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Measurement of the Ξ_c^+ Lifetime

CLEO Collaboration

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Abstract

The Ξ_c^+ lifetime is measured using 9.0 fb^{-1} of e^+e^- annihilation data collected on and just below the $\Upsilon(4S)$ resonance with the CLEO II.V detector at CESR. The Ξ_c^+ lifetime is measured using an unbinned maximum likelihood fit. The preliminary result for the Ξ_c^+ lifetime is $(503 \pm 47(\mathrm{stat.}) \pm 18(\mathrm{syst.}))$ fs.

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I. INTRODUCTION

Charm baryon lifetime measurements provide insight into the dynamics of non-perturbative heavy quark decays. The theoretical situation is rich with possibilities. Unlike the case of charm mesons the exchange mechanism is not helicity suppressed and therefore can be comparable in magnitude to the spectator diagram. In addition, color suppression is only active for particular decay channels. Thus spectator decays alone can not account for the hadronic width in charm baryon decay. The hadronic width is modified by at least three effects: (a) destructive interference between external and internal spectator diagrams, (b) constructive interference between internal spectator diagrams, and (c) W-exchange diagrams. Effects (a) and (b) are expected to be operative in the decay of the Ξ_c^+, while (a) and (c) play a role in Λ_c^+ decay. While several models [1] can account for the apparent lifetime hierarchy, $\tau_{\Xi_c^+} > \tau_{\Lambda_c^+} > \tau_{\Xi_c^0} > \tau_{\Omega_c}$, a detailed understanding of the various contributions to the hadronic width requires input from experiment.

The lifetimes of the charm baryons are not measured as precisely as the charm mesons (D^0, D^+, D_s) which are measured, by individual experiments [2], to a precision of $\sim$1 - 3%. The Λ_c^+'s lifetime is the most precisely measured of the charm baryons. Recently, CLEO and SELEX measured this lifetime to a precision of 5% [3,4]. Other charm baryon lifetimes (Ξ_c^+, Ξ_c^0, and Ω_c) are measured to $\geq$ 20% uncertainty [2]. This paper presents CLEO's preliminary measurement of the Ξ_c^+ lifetime, the first measurement of this lifetime from an e^+e^- colliding beam experiment.

II. DATA SAMPLE AND EVENT SELECTION

This analysis uses an integrated luminosity of 9.0 fb^{-1} of e^+e^- annihilation data taken with the CLEO II.V detector at the Cornell Electron Storage Ring (CESR). The data were taken at energies at and below the Υ(4S) resonance ($\sqrt{s}$ =10.58 GeV) and include $\sim 11\times10^6$ $e^+e^- \to c\bar{c}$ events. This analysis relies heavily on the charged particle tracking capabilities of the CLEO II.V detector [5]. The precise location of both primary and secondary vertices is greatly aided by a small-radius, low-mass beam pipe surrounded by a three-layer double-sided silicon strip tracker [6]. The trajectories of charged particles are reconstructed using two drift chamber systems in addition to the silicon strip tracker. For this data set the main drift chamber uses a 60:40 mixture of helium propane gas in place of its standard 50:50 argon-ethane mix. This change in gas improves both the hit efficiency and specific ionization resolution while at the same time decreases the effects of multiple scattering. A Kalman filter track reconstruction algorithm [7] is used to reconstruct the three dimensional trajectories of charged particles. The response of the detector to both signal and background events is modeled in detail using the GEANT [8] Monte Carlo package.

The Ξ_c^+ is reconstructed from the decay $\Xi^-\pi^+\pi^+$. Each Ξ^- is reconstructed using the $\Lambda\pi^-$ mode while Λ's are reconstructed from $p\pi^-$ (the charge conjugate mode is implied throughout this paper). For this analysis we assume that the Ξ_c^+ is produced at the primary event vertex and is not a decay product of another long lived weakly decaying particle. Each Ξ_c^+ candidate's proper time, t, and proper time uncertainty, σ_t, is determined from

$$t = \frac{m_{\Xi_c^+}}{c p_{y_{\Xi_c^+}}} (y_{\rm decay} - y_{\rm production}) \tag{1}$$

and

$$\sigma_t = \frac{m_{\Xi_c^+}}{c \mid p_{y_{\Xi_c^+}} \mid} \sqrt{\sigma^2_{y_{\rm decay}} + \sigma^2_{y_{\rm beam\ position}} + \sigma^2_{y_{\rm beam\ size}}} \,. \tag{2}$$

In the above equations the Ξ_c^+ mass, $m_{\Xi_c^+}$, is set to the PDG [2] value of 2466.3±1.4 MeV/c^2. A best-fit decay vertex of the Ξ^- pseudo-track and the two π^+'s determines $y_{\rm decay}$ and its uncertainty, $\sigma_{\rm y_{decay}}$. The production point of a Ξ_c^+ cannot be well measured on an event-by-event basis. Instead we use a combination of the known CESR beam profile and a measurement of the beam centroid to provide the estimate of the Ξ_c^+ production point. In the CLEO environment the dimensions (σ) of the beam profile are 1 cm along the beam line, z, 350 μm along the horizontal direction perpendicular to the beam line, x, and 7 μm ($\sigma_{y_{\rm beam\ size}}$) along the vertical direction, y. Since the typical decay length of a Ξ_c^+ ($\sim$ 150 μm) is significantly less than the beam extent in z and x essentially all useful decay length information comes from the y-coordinate. A run-averaged collision point of the e^+ and e^- beams, $y_{\rm beam\ position}$, is used to estimate $y_{\rm production}$. The uncertainty in $y_{\rm beam\ position}$, $\sigma_{y_{\rm beam\ position}}$, is also calculated run-by-run. The Ξ_c^+'s component of momentum in the y direction, $p_{y_{\Xi_c^+}}$, is calculated from the momentum of its decay products.

While much of the Ξ_c^+ selection criteria are similar to that of previous CLEO charm baryon analyses [9–11] some additional requirements suited for a lifetime measurement are imposed. To select high momentum candidates and reduce B-meson related backgrounds we require the Ξ_c^+'s momentum fraction, $p_{\Xi_c^+}/p_{\Xi_c^+\ \rm max}$, to be larger than 0.5. For each candidate we impose $\sigma_t < 1.5$ ps. A minimum $\Xi^-\pi^+\pi^+$ vertex probability of 0.001 (based on the vertex χ^2) is required to obtain a sample of well-defined decay lengths. To ensure that only one Ξ_c^+ candidate per event is used, the candidate with the smallest vertex χ^2 is chosen in the events where multiple candidates pass all other selection criteria ($\sim$ 7% of events). Figure 1 shows the Λ, Ξ^-, and Ξ_c^+ reconstructed mass distributions for candidates used in the lifetime analysis. A fit of the Ξ_c^+ mass distribution using one Gaussian for the signal and a linear function for the background yields 250 ± 18 reconstructed Ξ_c^+'s and a Gaussian σ of 4.3 MeV/c^2. The fraction of background within $\pm 2\ \sigma$ of the fitted Ξ_c^+ mass is 12.8%. The average flight path in the y direction of the Ξ_c^+'s used in this analysis is 100 μm. The efficiency of the selection cuts for detecting signal Monte Carlo events, including (not including) acceptance, is 7.6% (17%). Events within $\pm$40 MeV/c^2 of the mean reconstructed Ξ_c^+ mass (2468 MeV/c^2), as shown in Figure 1, are used in the determination of the Ξ_c^+ lifetime. This wide mass region is used to estimate the non-Ξ_c^+ contribution to the lifetime.

III. LIFETIME DETERMINATION METHOD

The Ξ_c^+ lifetime is obtained from an unbinned maximum likelihood fit to the proper time distribution. The likelihood function is

$$L(\tau_{\rm sig}, S, \sigma_{\rm mis}, f_{\rm mis}, \tau_{\rm BG}, f_{\tau_{BG}}, f_{\rm flat}) =$$

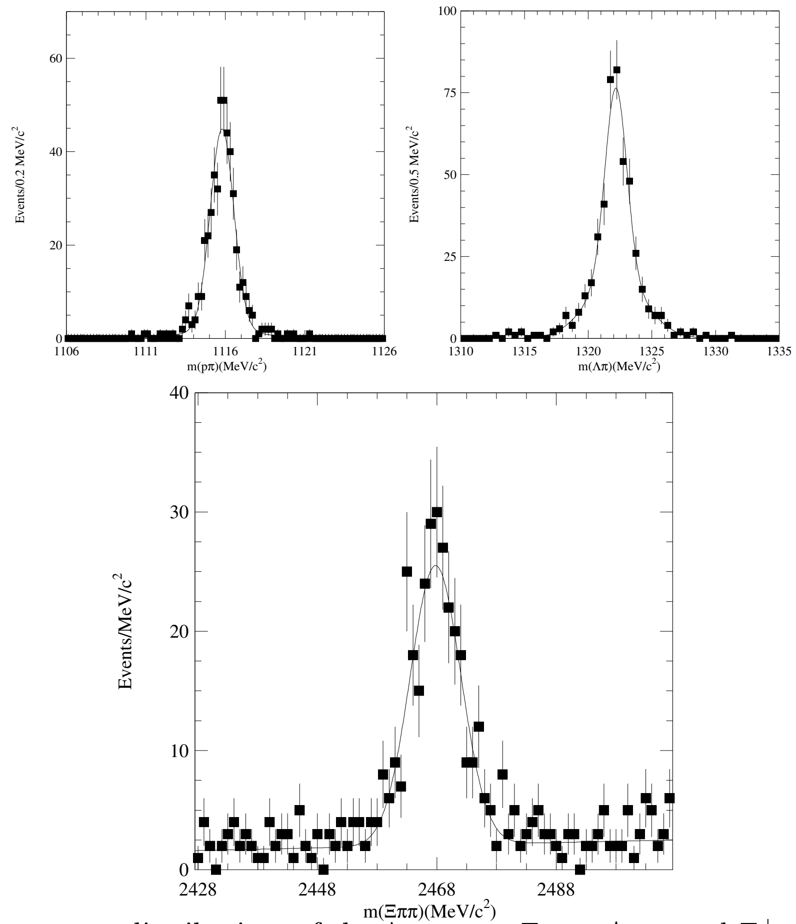

FIG. 1. Invariant mass distributions of the $\Lambda \to p\pi^-$, $\Xi^- \to \Lambda\pi^-$, and $\Xi_c^+ \to \Xi^-\pi^+\pi^+$ candidates used to determine the Ξ_c^+ lifetime.

$$\prod_i \int_0^\infty \left[\underbrace{p_{\mathrm{sig,i}} E(t'|\tau_{\mathrm{sig}})}_{\text{signal fraction}} + \underbrace{(1 - p_{\mathrm{sig,i}}) \left(f_{\tau_{\mathrm{BG}}} E(t'|\tau_{\mathrm{BG}}) + (1 - f_{\tau_{\mathrm{BG}}}) \delta(t') \right)}_{\text{background fraction}} \right]$$
$$\times \left[\underbrace{(1 - f_{\mathrm{mis}} - f_{\mathrm{flat}}) G(t_{\mathrm{i}} - t'|S\sigma_{\mathrm{t,i}})}_{\text{proper time resolution}} + \underbrace{f_{\mathrm{mis}} G(t_{\mathrm{i}} - t'|\sigma_{\mathrm{mis}})}_{\text{mis-measured frac.}} + \underbrace{f_{\mathrm{flat}} G(t_{\mathrm{i}} - t'|\sigma_{\mathrm{flat}})}_{\text{flat frac.}} \right] dt'$$

with the product over all Ξ_c^+ candidates, $G(t|\sigma) \equiv \exp(-t^2/2\sigma^2)/\sqrt{2\pi}\sigma$ and $E(t|\tau) \equiv \exp(-t/\tau)/\tau$.

There are three inputs to the fit for each Ξ_c^+ candidate: the measured proper time, t_{i}, the estimated uncertainty in the proper time, $\sigma_{\mathrm{t,i}}$, and a mass dependent signal probability, $p_{\mathrm{sig,i}}$. The signal probability distribution is obtained from a fit to the Ξ_c^+ mass distribution.

The proper time distribution is parameterized as consisting of signal events with lifetime, τ_{sig}, a fraction, $f_{\tau_{\mathrm{BG}}}$, of background events with non-zero lifetime, τ_{BG}, from charm backgrounds, and the remaining background events with zero lifetime. The likelihood function allows for a global scale factor, S, for the proper time uncertainties. The likelihood function also accounts for events in which the proper time uncertainty is underestimated by fitting for a $\sigma_{\rm mis}$ and fraction, $f_{\rm mis}$ (caused by non-Gaussian multiple scattering, for instance) and also a fraction, $f_{\rm flat}$ of events with a fixed $\sigma_{\rm flat} = 8$ ps to account for proper time outliers.

The unbinned maximum likelihood fit yields a signal lifetime, $\tau_{\rm sig} = 497 \pm 47$ fs. The proper time distribution and the unbinned maximum likelihood fit are shown in Figure 2.

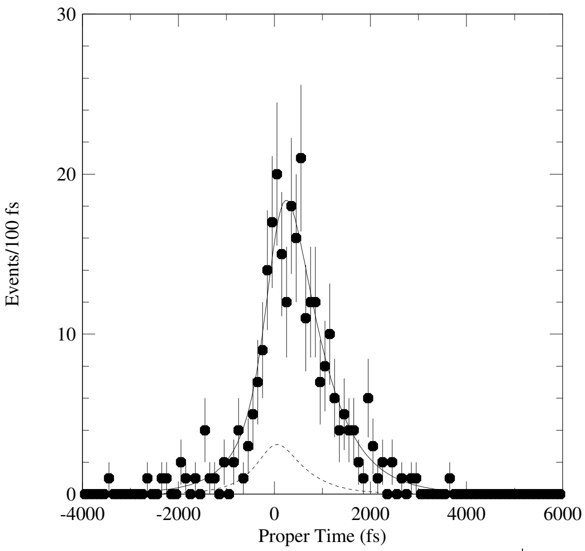

FIG. 2. Proper time distribution of events within $\pm 2\ \sigma$ of the Ξ_c^+ mass peak. The scaled proper time fit (solid line) and scaled background component of the fit (dotted line) are superimposed on the data.

In order to check the consistency of this lifetime result the analysis procedure is repeated as a function of Ξ_c^+ charge, azimuthal angle, polar angle, momentum, silicon detector hit criteria, and data taking period. In all cases the lifetimes are statistically consistent.

IV. SYSTEMATIC ERRORS

The contributions to the systematic error are given in Table I and discussed below.

The uncertainty of the Ξ_c^+ mass could be a source of bias in the lifetime measurement as this mass is used to determine the proper time. The PDG [2] uncertainty of the Ξ_c^+ mass of ± 1.4 MeV/c^2 yields a systematic error contribution of ± 0.3 fs. The systematic bias of the Ξ_c^+ momentum from an incorrect magnetic field could yield a systematic shift in the reconstructed masses. Such a shift would then cause a bias in the lifetime measurement. We estimate this systematic error contribution to be $^{+0.6}_{-0.0}$ fs.

The global detector size and beam pipe geometry is studied to understand their contribution to the systematic error in the lifetime. The results of the study yield a lifetime uncertainty of 0.1% resulting in a systematic error contribution of ± 0.5 fs. The potential bias in the decay length measurement is determined by measuring the average decay length of a "zero-lifetime" sample of $\gamma\gamma \to 4\pi$ events. We measure an average decay length of $0.0 \pm 0.9\ \mu$m and use the uncertainty in this measurement to calculate the contribution to

Contribution	Uncertainty (fs)
Ξ_c^+ mass	± 0.3
Ξ_c^+ momentum	$^{+0.6}_{-0.0}$
global detector size & decay length bias	± 2.5
signal probability	$^{+2.7}_{-3.6}$
proper time outliers	± 3.3
y beam position	± 7
proper time - mass correlation	± 7.2
Monte Carlo statistics	± 9.2
fit mass region	± 10
Total	± 18

TABLE I. Contributions to the systematic error of the Ξ_c^+ lifetime.

the total systematic error. The average of the quotient of 0.9 μm and the $\beta\gamma c$ for each Ξ_c^+ candidate is 2.5 fs. We take this to be the estimate of the Ξ_c^+ proper time bias due to a decay length bias. Adding these two systematic errors in quadrature yields 2.5 fs.

The signal probability, $p_{\mathrm{sig,i}}$, contribution to the systematic error is obtained from differences in the fitted lifetime values when the signal probability is varied by ± 1 $\sigma_{p_{\mathrm{sig,i}}}$. This study yields a systematic error of $^{+2.7}_{-3.6}$ fs.

The proper time outlier contribution is obtained from the maximal difference of lifetimes from the following three methods of accounting for outliers: a) a $\sigma_{\mathrm{flat}} = 8$ ps contribution in the likelihood function (this is the nominal method of accounting for proper time outliers), b) a $\sigma_{\mathrm{flat}} = 16$ ps contribution in the likelihood function, and c) a proper time cut (absolute value) of less than 4 ps and no σ_{flat} contribution to the likelihood function. The maximal difference between these three methods is 3.3 fs which is taken as the proper time outlier systematic error.

The y beam position systematic error estimates the variation in the lifetime when the y beam position is shifted from its true position. Shifting the beam spot location subsequently shifts decay length and proper time measurements. For an infinite data sample in a perfectly isotropic detector, a shift in the y beam position would not affect a lifetime measurement as it would average out to zero. A possible lifetime bias can be estimated by measuring the lifetime after shifting the y beam spot location. The beam spot location is shifted by various amounts, and in the vicinity of zero shift, the slope of the change in lifetime vs. the change in beam position location is 3.5 fs/μm. Multiplying this slope by ± 2 μm, the uncertainty in the y beam position, yields a systematic error of ± 7 fs.

There is a correlation between the measured proper time and reconstructed mass of a charm meson or baryon. This correlation is due to the mis-measurement of the opening angle(s) between the daughter tracks in a short-lived decay. An overestimate of the opening angle(s) tends to bias the measured proper time and mass to larger values of these quantities. In Fig. 3 the average lifetime vs. invariant mass correlation is shown for case of the Ξ_c^+ using both data and Monte Carlo events. There is good agreement in the rate of change in lifetime vs. invariant mass for the two samples. The proper time vs. mass contribution to the systematic error is obtained by multiplying the slope of the lifetime vs. measured $\Xi^-\pi^+\pi^+$ reconstructed mass by the σ of the central mass value. This contribution to the systematic uncertainty is ± 7.2 fs.

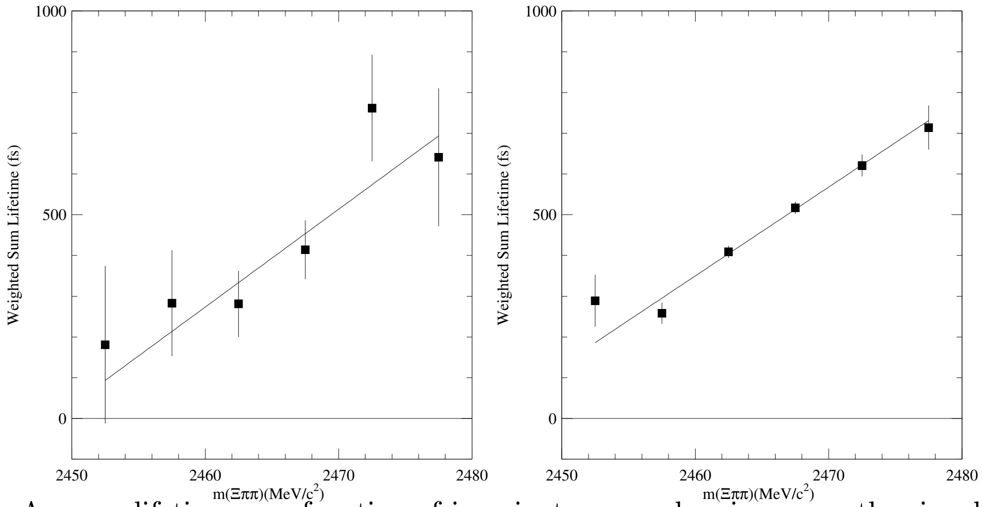

FIG. 3. Average lifetime as a function of invariant mass subregions near the signal region for CLEO II.V data (left) and tagged Monte Carlo events (right). For data and Monte Carlo, the lifetime vs. invariant mass slopes agree with values of 24 and 22 fs/(MeV/c^2), respectively.

In order to check for other sources that could bias the lifetime measurement, e.g. event selection and likelihood function parameterization, a sample consisting of background events extracted from CLEO II.V data and simulated Ξ_c^+ events is studied. The relative amount of signal and background component in the sample is arranged to be the same as that of the full CLEO II.V data set. This data set is run through the full analysis and the Ξ_c^+ lifetime extracted from the maximum likelihood fit is compared with the input lifetime (449.0 fs). This procedure yields a Ξ_c^+ lifetime of 443.2 ± 9.2 fs, 5.8 fs lower than the input Monte Carlo signal lifetime. The statistical uncertainty in this measurement, 9.2 fs, is included as a component of the total systematic error ("Monte Carlo statistics") in Table I. The 5.8 fs difference between the input and output signal Monte Carlo lifetime is applied as a correction to the Ξ_c^+ lifetime value from the CLEO II.V data.

To estimate the systematic error due to the mass range used in the maximum likelihood fit (± 40 MeV/c^2) a study is performed where the mass interval is varied and the lifetime recalculated. A variety of mass intervals are used in the study including narrower intervals (e.g. ± 20 MeV/c^2), wider intervals (e.g. ± 60 MeV/c^2) and asymmetric intervals (e.g. $-60,+40$ MeV/c^2). From the results of this study a systematic error of ± 10 fs is assigned due to the mass region used in the maximum likelihood fit.

The final measured Ξ_c^+ lifetime value (without systematic error) is 502.6 ± 47.3 fs. The total systematic uncertainty of ± 18 fs is obtained by adding all the contributions listed in Table I in quadrature.

V. SUMMARY

A new measurement of the Ξ_c^+ lifetime, $\tau_{\Xi_c^+} = 503 \pm 47(\text{stat.}) \pm 18(\text{syst.})$ fs, has been made using the CLEO II.V detector and 9.0 fb^{-1} of integrated luminosity. This is the first Ξ_c^+ lifetime measurement from an e^+e^- experiment. Many of the contributions to the systematic error in this measurement are different from those of fixed-target experiments. This result is somewhat higher than the current world average, 330^{+60}_{-40} fs. We can combine this result with the recent CLEO II.V measurement [3] of the Λ_c^+ lifetime, $\tau_{\Lambda_c^+} = 179.6 \pm 6.9(\text{stat.}) \pm 4.4(\text{syst.})$ fs to obtain $\tau_{\Xi_c^+}/\tau_{\Lambda_c^+} = 2.8 \pm 0.3$ (statistical error only). This measured ratio is higher than the expectation, ~ 1.3, from the $1/m_c$ expansion calculation of Ref. [1].

VI. ACKNOWLEDGMENTS

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