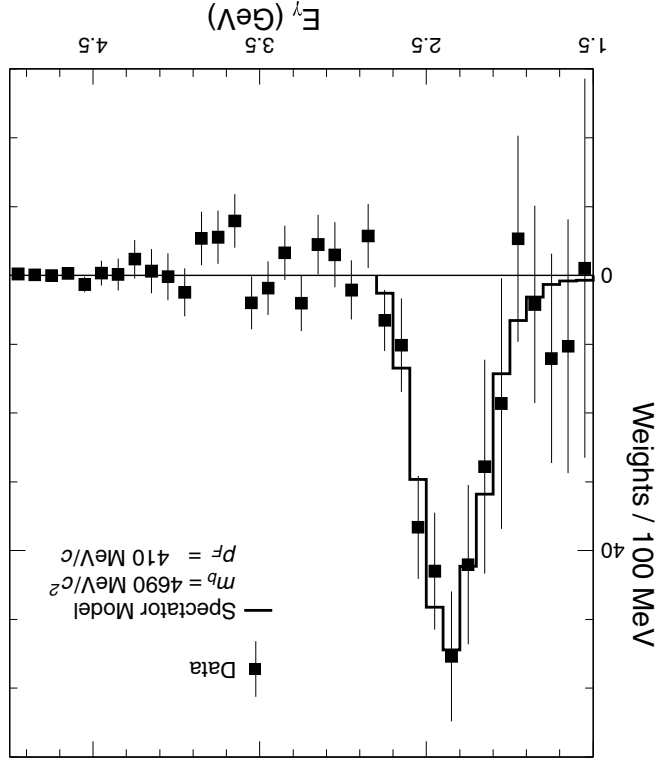
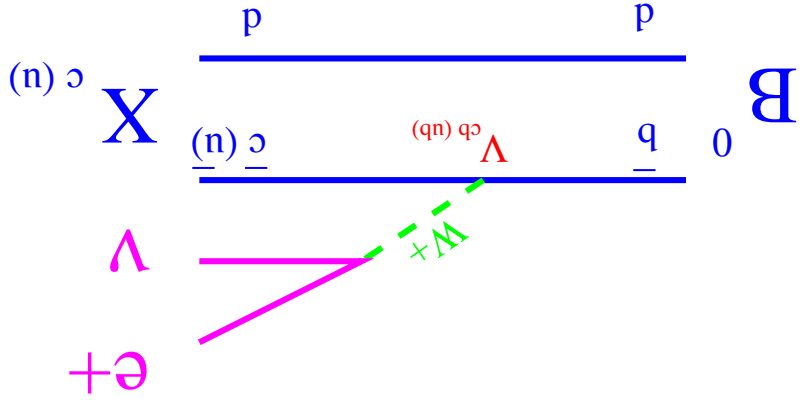


**CKM Physics from CLEO: $|V^{cb}|$, $|V^{ub}|$
and how $b \rightarrow s\gamma$ helps**

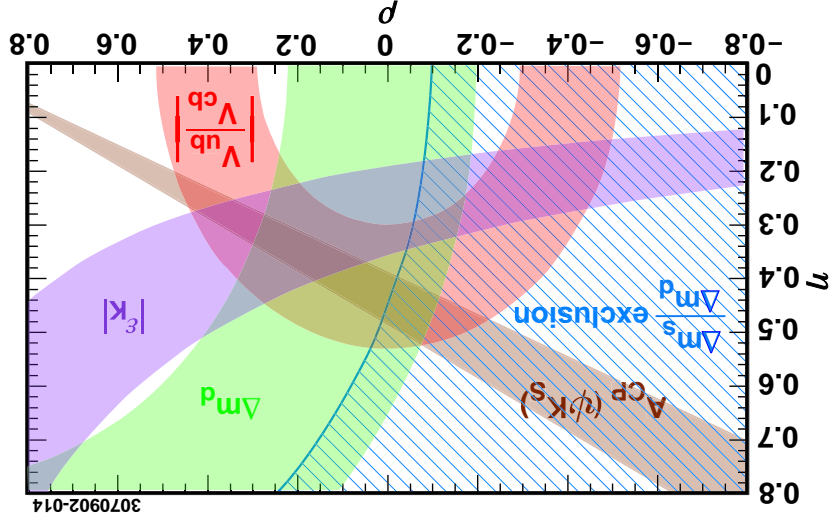


**Karl Ecklund, Cornell University
May 22, 2003**

$|V^{cb}|$ and $|V^{ub}|$ in the Unitarity Triangle

Program of heavy flavor physics — test flavor sector of Standard Model
 Precision measurements of $|V^{ub}|$ and $|V^{cb}|$ needed to test CKM paradigm
 for Flavor mixing and CP violation

Status of test: Unitarity Triangle; apex at (ρ, η)



- Need sides and angles
- $|V^{cb}|$ is base of UT
- $|V^{ub}|$ is height of UT
- Tree level $b \rightarrow cl\nu, b \rightarrow ul\nu$:
- New physics unlikely
- No Final State Interactions
- $\hat{Q}CD$ corrections from HQET

Non-perturbative QCD is hard: largest uncertainties

Must test predictions of HQET and make multiple measurements!

CKM Measurements in Semileptonic B Decays

In naive spectator picture the process is analogous to μ decay

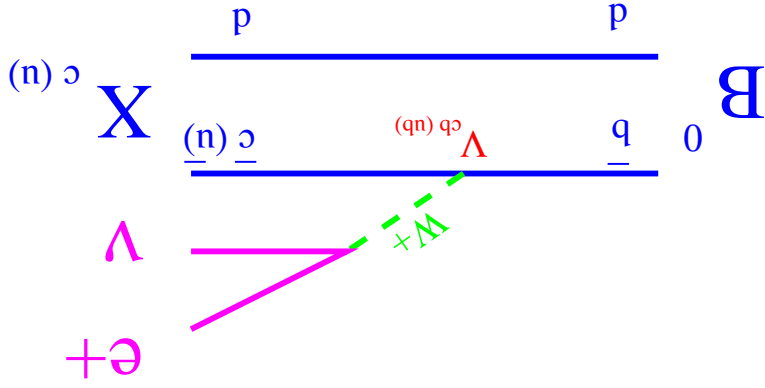
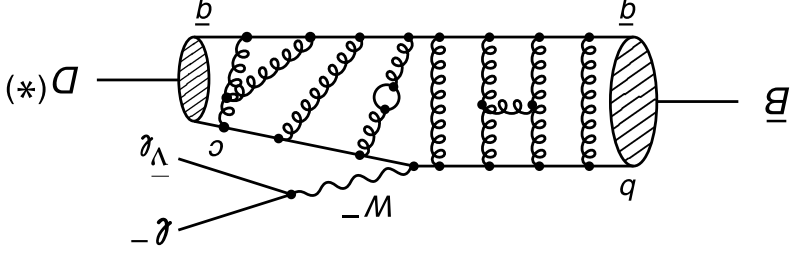
$$\Gamma(b \rightarrow u\ell\nu) \approx \frac{G_F^2 m_b^5}{192\pi^3} |V_{ub}|^2$$

Rate gives $|V_{ub}|^2$

Complication!

QCD Corrections are needed to extract weak physics
 Both perturbative and non-perturbative QCD Corrections:
 Directly calculate or measure via related processes
 Use many techniques and compare results to gain confidence in QCD corr.

Two approaches: Exclusive and Inclusive measurements



$|V_{cb}|$ from $\bar{B} \rightarrow D^* \ell \bar{\nu}$

Extracting $|V_{cb}|$ from exclusive decays:

The decay rate is given by

$$\frac{d\Gamma}{dw} = \frac{G_F^2}{48\pi^3} |V_{cb}|^2 [\mathcal{F}(w)]^2 \mathcal{K}(w)$$

$$w = v_B \cdot v_{D^*} = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}$$

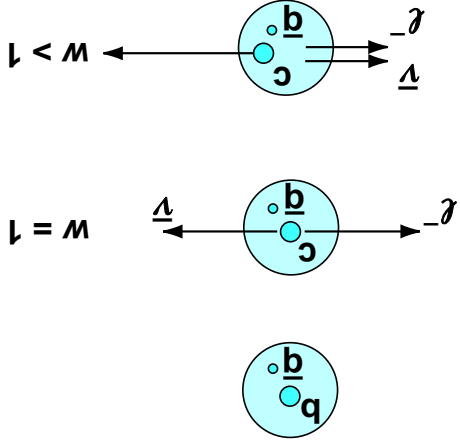
- $\mathcal{K}(w)$ contains kinematic factors and is *known*

- $\mathcal{F}(w)$ is the form factor describing $B \rightarrow D^*$ transition

- HQET relations simplify the form factor

- HQS normalizes at zero recoil ($w = 1$): As $M_{D^*} \rightarrow \infty$, $\mathcal{F}(1) \rightarrow 1$
- Corrections to HQS limit at $\mathcal{O}(1/M_{D^*}^2)$: $\mathcal{F}(1) = 0.91 \pm 0.04$

Plan: Measure $d\Gamma/dw$ and Extrapolate to $w = 1$ to extract $\mathcal{F}(1)|V_{cb}|$.



CLEO $B \rightarrow D^* \ell \bar{\nu}$ PRL 89, 081803 (2002) & PRD 67, 032001 (2003)

(3.1 fb⁻¹ 3.3 MB \bar{B})

Given yields in 10 w bins

Fit using Caprini form factor

Parameters:

- $\mathcal{F}(1)|V^{cb}|$ (intercept)

- ρ^2 (slope)

$$\mathcal{F}(1)|V^{cb}| = (43.1 \pm 1.3 \pm 1.8) \times 10^{-3}$$

$$\rho^2 = 1.61 \pm 0.09 \pm 0.21$$

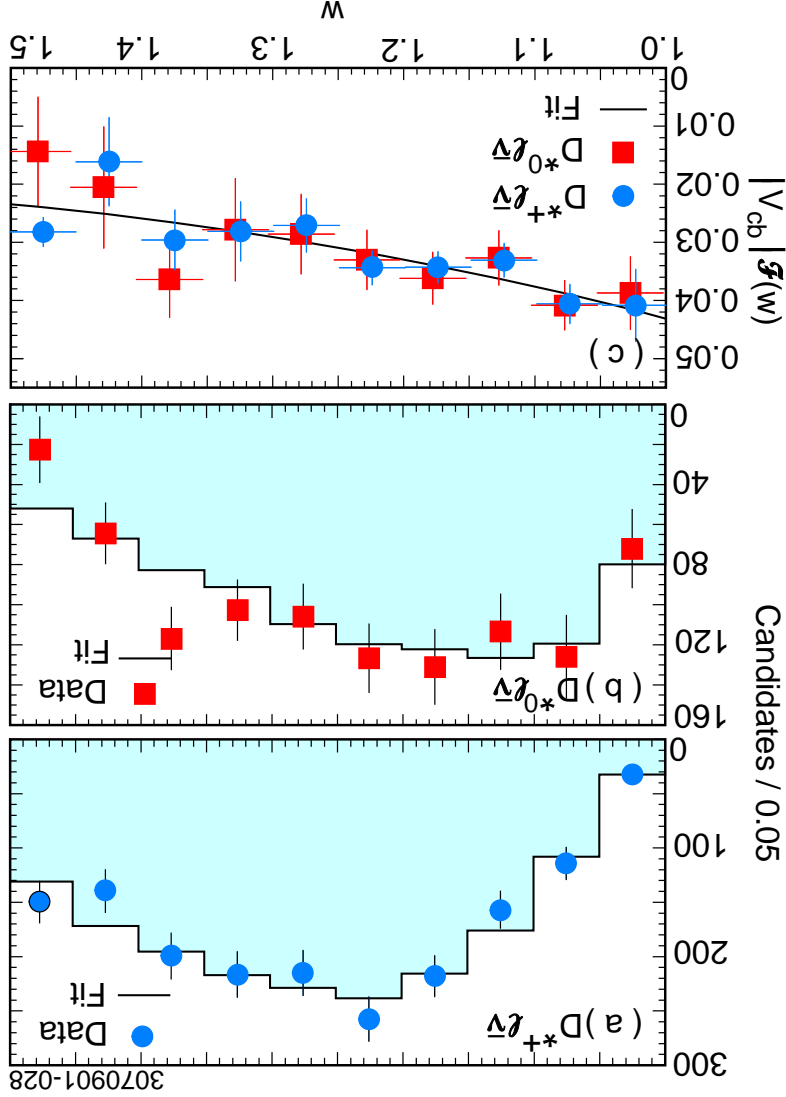
$$|V^{cb}| = (47.4 \pm 1.4 \pm 2.0 \pm 2.1) \times 10^{-3}$$

Theory: $\mathcal{F}(1) = 0.91 \pm 0.04$

6.7% precision

Systematics! efficiency, bkgds, BFs

Larger $|V^{cb}|$ than previous results



Inclusive $b \rightarrow c\ell\bar{\nu}$

Rather than focusing on one hadronic final state where corrections may be calculated reliably,

Sum over all states and compare to quark-level calculation

$$\sum_i \Gamma(\bar{B} \rightarrow X_c^{(i)} \ell \bar{\nu}) = \Gamma(b \rightarrow c \ell \bar{\nu})$$

Sum over hadronic states: $X_c^{(i)} = D, D^*, D^{**}, D\pi$ non-resonant, ...

Relies on **assumption of quark-hadron duality**

Hard to quantify; must be tested!

Fortunately there are other observables besides Γ

- lepton energy spectrum
- hadronic recoil mass

Use these to constrain theory parameters and test consistency

Theoretical Tools for Inclusive $b \rightarrow c\bar{l}\nu$

Heavy Quark Expansion in powers of $1/M_B$ and α_s

Operator Product Expansion - introduce parameters as matrix elements of non-perturbative operators:

At order $1/M$:

$\bar{\Lambda} \approx M_B - m_b$ energy of light degrees of freedom

At order $1/M^2$:

λ_1 - kinetic energy of b quark in B meson

λ_2 - hyperfine interaction of b spin with light d.o.f.

(determine $\lambda_2 = 0.128 \pm 0.010 \text{ GeV}^2$ from $B-B^*$ mass splitting)

At order $1/M^3$:

ρ, \mathcal{T} - six more parameters with less-intuitive interpretations

and so on ... [c.f. Manohar and Wise, *Heavy Quark Physics*]

Use HQE/OPE tools to calculate semileptonic decay rate

$$\Gamma_{\text{SL}} = G_2^F |V_{cb}|^2 M_B^5 \left[G_0 + \frac{M_B}{1} G_1(\bar{V}, \lambda_1, \lambda_2) + \frac{M_B^2}{1} G_2(\bar{V}, \lambda_1, \lambda_2) \right] + \frac{1}{1} M_B^3 G_3(\bar{V}, \lambda_1, \lambda_2 | \rho_1, \rho_2, T_1, T_2, T_3, T_4) + \mathcal{O}\left(\frac{M_B^4}{1}\right)$$

and moments of decay spectra in $B \rightarrow X^c \ell \bar{\nu}$:

$$\langle E_\ell \rangle, \langle E_\ell^2 \rangle, \langle M_X^2 \rangle \quad [\text{Falk, Luke, Savage, Gremm, Kapustin, Bauer, Trott}]$$

$$\text{and } B \rightarrow X^s \gamma: \langle E_\gamma \rangle, \langle E_\gamma^2 \rangle \quad [\text{Bauer, Ligeti et al.}]$$

Example:

$$\langle E_\gamma \rangle = \frac{M_B}{2} \left[1 - .385 \frac{\pi}{\alpha_s} - .620 \beta_0 \left(\frac{\pi}{\alpha_s} \right)^2 - \frac{M_B}{\bar{\Lambda}} \left(1 - .954 \frac{\pi}{\alpha_s} - 1.175 \beta_0 \left(\frac{\pi}{\alpha_s} \right)^2 \right) \right] - \frac{12 M_B^3}{13 \rho_1 - 33 \rho_2} - \frac{4 M_B^3}{T_1 + 3 T_2 + T_3 + 3 T_4} - \frac{9 M_B M_D^2 C^7}{\rho^2 C^2} + \mathcal{O}(1/M_B^4)$$

$B \rightarrow X_s \gamma: E_\gamma$ Moments

CLEO $b \rightarrow s \gamma$ spectrum

PRL 87, 251807 (2001) $\langle E_\gamma \rangle \approx m_b/2$

Broadened by

- Fermi motion
- gluon bremsstrahlung
- B boost in lab

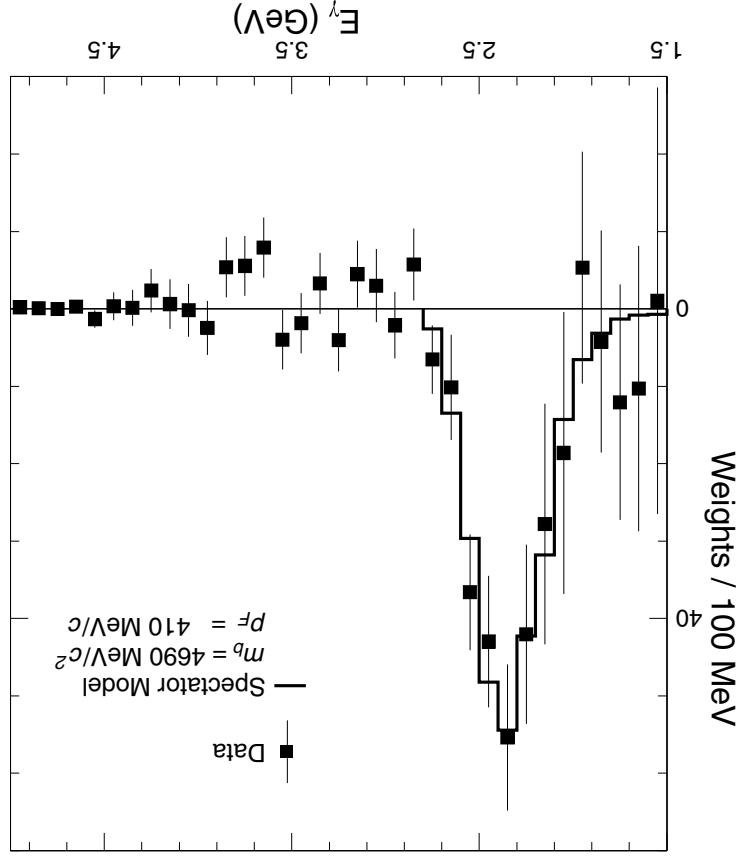
Use first moment to determine $\bar{\Lambda}$

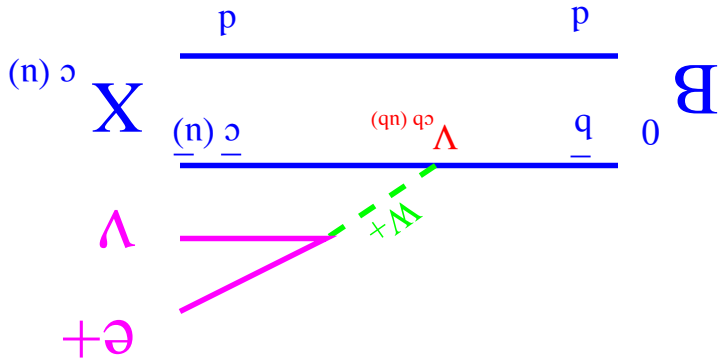
$$\bar{\Lambda} = 0.35 \pm 0.08 \pm 0.10 \text{ GeV}$$

Theory: Bauer PRD57, 5611 (1998)

Ligeti *et al.*, PRD60, 034019 (1999)

$$\begin{aligned} \langle E_\gamma \rangle &= 2.346 \pm 0.032 \pm 0.011 \text{ GeV} \\ \langle (E_\gamma - \langle E_\gamma \rangle)^2 \rangle &= 0.0231 \pm 0.0066 \pm 0.0022 \text{ GeV}^2 \end{aligned}$$





CLEO PRL 88, 251808 (2001)

Require $E_\ell > 1.5 \text{ GeV}$

(P_ν, E_ν) from hermetic detector

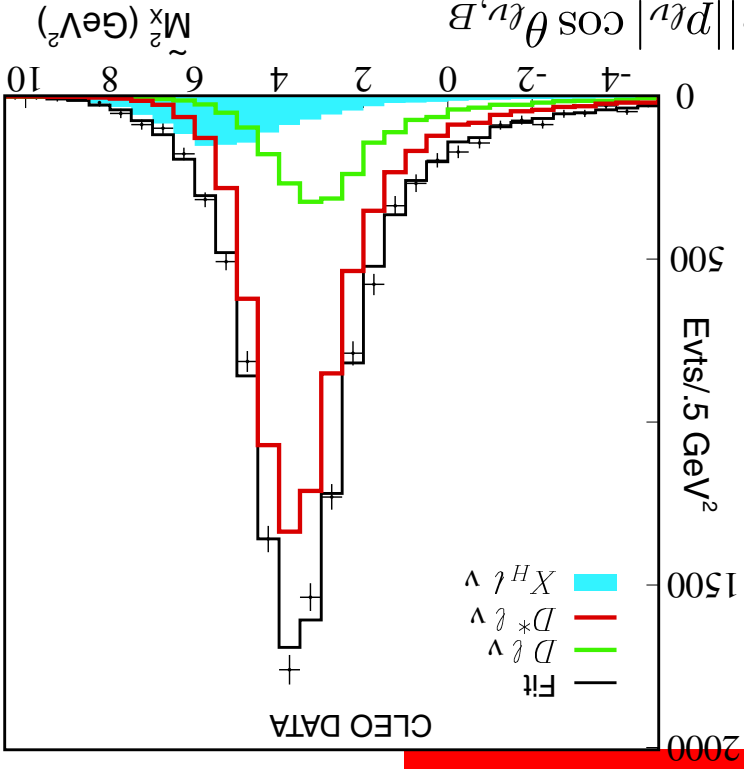
$$M_X^2 = M_B^2 + M_\nu^2 - 2E_B E_{\ell\nu} + 2|p_B||p_{\ell\nu}|\cos\theta_{\ell\nu,B}$$

$$\widetilde{M_X^2} = M_B^2 + M_\nu^2 - 2E_B E_{\ell\nu} \approx M_X^2$$

$$\langle M_X^2 - \widetilde{M_X^2} \rangle = 0.251 \pm 0.023 \pm 0.062 \text{ GeV}^2$$

$$\langle (M_X^2 - \widetilde{M_X^2})^2 \rangle = 0.639 \pm 0.056 \pm 0.178 \text{ GeV}^4$$

Spin-averaged D mass: $\frac{M_D}{4} = (M_D + 3M_{D^*})/4$



$B \rightarrow X^c \ell \nu: M_X^2$ Moments

Determination of $\bar{\Lambda}$ and λ_1

Combine
 $B(B \rightarrow X^c \ell \nu) = (10.39 \pm 0.46)\%$
 (CLEO, $B \rightarrow X^u \ell \nu$ removed)
 and τ_B (PDG2000) to find
 $\Gamma_{SL} = (0.427 \pm 0.020) \times 10^{-10}$ MeV

Add $\bar{\Lambda}$, λ_1 to determine

$$|V_{cb}| = (40.4 \pm 0.5 \pm 0.9 \pm 0.8) \times 10^{-3}$$

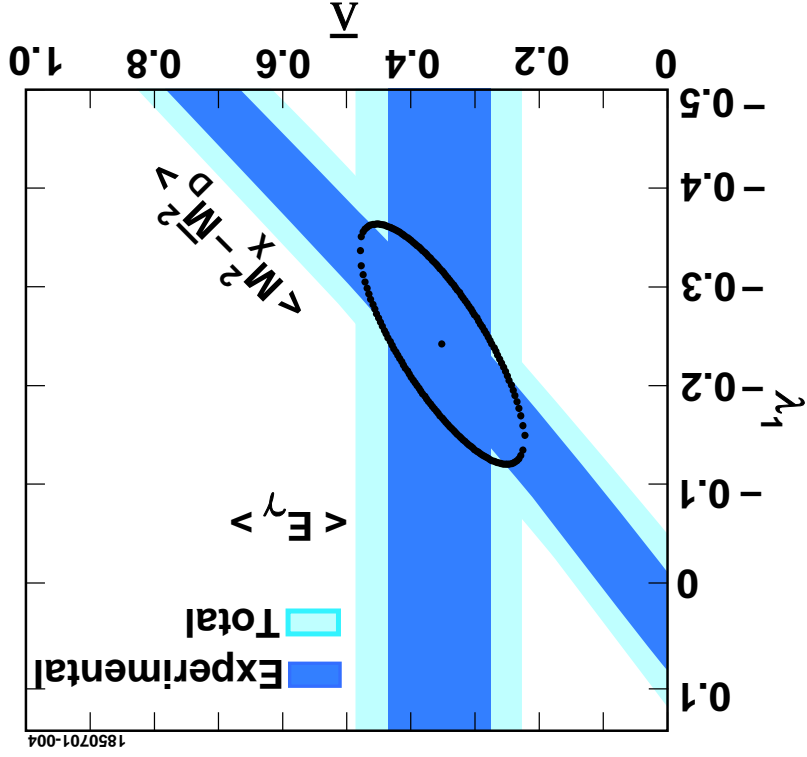
(M) (T) (T)

3.2% determination of $|V_{cb}|$

implicit q-H duality assumption

E_{ℓ} moments also sensitive to $\bar{\Lambda}$, λ_1

How consistent?



$$\bar{\Lambda} = 0.35 \pm 0.07 \pm 0.10 \text{ GeV}$$

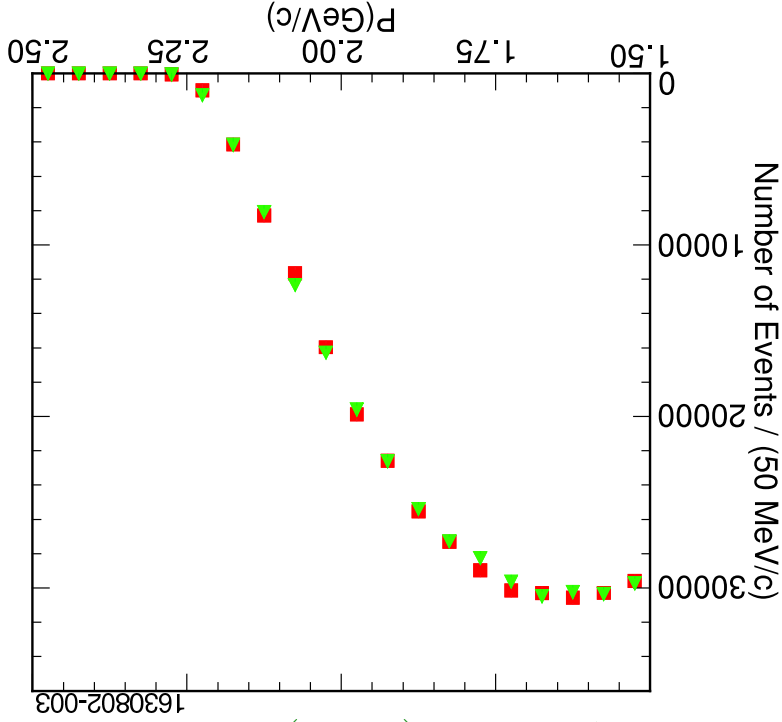
$$\lambda_1 = -0.238 \pm 0.071 \pm 0.078 \text{ GeV}^2$$

Warning: scheme dependence

MS to order $1/M^3$, $\beta_0 \alpha_s^2$

$B \rightarrow X^c \ell \nu : E_\ell$ Moments

CLEO Lepton Spectrum (3 fb^{-1})
 PRD 67, 072001(2003)

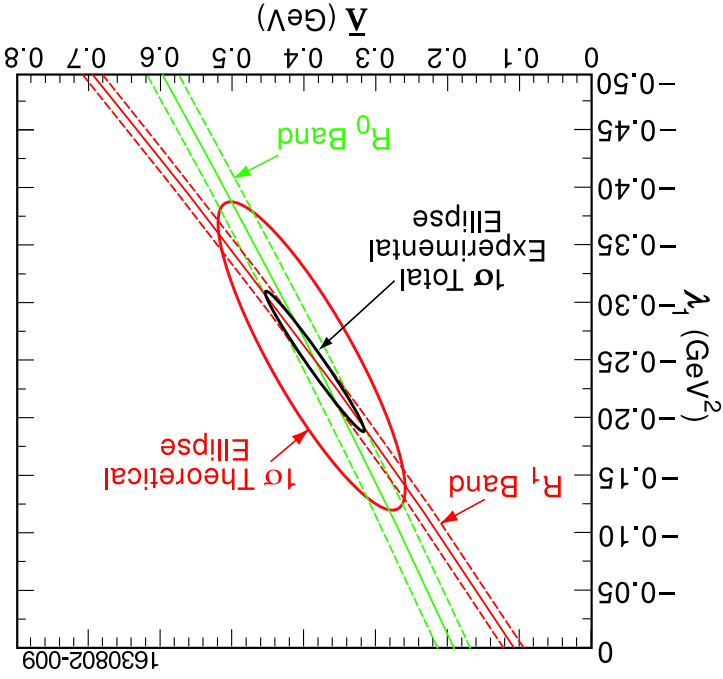


	R_0	R_1 (GeV)
Electrons	0.6184(16)(17)	1.7817(08)(10)
Muons	0.6189(23)(20)	1.7802(11)(11)
Combined	0.6187(14)(16)	1.7810(07)(09)

Generalized Energy Moments:
 Gremm *et al.* PRL77,20 (1996)

$$R_0 = \frac{\int_{1.5 \text{ GeV}} \frac{dF}{dE_\ell} dE_\ell}{\int_{1.7 \text{ GeV}} \frac{dF}{dE_\ell} dE_\ell}$$

$$R_1 = \frac{\int_{1.5 \text{ GeV}} E_\ell \frac{dF}{dE_\ell} dE_\ell}{\int_{1.5 \text{ GeV}} \frac{dF}{dE_\ell} dE_\ell}$$



Comparing Constraints on $\bar{\Lambda}, \lambda_1$

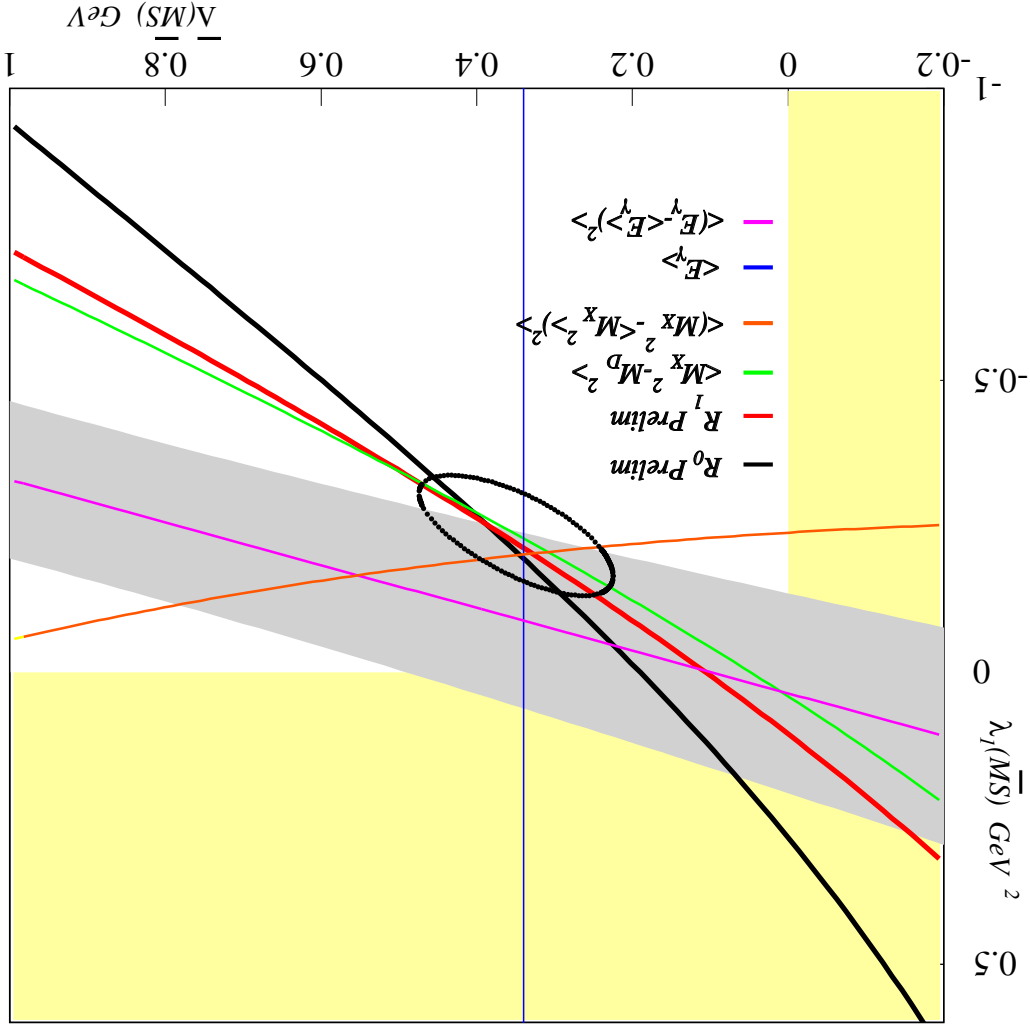
Moment Measurements
from CLEO

All in agreement!
Worst within 1σ (E+T)
 $\langle (E_\gamma - \langle E_\gamma \rangle)^2 \rangle$

Ellipse shows E+T from
 $\langle E_\gamma \rangle$ and $\langle M_X^2 \rangle$

So far inclusive method
looks good, but ...

- Uncertainties still large
- Hints of trouble for $\langle M_X^2 \rangle$ as E_{\min}^{ℓ} is lowered (BABAR@ICHEP02)



Measurement of Semileptonic Branching Fraction

- Update of PRL 76, 1570 (1996)
- 10 fb^{-1} of $B\bar{B}$ data
- $p > 1.4 \text{ GeV}/c$ lepton tag

98% $B \rightarrow X\ell\nu$; $Q_\ell = \text{flavor tag}$

- Additional electron (un)like sign

- Remove backgrounds

- Unfold primary and secondary

leptons using charge, kinematic

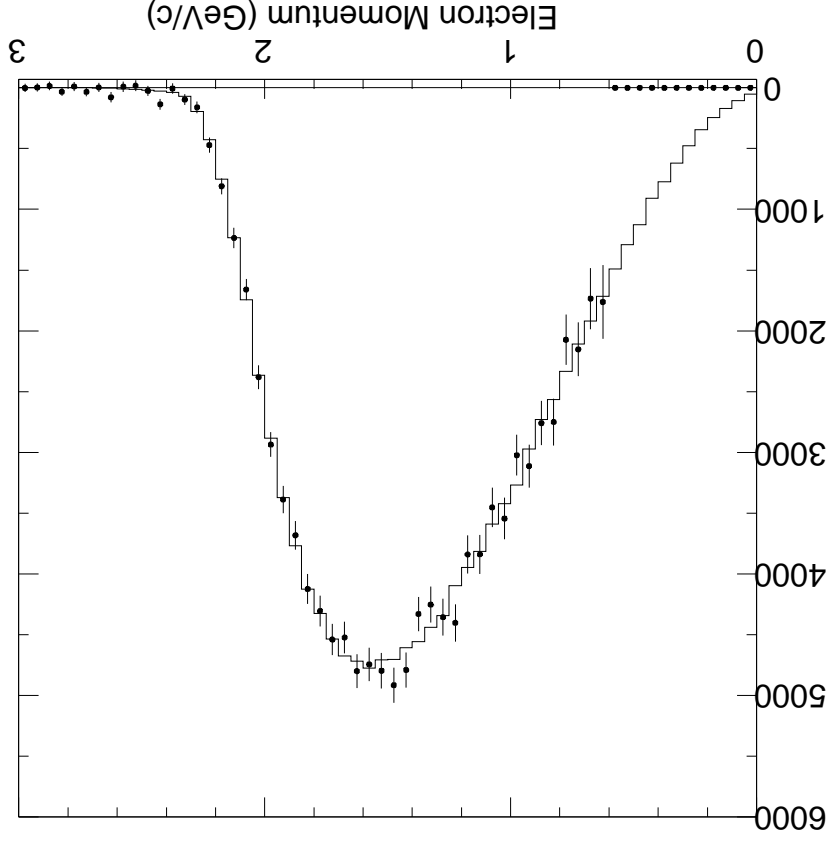
correlations

- Correct for $B^0\text{-}\bar{B}^0$ mixing

$$B(B \rightarrow X e^+ \nu) = (10.88 \pm 0.08 \pm 0.33)\%$$

PRELIMINARY

Coming soon: Spectral moments for $E_{\text{min}}^\ell = 0.7 \text{ GeV}$



|V^{cb}| Summary and Outlook

Measurement	$ V^{cb} \times 10^3$	$\delta V^{cb}/V^{cb}$
CLEO $\bar{B} \rightarrow D^* \ell \bar{\nu}$	$(47.4 \pm 2.4 \pm 2.1)$	6.7%
WG Average $\bar{B} \rightarrow D^* \ell \bar{\nu}$	$(42.0 \pm 1.2 \pm 1.8)$	5.2%
CLEO $\bar{B} \rightarrow X^c \ell \bar{\nu}$	$(40.4 \pm 1.0 \pm 0.8)$	3.2%

- Inclusive techniques are currently more precise but with reliance on theoretical framework to determine non-perturbative parameters

- Hints of a discrepancy (2σ) for $\bar{B} \rightarrow D^* \ell \bar{\nu}$

- Working Group Average has only a 5% Confidence Level

- Exclusive/Inclusive agreement tests quark-hadron duality

- CLEO Exclusive and Inclusive differ by 2σ

- WG Average Exc. and Inc. are in excellent agreement

- Expect to hear more from CLEO on inclusive analyses soon

Experimental Challenges in $b \rightarrow ul\nu$

Approaches:

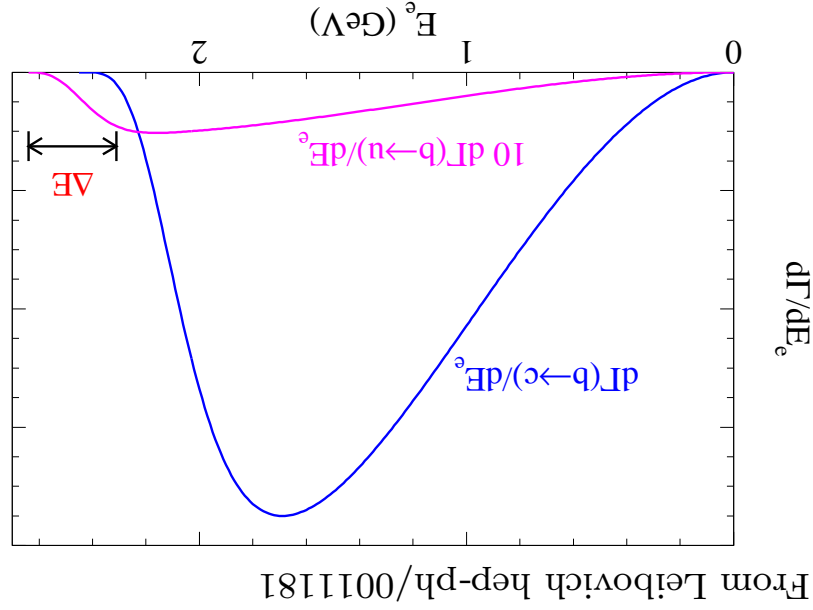
- Exclusive Reconstruction
 - + Constraints from full recon
 - + Inclusive Reconstruction
 - + Kinematic cuts (% of rate)

- $E_\ell \gtrsim 2.4 \text{ GeV}$ (13%)
- $q^2 \gtrsim 12 \text{ GeV}^2$ (20%)
- $M_X \lesssim M_D$ (70%)

Both approaches currently suffer from large uncertainties

- Exc: Poorly form factors
 - Inc: Effect of kinematic cuts
- (...not very inclusive!)

→ Important to pursue both inclusive and exclusive measurements.



Large $b \rightarrow cl\nu$ backgrounds

- Signal is 1% of background!
- Suppress using kinematics

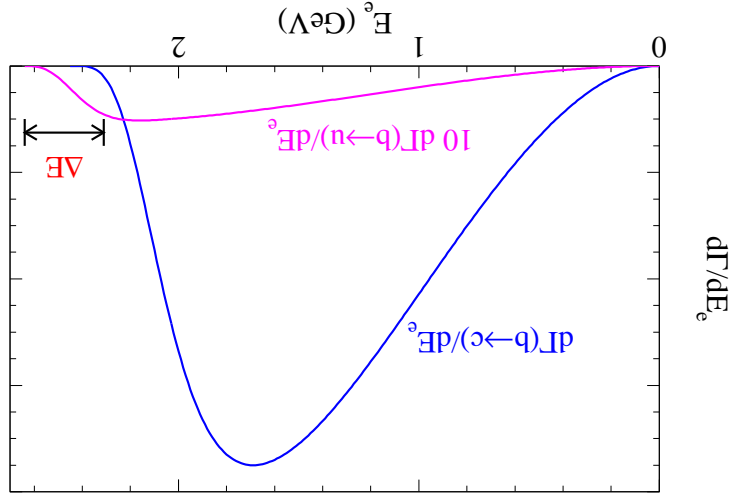
$|V^{ub}|$ from lepton spectrum and $b \rightarrow s\gamma$

To measure $b \rightarrow u\ell\nu$

Must suppress $b \rightarrow c\ell\nu$

Cutting on E_ℓ introduces problems:

- Large model dependence (What fraction above cut?)
- At edge of spectrum sensitive to b quark motion

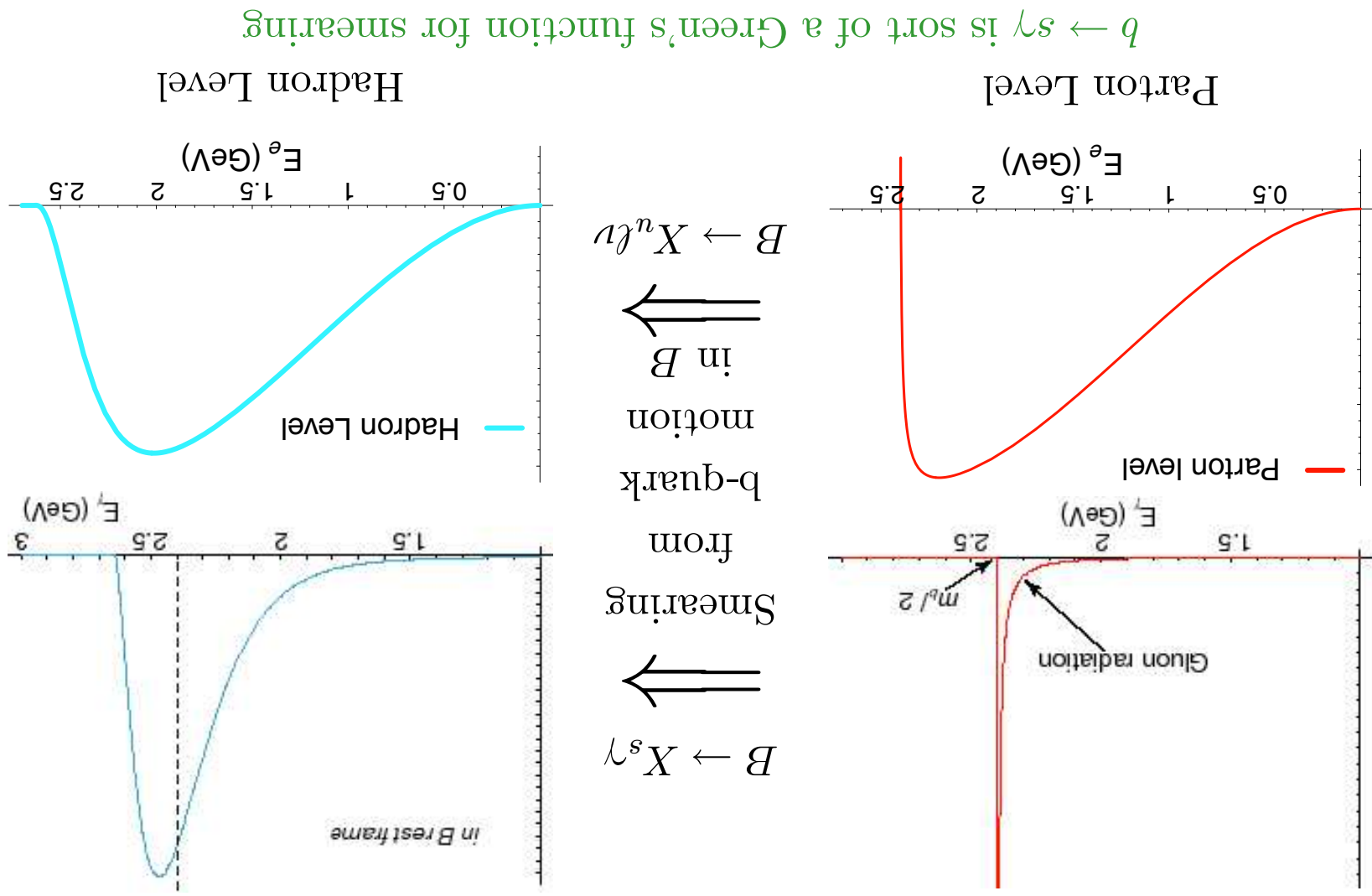


Idea: Reduce problems by using $b \rightarrow s\gamma$ photon spectrum

To first order same non-perturbative QCD effects smear the spectra
 Both are heavy \rightarrow light decays ($m_s, m_u, m_c, m_\nu \approx 0$)

Neubert; Bigi, Shifman, Uraltsev, Vainshtein; Leibovich, Low, Rothstein

How $B \rightarrow X_s \gamma$ helps $|V^{ub}|$



$b \rightarrow s \gamma$ is sort of a Green's function for smearing

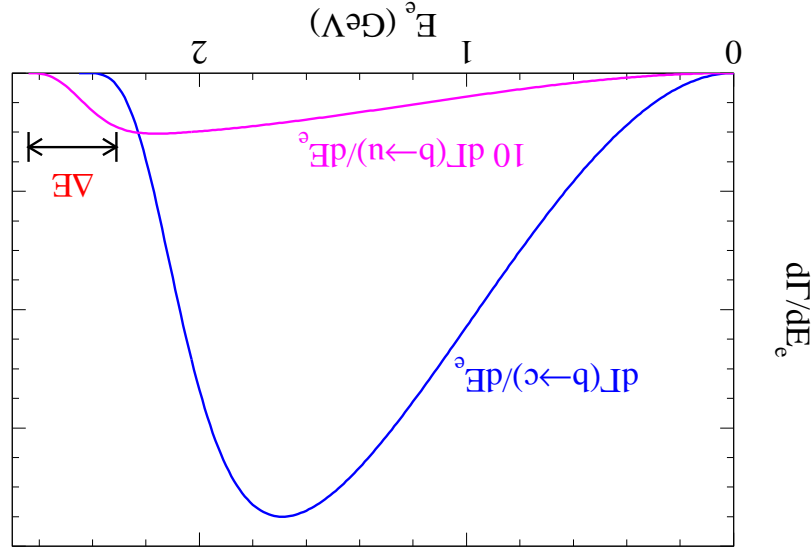
Measurement of Endpoint Rate

CLEO, Phys. Rev. Lett. **88**, 231803 (2002) $9.1/4.3 \text{ fb}^{-1} \text{ On/OFF-}\tau(4S)$

Analysis Strategy:

- Lepton energy cut $E > 2.2 \text{ GeV}$
- Control $B \rightarrow X^c \ell \nu$ by fit below 2.2 GeV
- Remove $e^+ e^- \rightarrow q \bar{q} \rightarrow \ell$

- suppress with event shape
- subtract with off- $\tau(4S)$ data
- Remove other backgrounds



Lepton Yields:

N_{on}	8967	$B \rightarrow X^c \ell \nu$	$4562 \pm 33 \pm 246$
N_{off}	983	Backgrounds	$474 \pm 22 \pm 67$
$N_{B\bar{B}}$	$6938 \pm 115 \pm 20$	$B \rightarrow X^u \ell \nu$	$1901 \pm 122 \pm 256$

$|V^{ub}|$ from lepton spectrum and $b \rightarrow s\gamma$

In $(2.2 < p_T < 2.6)$ GeV/c

• suppress and subtract $q\bar{q}$ (cyan)

• subtract $B \rightarrow X^c l \nu$ yield (hist)

• $N^{ub} = 1901 \pm 122 \pm 256$

$B \rightarrow X^u l \nu$ events

• $\Delta B^u = (2.30 \pm 0.15 \pm 0.35) \times 10^{-4}$

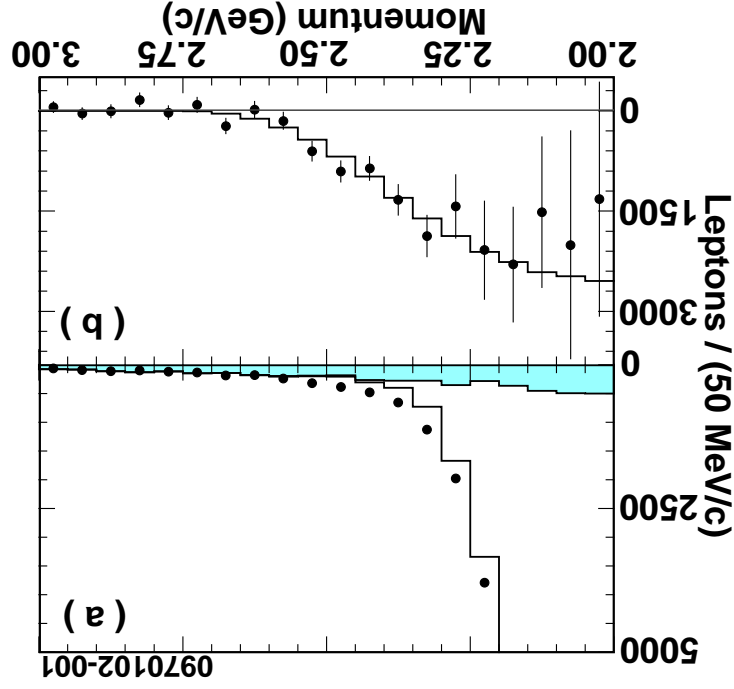
• From the $b \rightarrow s\gamma$ spectrum

$f_u = 0.130 \pm 0.024 \pm 0.015$

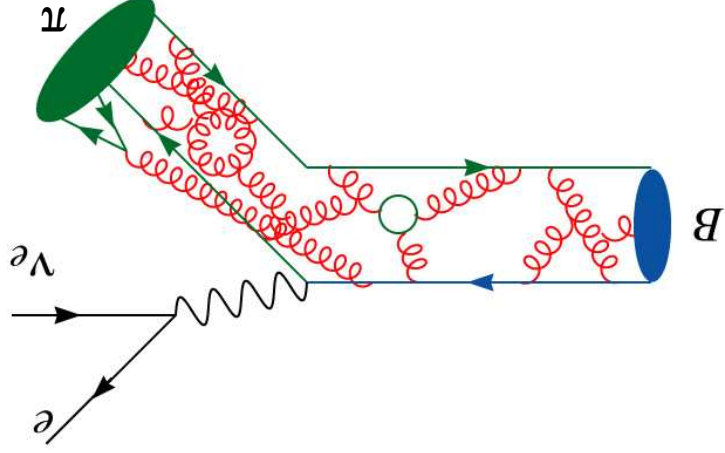
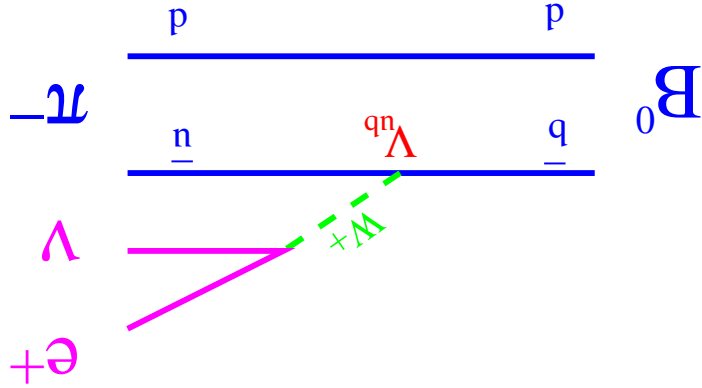
$B(B \rightarrow X^u l \nu) = \Delta B / f_u = (1.77 \pm 0.29 \Delta_B \pm 0.38 f_u) \times 10^{-3}$ implies

$$|V^{ub}| = (4.08 \pm 0.34^{\text{exp}} \pm 0.44 f_u \pm 0.16 \Gamma \pm 0.24 \Lambda / M^B) \times 10^{-3}$$

Improved 15% uncertainty CLEO, Phys. Rev. Lett. **88**, 231803 (2002)



$|V^{ub}|$ from Exclusive Semileptonic B Decays



Once again,

QCD Corrections are needed to extract weak physics

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2 p_\pi^3}{24\pi^3} |f_1(q^2)|^2 |V^{ub}|^2$$

Form factors needed from theory (LQCD, LCSR, quark models)

Neutrino Reconstruction

Uses hermeticity of detector (CLEO 95% of 4π):

$$E_{\text{miss}} = 2E_{\text{beam}} - \sum_i E_i$$

$$\vec{p}_{\text{miss}} = -\sum_i \vec{p}_i$$

$$\vec{p}_\nu \equiv \vec{p}_{\text{miss}}; E_\nu \equiv |\vec{p}_{\text{miss}}|$$

(better resolution than E_{miss})

$$\bullet \sigma(\vec{p}_\nu) \approx 110 \text{ MeV}/c$$

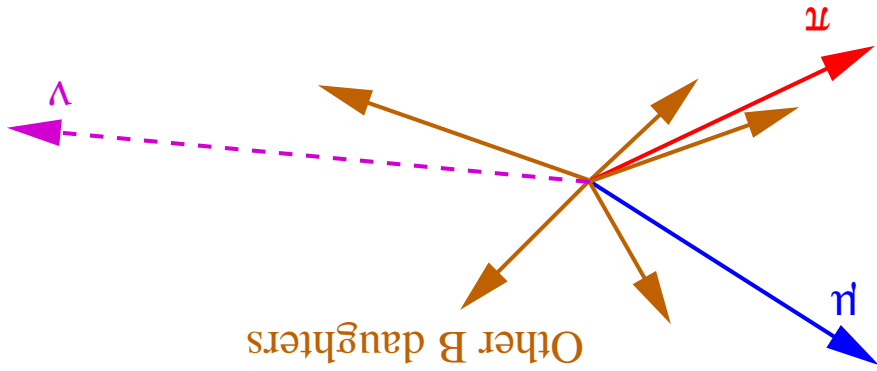
Gives powerful kinematic constraints for full reconstruction:

$$M_{m\ell\nu} = \sqrt{E_{\text{beam}}^2 - |\alpha\vec{p}_\nu + \vec{p}_\ell + \vec{p}_m|^2}$$

$$\Delta E = (E_\nu + E_\ell + E_m) - E_{\text{beam}}$$

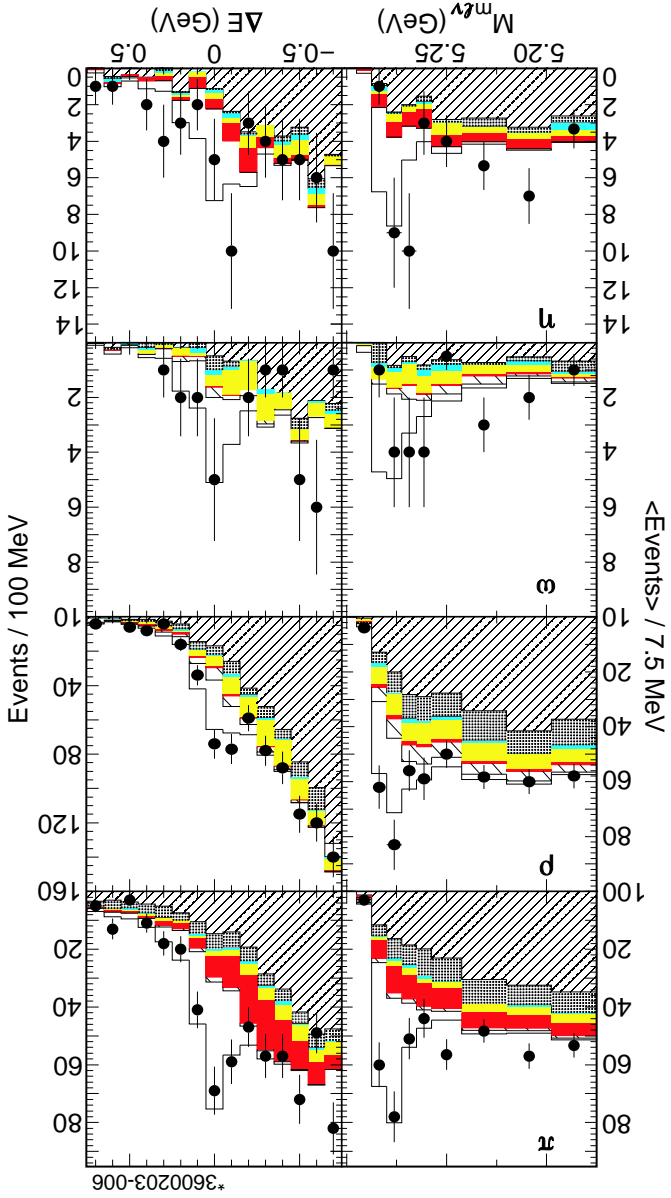
(α rescales magnitude of \vec{p}_ν for slightly improved mass resolution)

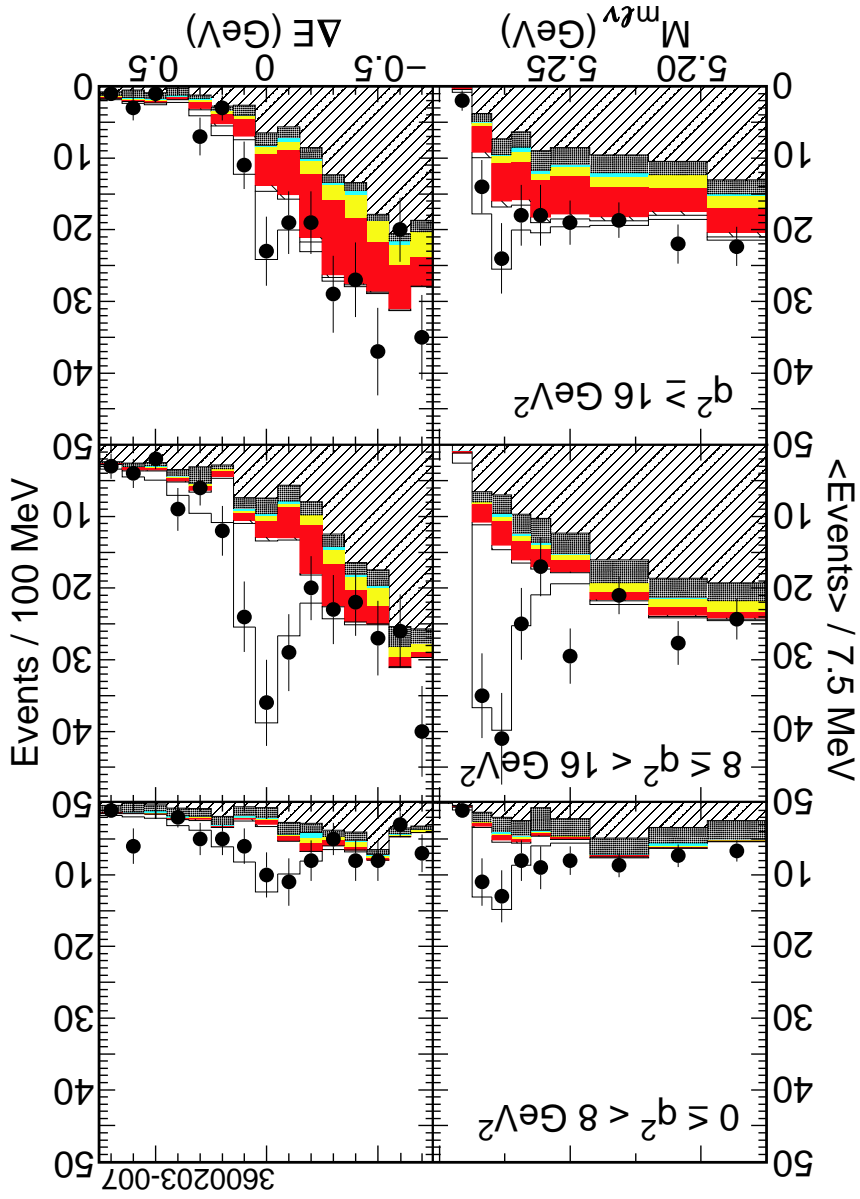
Energy and momentum conservation: $\Delta E \approx 0$, $M_{m\ell\nu} = M_B$ for signal
 Reject “ghost” tracks & shower fragments from hadronic interactions.



Simultaneous Maximum Likelihood Fit

- $\Delta E, M_{m\ell\nu}$ variables
- 7 signal mode topologies [$\pi, \rho, \omega, \eta, \ell\nu$]
- Isospin & quark symmetry constraints:
 - $\Gamma(\pi^-) = 2\Gamma(\pi^0)$
 - $\Gamma(\rho^-) = 2\Gamma(\rho^0) = 2\Gamma(\omega)$
- 3 q^2 bins for π and ρ
- Net event charge $|\Delta Q| = 0, 1$
- Accounts for crossfeed
- $\pi \rightarrow \rho, \rho \rightarrow \pi$ etc



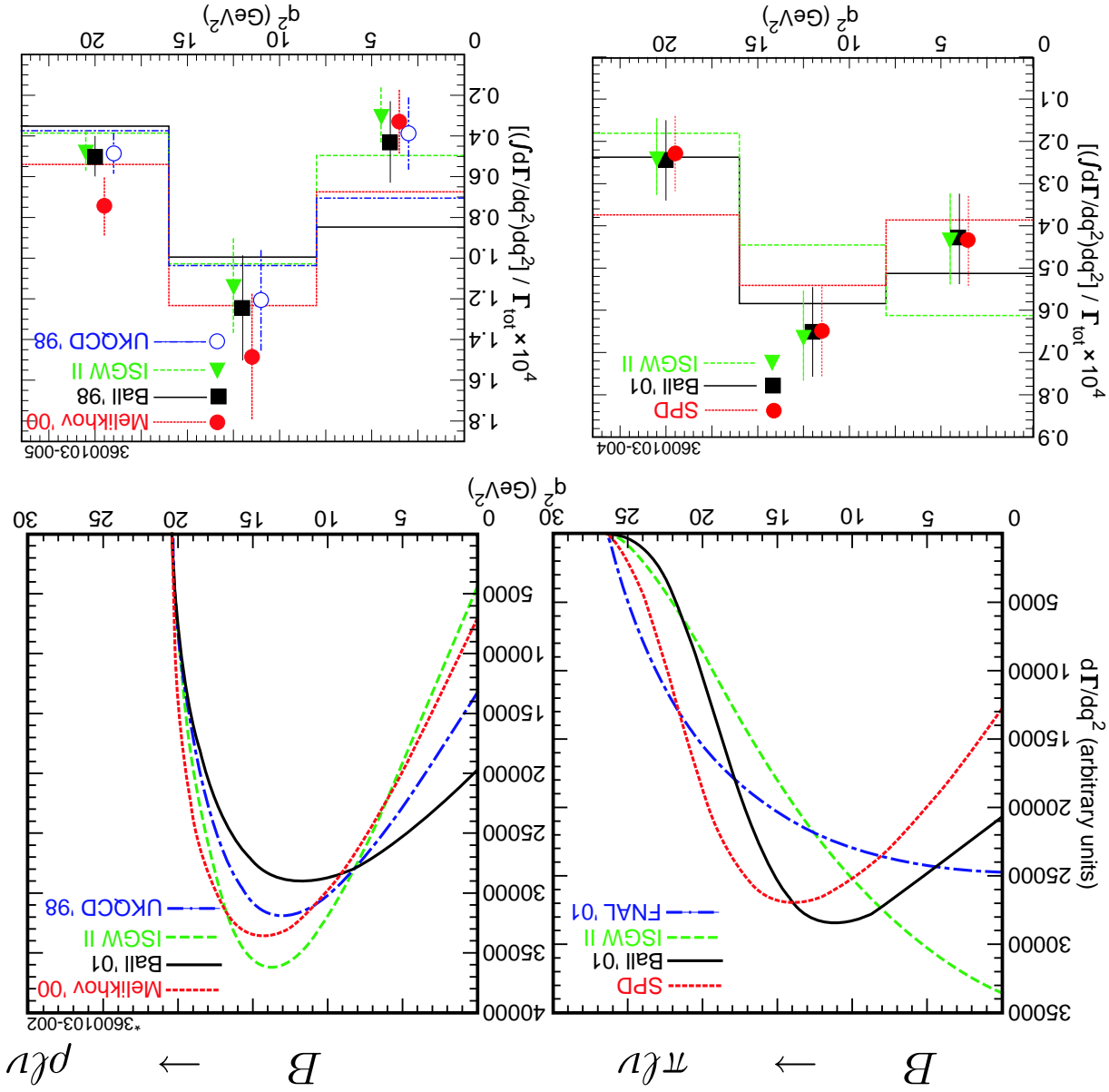


$B \rightarrow \pi \ell^+ \nu$ q^2 binning

Projections show $\Delta Q = 0$

($|\Delta Q| = 1$ also in fit)

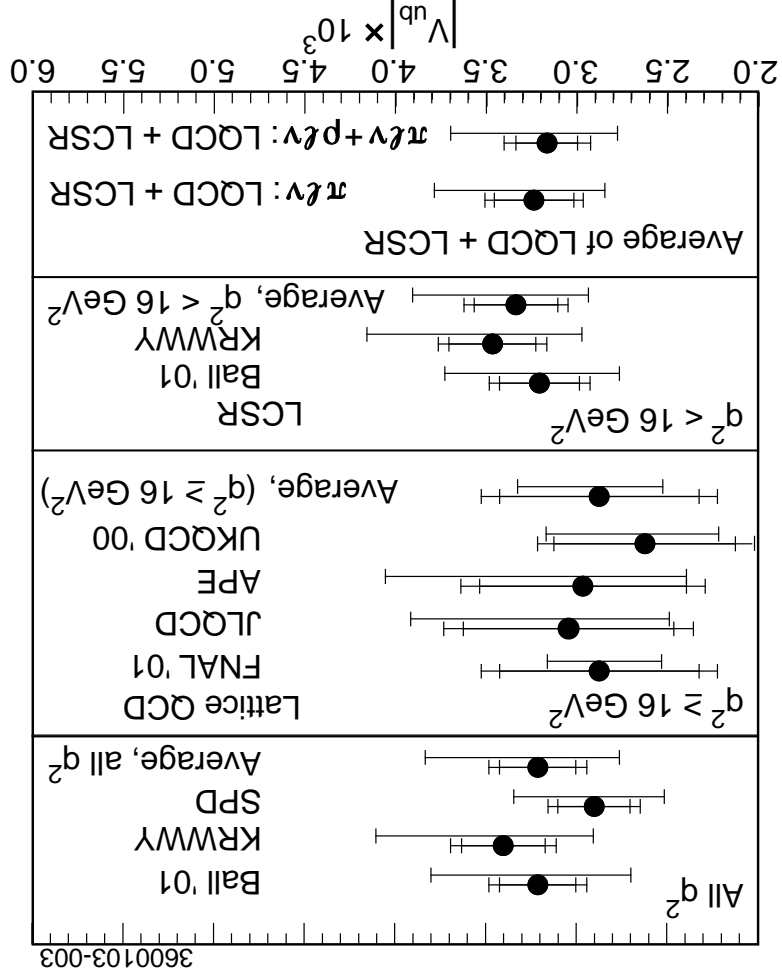
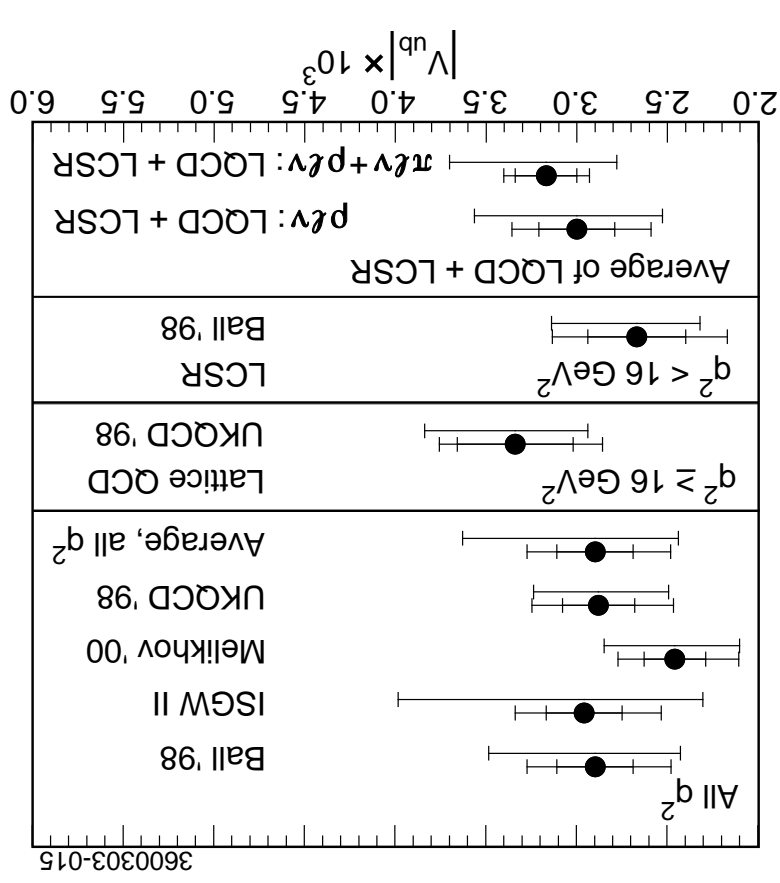
- points on-resonance data
- open histogram signal
- red histogram cross-feed
- from V or η modes
- yellow $B \rightarrow X^u \ell \nu$ other
- cyan fakes
- dotted continuum
- hatched $b \rightarrow c$



- discriminate amongst FFs
- extract $|V_{ub}|$
- $B \rightarrow \pi l \nu$
 - small FF dependence
 - ISGW II is disfavored
 - $B \rightarrow \rho l \nu$
 - larger FF dependence

Extractions of $|V^{ub}|$ from $B \rightarrow \pi \ell \nu$ and $B \rightarrow \rho \ell \nu$

hep-ex/0304019, submitted to PRD



$|V^{ub}| = (3.17 \pm 0.17_{+0.16}^{-0.17} - 0.39 \pm 0.03) \times 10^{-3}$ +18% -14% measurement of $|V^{ub}|$, dominated by theory uncertainty

$(\pi + \rho \text{ LQCD+LCSR})$

Summary and Outlook

- CLEO is pioneering measurements of $|V_{ub}|$ and $|V_{cb}|$
- Analyses using mature data and MC samples
 - Inclusive and Exclusive techniques
 - Moments and Rates in inclusive semileptonic B decays
 - Obtain $|V_{cb}|$ ($\sigma \approx 3\%$) and $|V_{ub}|$ ($\sigma \approx 15\%$)
 - Insight into CKM electroweak and QCD physics
- Most results are limited by systematic and theory uncertainties
- Techniques to reduce model dependence
 - Use of $b \rightarrow s\gamma$ photon spectrum
 - Measurement of partial rates, testing form factors
- Future progress on CKM physics
 - New CLEO B analyses – CLEO-c: CKM, QCD in charm decays

Backup Slides

Status of $\mathcal{F}(1)|V^{cb}|$

Correlated $\mathcal{F}(1)|V^{cb}|$ & ρ^2

$|V^{cb}|$ WG Combined 2d-fit

accounts for correlations

(stat&yst) among expts.

Currently 5% C.L.

N.B. Only CLEO

- Includes D^*0

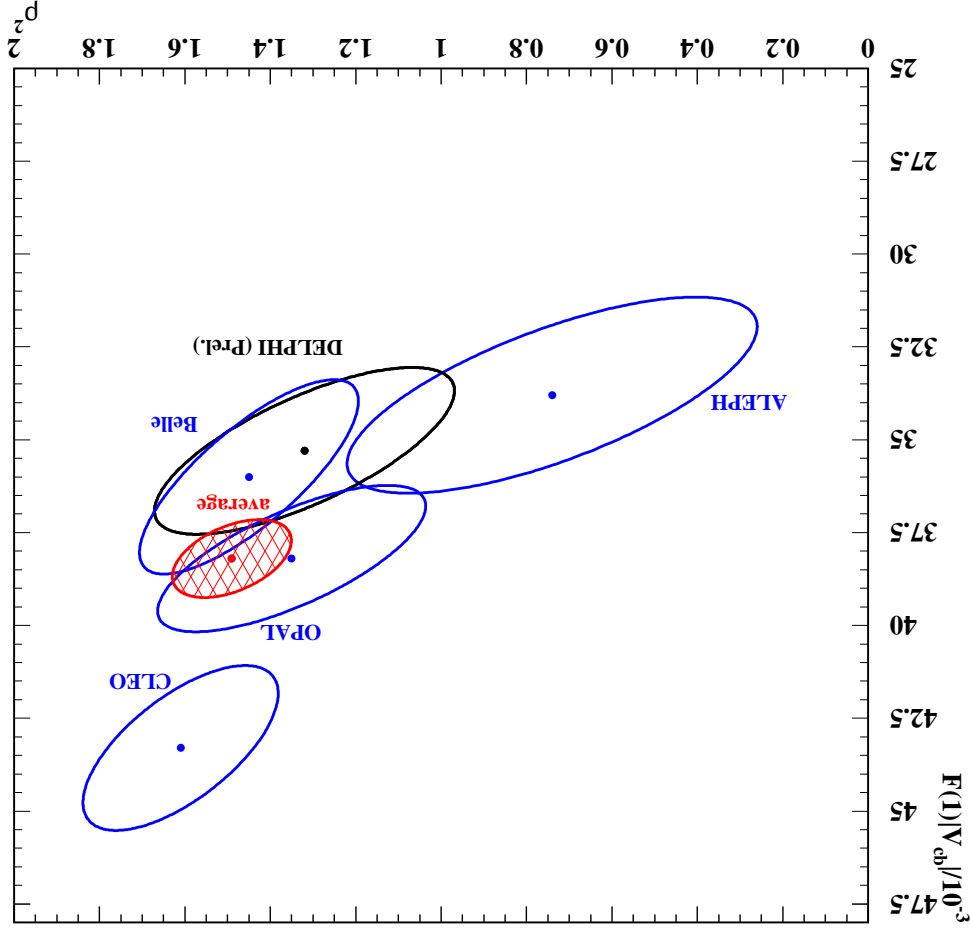
- Fits data simultaneously

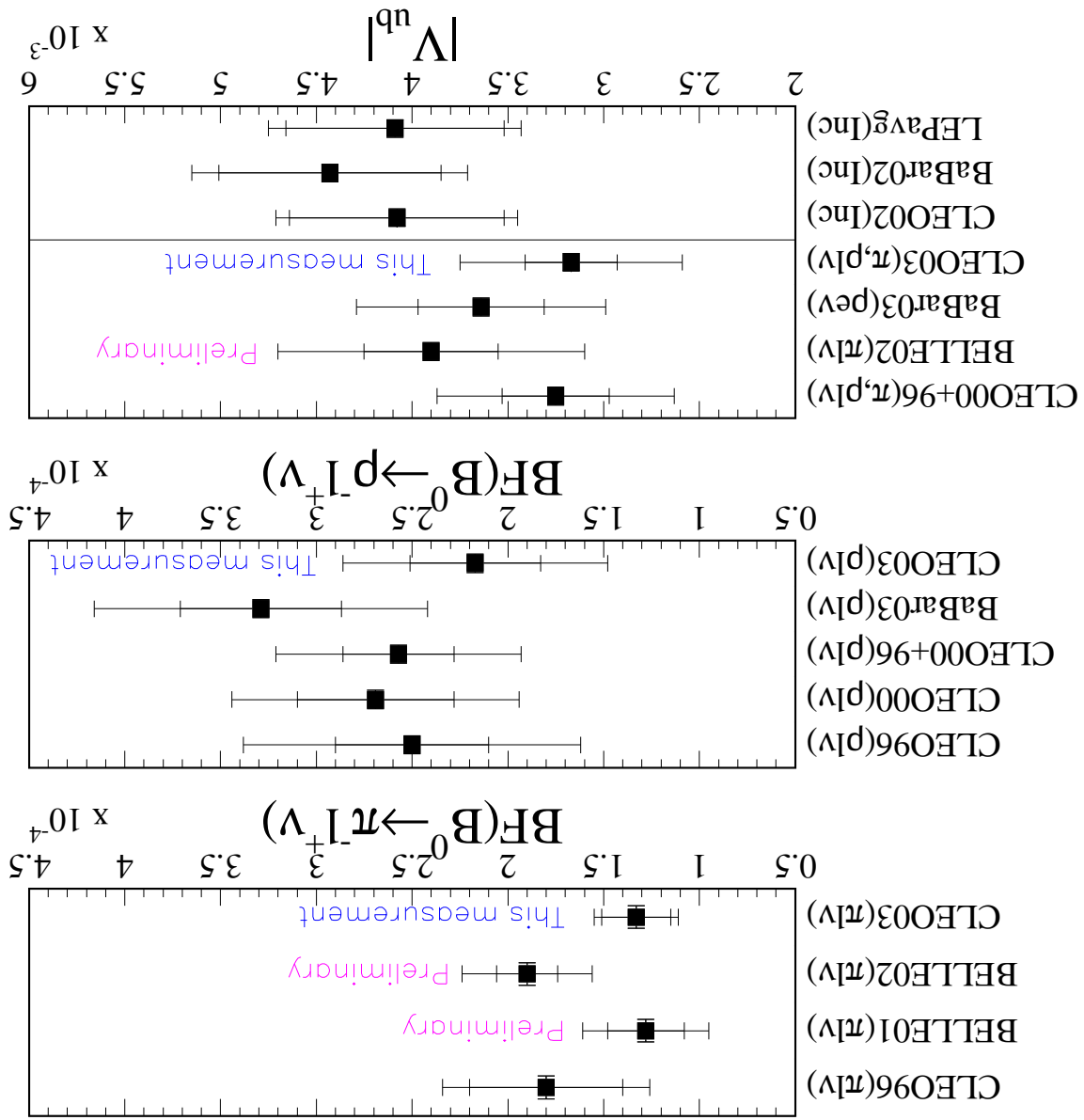
for $D^*X\ell\nu$ background

Others share $D^*X\ell\nu$

estimate & model

Ellipses are $\Delta\chi^2 = 1$ for each measurement (stat+yst)





CLEO's Future in CKM Physics

Apart from $\sin 2\beta$, CKM constraints are limited by QCD corrections. CLFO-c program of weak decay physics at charm threshold can help validate those QCD calculations.

- D^+ and D_s^+ decay constants help limits from B oscillations

- semileptonic D decay form factors help in B decays, $|V^{ub}|$

- charm branching fractions ($D^0 \rightarrow K^- \pi^+$) help $|V^{cb}|$

Impact of shrinking theory

uncertainties only shown on bottom.

