Upsilon$
Require detector otherwise empty


## 〔 Decays to Invisible Particles



## 〔 Decays to Invisible Particles

## 90\%CL limits:

$$
\begin{aligned}
& \mathrm{B}(\mathrm{Y} \rightarrow \text { "invisible" })_{\text {Belle }}<0.25 \% \\
& \mathrm{~B}(\mathrm{Y} \rightarrow \text { "invisible" })_{\text {cLEO }}<0.39 \%
\end{aligned}
$$



Each limit is an order of magnitude better than previous best
Combined limit about half $\chi \chi$ prediction of $0.41 \%$
Betters gravitino mass limit by $\times 4$ to $\mathrm{m}_{3 / 2}>1.2 \times 10^{-7} \mathrm{eV}$
Such BSM decays also accessible in charmonium! More limited mass range
Smaller predicted branching fraction
See R. McElrath's talk next in this session!

## Radiative Decays to Higgs?

Dermisek, Gunion, McElrath propose adding to the MSSM a non-SM-like pseudoscalar higgs $\mathrm{a}_{0}$ with $\mathrm{m}_{\mathrm{a} 0}<2 \mathrm{~m}_{\mathrm{b}}$ [hep-ph/0612031] "NMSSM" "natural," avoids fine tuning
evades the LEP limit $M_{h}>100 \mathrm{GeV}$ since $h \rightarrow a_{0} a_{0}$, but $a_{0} \nrightarrow b b$ and LEP sought $b$ jets $a_{0} \rightarrow \tau^{+} \tau$ should predominate if $m_{a 0}>2 m_{\tau}$
Should be visible in $\Upsilon \rightarrow \gamma a_{0}$
Experimentally, CLEO seeks monochromatic $\gamma$
Use $\mathrm{r}(2 \mathrm{~S}) \rightarrow \pi \pi \mathrm{r}(1 \mathrm{~S})$ tag to eliminate $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \tau \tau \gamma$ background
Flag presence of $\tau$ pair with two 1 -prong $\tau$ decays (one lepton), missing energy



ULs improved an order of magnitude or more

Rules out many, but not all NMSSM models

## Other Radiative Decays

Among the most common radiative decays in $\mathrm{J} / \psi$ is $\gamma \mathrm{f}_{2}(1270)$.
Unlike in the J/ $\psi$ system, few exclusive radiative decays of the $r$ are known, but CLEO has now found this decay for $r$ in two modes.


## Radiative Decays to f's

For $\Upsilon \rightarrow \gamma \mathrm{f}_{\mathbf{2}}(\mathbf{1 2 7 0})$ simple scaling from charmonium works:
Expect $\mathrm{B}\left(\psi \rightarrow \gamma \mathrm{f}_{2}\right) / \mathrm{B}\left(\mathrm{r} \rightarrow \gamma \mathrm{f}_{2}\right)=\left(\mathrm{a}_{\mathrm{c}} / \mathrm{q}_{\mathrm{b}}\right)^{2}\left(\mathrm{~m}_{\mathrm{b}} / \mathrm{m}_{\mathrm{c}}\right)^{2}\left(\Gamma_{\mathrm{bb}} / \Gamma_{\mathrm{cc}}\right) \approx 20$ Observe

$$
\begin{aligned}
& \mathrm{B}\left(\mathrm{r} \rightarrow \gamma \mathrm{f}_{2}(1270)\right)=(10.2 \pm 0.8 \pm 0.7) \times 10^{-5} \quad\left(\pi^{+} \pi^{-}\right) \text {PRD73, (232001(2006) } \\
& \mathrm{B}\left(\mathrm{r} \rightarrow \gamma \mathrm{f}_{2}(1270)\right)=(10.5 \pm 1.6 \pm 1.9) \times 10^{-5}\left(\pi^{0} \pi^{0}\right) \text { PRR75, 072001 (2007) } \\
& \mathrm{B}\left(\Upsilon \rightarrow \gamma \mathrm{f}_{2}(1270)\right)=(10.23 \pm 0.97) \times 10^{-5} \quad(\text { combined }) \\
& \mathrm{B}\left(\psi \rightarrow \gamma \mathrm{f}_{2}\right) / \mathrm{B}\left(\Upsilon \rightarrow \gamma \mathrm{f}_{2}\right)=14.0 \pm 1.7
\end{aligned}
$$

Dominant helicity $=0$, as expected from theory

## Radiative Decays to $\eta, \eta^{\prime}$

Another prominent radiative decay is $\mathrm{J} / \psi \rightarrow \eta^{\prime}$ :

$$
\begin{aligned}
& \mathrm{B}\left(\mathrm{~J} / \psi \rightarrow \gamma \eta^{\prime}\right)=(4.7 \pm 0.3) \times 10^{-3} \\
& \mathrm{~B}\left(\mathrm{~J} / \psi \rightarrow \gamma \eta^{\prime}\right) / \mathrm{B}\left(\mathrm{~J} / \psi \rightarrow \gamma \mathrm{f}_{2}\right)=3.4 \pm 0.4 \\
& \mathrm{~B}\left(\mathrm{~J} / \psi \rightarrow \gamma \eta^{\prime}\right)\left[\mathrm{B}\left(\Upsilon \rightarrow \gamma \mathrm{f}_{2}\right) / \mathrm{B}\left(\mathrm{~J} / \psi \rightarrow \gamma \mathrm{f}_{2}\right)\right]=(3.5 \pm 0.5) \times 10^{-4}
\end{aligned}
$$


naïve scaling
$\mathrm{B}(\mathrm{J} / \psi \rightarrow \gamma \eta)\left[\mathrm{B}\left(\Upsilon \rightarrow \gamma \mathrm{f}_{2}\right) / \mathrm{B}\left(\mathrm{J} / \psi \rightarrow \gamma \mathrm{f}_{2}\right)\right]=(0.7 \pm 0.1) \times 10^{-4}$
But we know the $\eta^{\prime}$ to be rather unconventional

- Anomalous 5x larger branching ratio compared to $\eta$
- 14\% gluonic content? - KLOE [PLB648 267 (2007)]
- Possible charmonium content?

Theoretical approaches include:

- VDM - Intemann [PRD 272755 (1983)]
- Mixing with $\eta_{b}$ - Chao [Nucl Phys B335 101 (1990)]
- Higher twist contribution - Ma [PRD65 097506 (2002)]


## Radiative Decays to $\eta, \eta^{\prime}$

## New 90\% CL limits from CLEO



Use 21 M r decays to get:
Naïve
scaling

$$
\begin{array}{ll}
\mathrm{B}\left(\mathrm{r} \rightarrow \eta^{\prime}\right)<1.9 \times 10^{-6} & 350 \times 10^{-6} \\
\mathrm{~B}(\mathrm{r} \rightarrow \gamma)<1.0 \times 10^{-6} & 70 \times 10^{-6}
\end{array}
$$

Significant improvement in limits
Naïve scaling fails by 2 orders of magnitude

Chao's mixing approach not supported for $\eta^{\prime}$ (factor of 30 )
Intemann's VDM predictions $\sim 10^{-7}$
Ma's predictions a bit below these limits

## Summary

Bottomonium is a useful complement to charmonium in studying QCD in production, spectroscopy and decay

New results in polarization of $\Upsilon$ in $\overline{\mathrm{pp}}$ production are not well described by NRQCD or $\mathrm{k}_{\mathrm{T}}$-factorization
A 2D fitting technique for $\mathrm{r}(\mathrm{nS}) \rightarrow \pi \pi(\mathrm{mS})$ transitions may help clarify a longstanding puzzle
The pseudoscalar hadronic transition $\mathrm{r}(2 \mathrm{~S}) \rightarrow \eta \mathrm{r}(1 \mathrm{~S})$ has finally been seen, about $1 / 3$ as large as scaling from charm predicts
Searches for decays of $\Upsilon(1 S)$ to invisibles have upper limits smaller than the predictions of $\chi \chi$ or gravitino
A search for low mass pseudoscalar higgs $a_{0}$ sees none
The radiative decay $\gamma(1 S) \rightarrow \gamma f_{2}(1270)$ has been seen at about the strength predicted from charmonium, but $\mathrm{r}(1 \mathrm{~S}) \rightarrow \eta \eta^{\prime}$ upper limit is two orders of magnitude smaller than naïve scaling from $\mathrm{J} / \psi$ decay


## Backup Slides




[^0]:    CDF PRL88,161802(2002)

